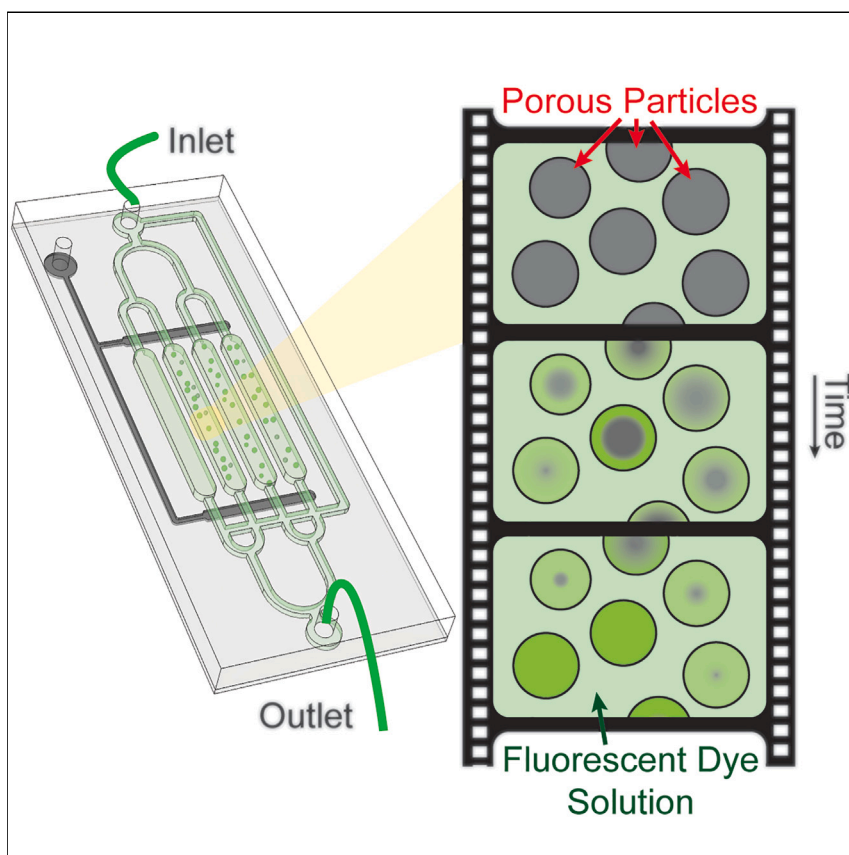


Resource

Accessibility study of porous materials at the single-particle level as evaluated within a microfluidic chip with fluorescence microscopy



This study introduces a novel method to evaluate the surface properties and accessibility of individual porous particles, two parameters that determine their efficiency as adsorbents and catalysts. The approach consists of the use of a multiplexed microfluidic device and a fluorescence microscope to screen the uptake of fluorescent molecules in different particles in a high-throughput fashion. The results showed great interparticle heterogeneities that could not have been resolved with traditional bulk methods.

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Highlights

A new method to study the accessibility of individual porous particles is proposed

A great interparticle heterogeneity (accessibility and surface area) was observed

Suppressing probe-wall interactions revealed accessibility as governed by porosity

Resource

Accessibility study of porous materials at the single-particle level as evaluated within a microfluidic chip with fluorescence microscopy

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SUMMARY

Understanding the mass-transfer phenomena taking place in solid catalysts, batteries, fuel cells, and adsorbents is essential to improve their performances. Uptake experiments of ultraviolet-active or fluorescent probes represent a direct way to provide an accessibility measure of porous particles. We propose a new method to evaluate the accessibility of functional porous materials at the single-particle level. A multiplexed microfluidic device and a fluorescence microscope are employed to assess the uptake of fluorescent molecules in porous particles over time. The device allows for performing multiple uptake experiments in parallel, enabling the comparison of different particles under the same conditions. We showcase the method by studying the diffusion and adsorption properties of a dye in different silica model particles. The approach allows for probing interparticle heterogeneity in accessibility and accessible surface area as well as the dependence of these parameters on electrostatic interactions between the particle and the probe molecules.

INTRODUCTION

Molecular transport is a key aspect in the applications of most functional porous materials, as it determines their performances as adsorbents, batteries, fuel cells, and solid catalysts.¹ The efficiency of these materials depends on the diffusion, adsorption, and desorption processes taking place inside their pores, which are in turn influenced by the physicochemical interactions between the pore walls and the guest molecules.^{1–4} Therefore, understanding these phenomena is essential for designing functional materials with much improved performances.

A direct way for elucidating mass-transfer processes in porous materials is based on uptake and release experiments of ultraviolet (UV)-active^{5,6} or fluorescent probes, directly providing a pore accessibility measure (i.e., how easily molecules enter the porous host). One example of such an approach is offered by the so-called AkzoNobel accessibility index (AAI) test^{4,7,8} introduced for fluid catalytic cracking (FCC) particles, which is also used industrially. The method is based on measuring the uptake of UV-active molecules into catalyst particles by tracking the relative concentration of the molecules in solution over time (Figures 1A and 1B), providing a relative measure of the penetration rate. In this approach, it is assumed that the behavior of the entire system replicates the one of an individual particle. However, structural and compositional differences exist within a catalyst batch^{9,10} that cannot be captured by ensemble-averaged analytical measurements.

THE BIGGER PICTURE

Porous materials find use in diverse industrial applications, from catalysis to environmental remediation. To improve their performance, tools for their precise characterization are required. This includes investigating mass-transfer phenomena taking place therein, along with the interactions between the guest molecules and the host material's pore walls. In this work, we introduce a microfluidic-based method for direct assessment of functional porous particles' accessibility. Using fluorescent probes, we monitor and quantify the uptake of molecules within individual porous particles over time, capturing dynamic processes and heterogeneities often not visible when using traditional bulk techniques. By facilitating real-time, single-particle analysis in a detailed and controlled fashion, our method shows great potential to unravel the mechanisms governing mass transport in porous solids.



Characterizing the uptake process of individual particles would be beneficial to supplement the data obtained from bulk methods and also to capture heterogeneities among particles. This has been tried with different techniques. Recently, confocal laser scanning microscopy (CLSM) has proven to be a useful tool for visualizing the inner structure of materials. It has been applied to monitor the uptake and distribution of dyes^{11–14} and dye-labeled particles^{15,16} on the single-particle scale. The approach allowed a direct visualization of the particle's accessible porosity and the correlation between its structure and activity. This provides useful insight for the design of more efficient materials. Moreover, microimaging techniques based on interference microscopy (IFM) and infrared microscopy (IRM)^{2,17,18} were successfully used for recording the evolution of guest molecule distributions in nanoporous host materials. Furthermore, advanced electron^{19–25} and X-ray^{26–31} microscopy techniques have been applied to (partially) map the pore volume of individual particles in 3 dimensions and to simulate mass transfer within them.

The mentioned analytical measurements require expensive equipment and sample preparation, and some of them are, unfortunately, destructive, particularly due to the potential for ion, electron, and X-ray beam damage, as observed in electron microscopy and synchrotron-based techniques.^{9,32,33} Furthermore, the number of particles that can be studied with these methods is very limited. Recently, microfluidic devices have been used to characterize catalysts at the single-particle level in a high-throughput fashion by isolating catalyst particles based on their activity³⁴ and metal loading.³⁵ However, this kind of approach has not yet been used to study intra-particle mass transport.

Here, we propose a fast, cheap, and reproducible method (Figures 1C and 1D) to compare accessibility between and within different porous particles in a high-throughput fashion. We used only a polydimethylsiloxane (PDMS) multiplexed microfluidic device and an LED-illuminated wide-field fluorescence microscope, and we imaged and compared the uptake of fluorescent molecules by individual mesoporous silica particles. Moreover, we performed experiments using different solution conditions to evaluate the influence of electrostatic interactions between guest molecules and host material on the overall uptake process. Furthermore, by suppressing these interactions, the measured accessibilities were—for the tested samples—able to probe pore size accurately, obtaining a distribution comparable to the results from the N₂ physisorption method. Additionally, the saturation values of the uptake curves allowed us to study changes in accessible surface area as a function of guest-host interactions of individual particles, which cannot be distinguished with bulk and non-chemically sensitive techniques, such as gas physisorption. Finally, we investigated through simulations how internal diffusion, adsorption, and external mass transfer affected the shape of the uptake curves.

The experiments were performed using microfluidic devices consisting of two PDMS layers and a glass slide (Figure S1), as previously reported.^{36,37} The top layer contains four chambers, which allow the performance of three experiments in parallel under the same conditions while keeping a reference chamber to control for photobleaching (Figure 1C). In the experiments, each chamber is loaded with various porous SiO₂ particles. Then, all chambers are filled with water to first fill pores of the hydrophilic material by capillary forces; this process takes place in less than a second.³⁸ Finally, the chambers are filled with a fluorescent dye solution. The mean fluorescence intensity, as a measure of dye concentration in each particle, is tracked individually as a function of time, resulting in individual uptake curves (Figure 1D) constructed from the experimental data using a self-developed MATLAB code. One can get

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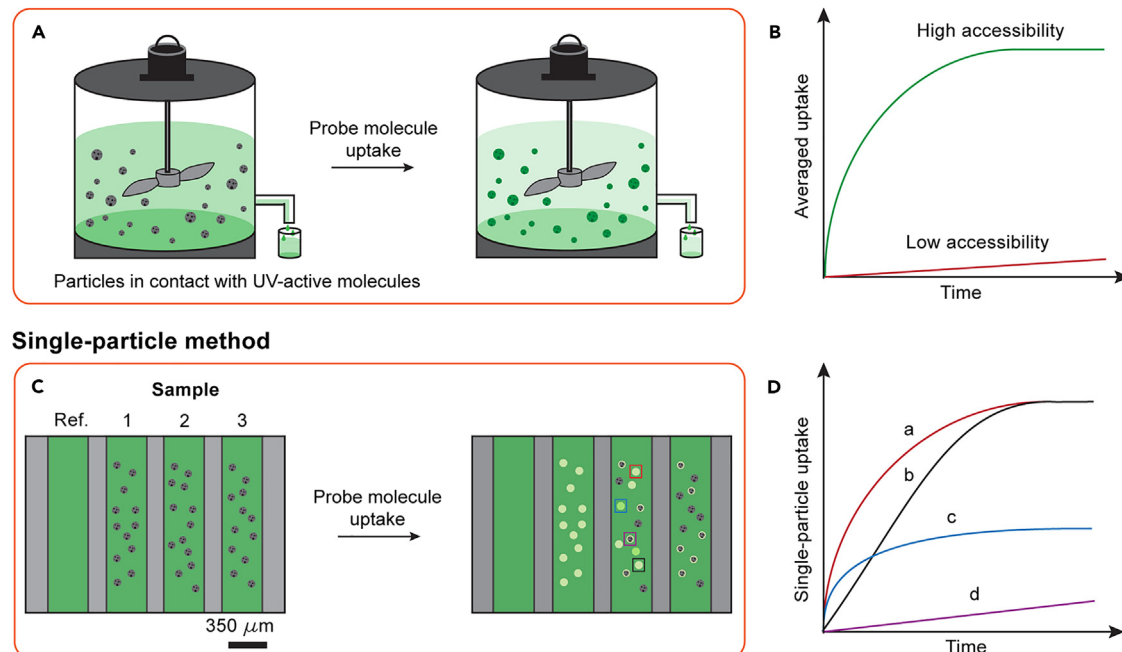
Bulk method

Figure 1. Schematic representation of the experimental methods to evaluate the accessibility of particles in bulk and at the single-particle level

(A) A stirred tank contains both UV-active molecules and porous particles. The concentration in the solution decreases due to the uptake of the porous material.

(B) Based on the concentration change, the bulk uptake (mol/g(material)) is computed and used to characterize the material's accessibility.

(C) A multiplexed microfluidic device containing 4 chambers is filled with porous particles and a liquid containing a fluorescent dye. One reference chamber (left) is left empty to control for photobleaching. As fluorescent molecules enter the porous particles, their fluorescence increases.

(D) The fluorescence of individual particles (in the highlighted squares) is tracked over time to assess the uptake of fluorophores and in turn the accessibility of individual particles. Curves a and b correspond to particles with the same accessible adsorption capacity (both curves plateau at the same value) but different accessibilities ($a > b$). Particle c is rather accessible (saturation is reached quickly), but the total uptake of fluorophores is less than in particles a and b. Particle d corresponds to a particle with very low accessibility (saturation is not reached during the time of the experiment).

information from the following features of these curves: (1) the final value of the curve contains information about the saturation state of the particle. If it is flat, then the equilibrium in the uptake process has been reached (i.e., the particle surface is saturated with dye, and there is no concentration change in the particle pore volume; [Figure S2](#)). Otherwise, uptake is still ongoing. (2) The intensity value reached after saturation contains information about the adsorption properties of the system. The higher this value, the more adsorption took place, which can be related to the surface area of the material. (3) The shape of the curve, i.e., how the curve's slope changes over time, contains information about the accessibility of the particle. The steeper the slope, the faster saturation is reached, and the more accessible the particle is.

Theoretical background

The interpretation of uptake data can be divided into two categories, based on the adsorption or the diffusion as the rate-limiting step. The latter represents the most common case for macroscopic adsorbent materials.^{39,40} Several models have been developed to describe the experimentally obtained uptake curves.⁴¹ However, most of these models require reaching a saturation state to extract the relevant parameters. The so-called intra-particle diffusion model⁴² does not have this requirement and is therefore widely used for slow-uptake experiments. Here, the fractional uptake $q(t)$, usually expressed in mg(probe)/g(solid), is plotted as a function of $t^{0.5}$.^{43–45,45–51,53–66}

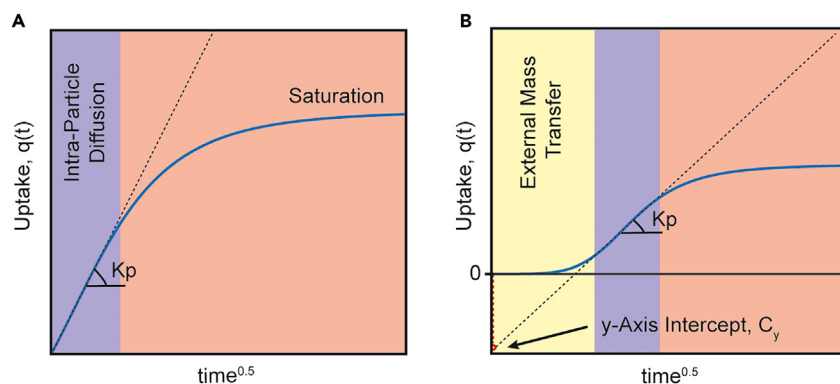


Figure 2. Comparison of uptake curves

Ideal uptake curve (A) with purely intra-particle diffusion and (B) with external mass-transfer contribution.

At low saturation values with an ideal mixing of the liquid phase (i.e., the dye concentration in solution is constant in space), this would initially result in a linear curve that eventually reaches a plateau, representing saturation of the sorbent material (Figure 2A). In the case of prominent external mass-transfer effects (no ideal mixing), a stagnant layer, i.e., a concentration gradient in the vicinity of the particle, is formed during uptake, slowing it down and resulting in a non-linear regime for small time values^{41,61} (Figure 2B). Typically, linear regression is performed on the linear part of the uptake curve (Equation 1), and its slope is used to quantify the so-called intra-particle diffusion rate constant⁶⁷ K_p (mg/g min^{0.5}), which we refer to as accessibility index:

$$q(t) = K_p t^{0.5} + C_y. \quad (\text{Equation 1})$$

The y-intercept C_y (mg/g) is typically used to evaluate the extent of the boundary layer thickness and therefore the external mass-transfer effects. When the fitted line passes through the origin, the external mass transport is negligible. Otherwise, a non-zero y-intercept value indicates a relevant contribution of the boundary layer effects to the measured intra-particle diffusion. Both positive^{43–58} and negative^{59–61} C_y values have been reported in the literature. Positive values are interpreted as fast adsorption by the material; thus, it is not possible to capture the actual starting point of the adsorption process. Negative values are related to a diffusion process retarded by the boundary layer effects. Moreover, some studies use the intercept of the fitted line with the x axis to evaluate external mass-transfer effects.^{62–66} Therefore, the exact physical meaning of the C_y parameter proposed in the aforementioned model remains unclear.

To investigate the significance of the accessibility index K_p and the y-intercept C_y , uptake simulations were performed by solving Fick's second law with the finite-difference method. In our model (supplemental experimental procedures section S3), no flux at the center of the particle and external mass-transfer effects at the particle surface were included in the boundary conditions. Moreover, adsorption was considered to be much faster than the diffusion process, which established diffusion to be the rate-limiting step. As a result, local equilibrium between the diffusing and adsorbed substance can be postulated. To simplify, we assumed a linear dependence between the concentrations of the free and adsorbed substances.

The molecular uptake in porous particles is mostly dominated by three parameters: (1) the internal particle diffusion coefficient D (m²/s), which increases with the pore size and pore interconnectivity; (2) the external mass-transfer coefficient k (m/s),

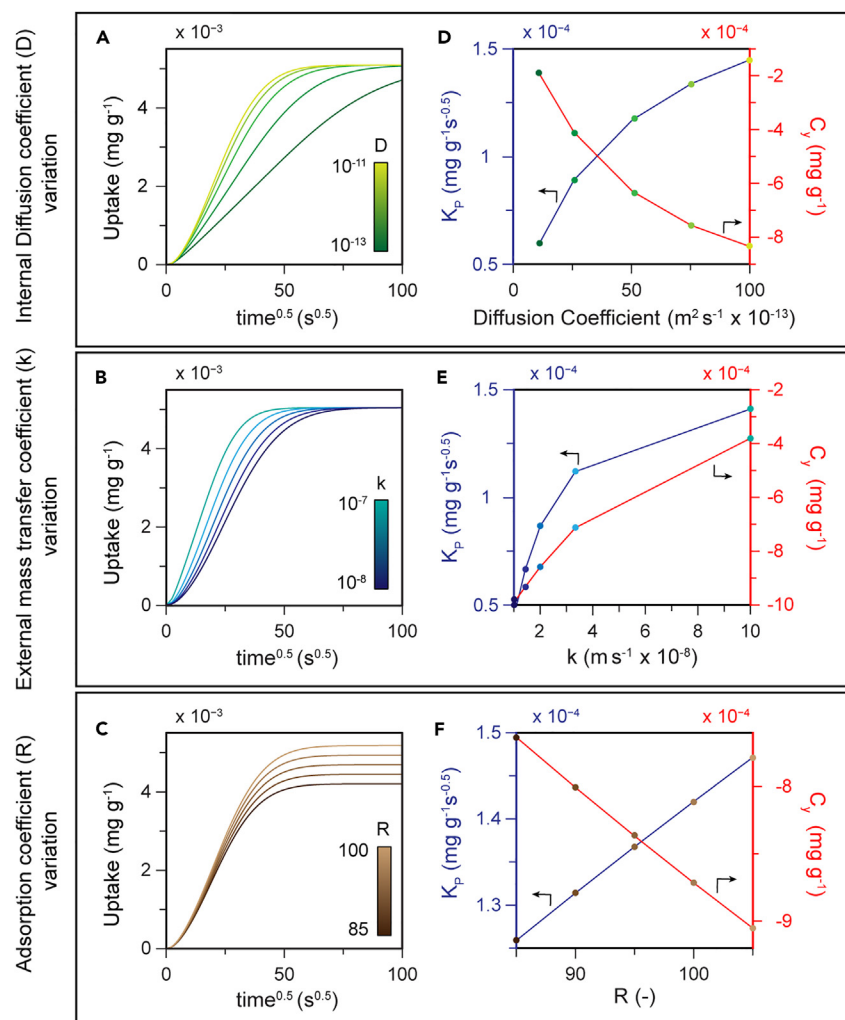


Figure 3. Simulations of uptake curves in a 35 μm spherical particle

(A–C) Uptake curves obtained changing (A) the internal diffusion coefficient D ($k = 10^{-8}$ m/s and $R = 100$), (B) the external mass-transfer coefficient k ($D = 10^{-12}$ m²/s and $R = 100$), and (C) the adsorption coefficient R ($D = 10^{-12}$ m²/s and $k = 10^{-8}$ m/s).

(D–F) The slopes (accessibility indices) and y intercepts of the inflection point tangents of the uptake curves shown in (A)–(C), respectively.

which depends on diffusion and convection outside the particle and correlates positively with D (supplemental experimental procedures section S3, Equation S7); and (3) the adsorption coefficient R (unitless proportionality constant expressing the ratio between adsorbed concentration and concentration in solution, supplemental experimental procedures section S3, Equation S2). The latter depends on the wall-molecule interactions as well as the number of accessible adsorption sites.

We performed a sensitivity analysis (Figure 3) to assess how these three parameters affect the uptake curve shape and its parameters K_p and C_y . Increasing the internal diffusion coefficient D of the particle resulted in a higher slope of the linear part of the uptake, i.e., higher accessibility index K_p , and a more negative y axis intercept C_y (Figures 3A and 3D). A similar effect on K_p is observed by increasing k (reducing the external mass-transfer limitations). However, it also shifts the linear regime of the uptake curve to shorter times, which results in a less negative y intercept (Figures 3B

and 3E). Finally, increasing the adsorption coefficient R increases the accessibility index K_p and decreases the y-intercept C_y (Figures 3C and 3F). It is worth noting that the external mass-transfer coefficient k and the effective diffusion coefficient $D' = \frac{D}{1+R}$, which includes adsorption, are positively correlated due to the boundary conditions equating flow at the two sides of the solid-liquid interphase (supplemental experimental procedures section S3, Equation S7). Hence, increasing the internal particle diffusion coefficient D will result in higher external mass transport (higher k), and vice versa. However, both parameters contribute differently to the y axis intercept C_y . Since the y axis intercept is determined by several parameters, it should not be used to evaluate external mass transfer only.

In an uptake experiment, while using particles of the same material and pore volume but different pore sizes, one varies the internal diffusion coefficient D and therefore the external mass-transfer coefficient k as well as the adsorption coefficient R (as different surface areas are obtained). All of these values correlate positively with the amount of adsorbed material (uptake, $q(t)$) and the accessibility index K_p . Interestingly our experimental results show that the accessibility index and the y axis intercept are correlated (Figure S3), proving the redundancy of using both parameters to characterize porous materials. Therefore, we will provide only the accessibility index K_p values obtained in the experiments to characterize and compare the processes.

RESULTS AND DISCUSSION

To showcase the developed method, we used SiO_2 particles with almost monodisperse pore-size distributions (i.e., 50, 35, and 23 nm) (Figures 5A and S4) often used as catalyst supports (e.g., olefin polymerization catalysis). Rhodamine 110 (Rh110) (Figure 5B) was used as a fluorescent probe due to its photostability,^{68,69} high quantum yield, and fluorescent intensity being proportional to its concentration (Figure S5A). Therefore, particle fluorescent intensity values were directly used to obtain the uptake curves (Figures S5B and S6), and the accessibility index was defined in $\text{min}^{-0.5}$ units. The particles were placed in the chambers, leaving one empty, which was used as a reference to check the photostability of the dye (Figure 1C). Uptake experiments were conducted for 5 h, and images were acquired every minute. Figures 4A and 4B display a cropped version of the fluorescence microscopy images recorded at the beginning and end of the experiments using 50 nm pore-size particles showing an overall, but heterogeneous, increase in intensity. Some particles of similar size display an intensity (i.e., concentration) gradient within them, whereas others show a more homogeneous dye distribution, hinting toward different pore connectivity. The final mean fluorescence intensity of the particles was higher than in the bulk solution due to the adsorption of the probe molecules in the pore structure. Figure 4C shows the mean intensities of particles of the same sample as a function of time (the initial intensity of each particle was subtracted). Even particles that belong to the same batch differ strongly in their uptake curves and, therefore, their accessibilities. Traditional bulk experiments could not have measured this, which highlights the importance of the proposed method for elucidating interparticle heterogeneity. Plotting the same uptakes versus $t^{0.5}$ results in a sigmoid-like (asymmetric sigmoid) curve (Figure 4D). The non-linear beginning of the curve suggests external mass-transfer limitations. That is, a concentration gradient is formed outside the particle that slows the internal diffusion down. Moreover, the fact that the curves are reaching a plateau means that, as expected, at some point in time, the particles are starting to get saturated with dye.

Apart from varying the pore size of the particles to compare the uptake rates, we evaluated how the guest-host electrostatic interactions reflected upon the overall uptake

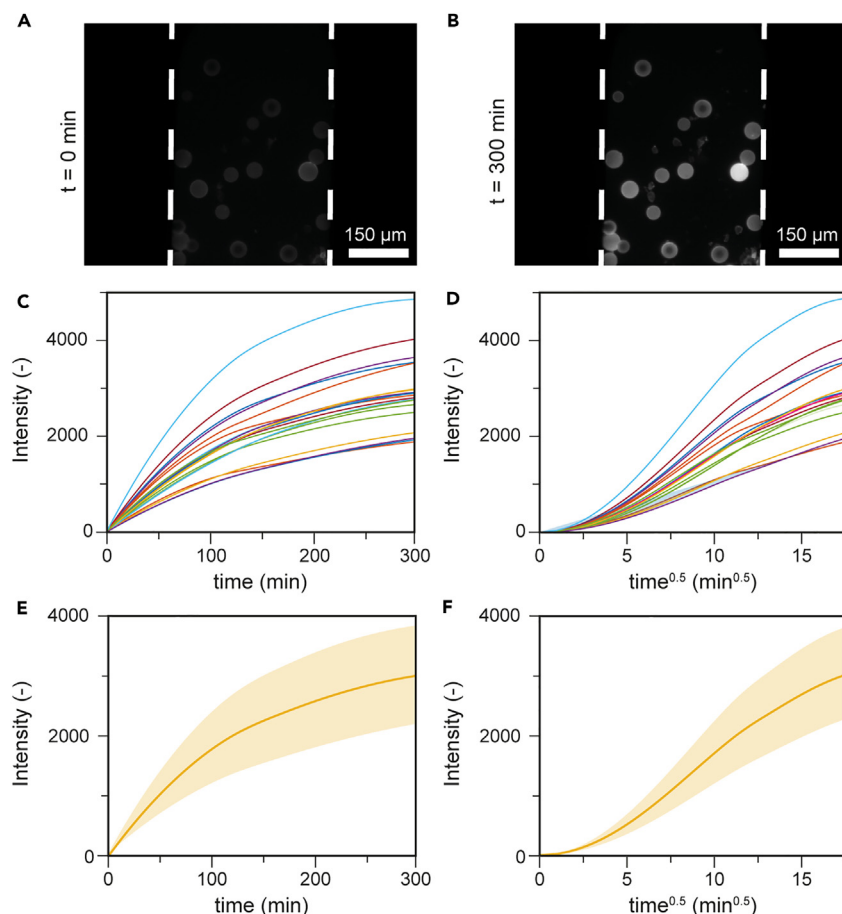


Figure 4. Example of on-chip uptake experiment and analysis of silica particles

(A and B) Zoomed-in and cropped fluorescence microscopy image of the microfluidic chamber containing silica particles with 50 nm pores at the (A) beginning and (B) end of the experiment. Scale bar: 150 μm .

(C) Uptake curves of particles shown in (A) and (B).

(D) Uptake curves are linearized when plotted over $t^{0.5}$.

(E and F) show the mean uptake curves obtained from the ones in (C) and (D). The shaded area represents the standard deviation of all particles considered (n = 18).

process. These interactions were tuned by using solutions at different ionic strength or pH. The pH affected the charge of the dye⁷⁰ and the pore-wall surface charge density, but its fluorescence properties remained unchanged (Figure S7). In the case of silica, higher pH results in more negative surface charge density.⁷¹ The ionic strength of the solution influences the extent of the electrical double layer (EDL), a region where the liquid is not electroneutral because it contains a high concentration of counterions attracted by an oppositely charged surface.⁷² If the characteristic length of the EDL (commonly called the Debye length) is greater than the pore radius, then there is an overlap between the EDLs extending from opposite surfaces in the pores (schematically shown in Figure 5C), which slows down or even prevents the entrance of (probe) molecules with the same charge as the counterions due to electrostatic repulsion.

We performed experiments using three different solutions: (1) pH = 4.3, (2) pH = 4.3 and 0.01 M NaCl as supporting electrolyte, and (3) pH = 7 (Figures 5C–5E). Solutions 1 and 2 have the same pH but different ionic strengths ($1.3 \cdot 10^{-4}$ and $9.4 \cdot 10^{-3}$ mol/L,

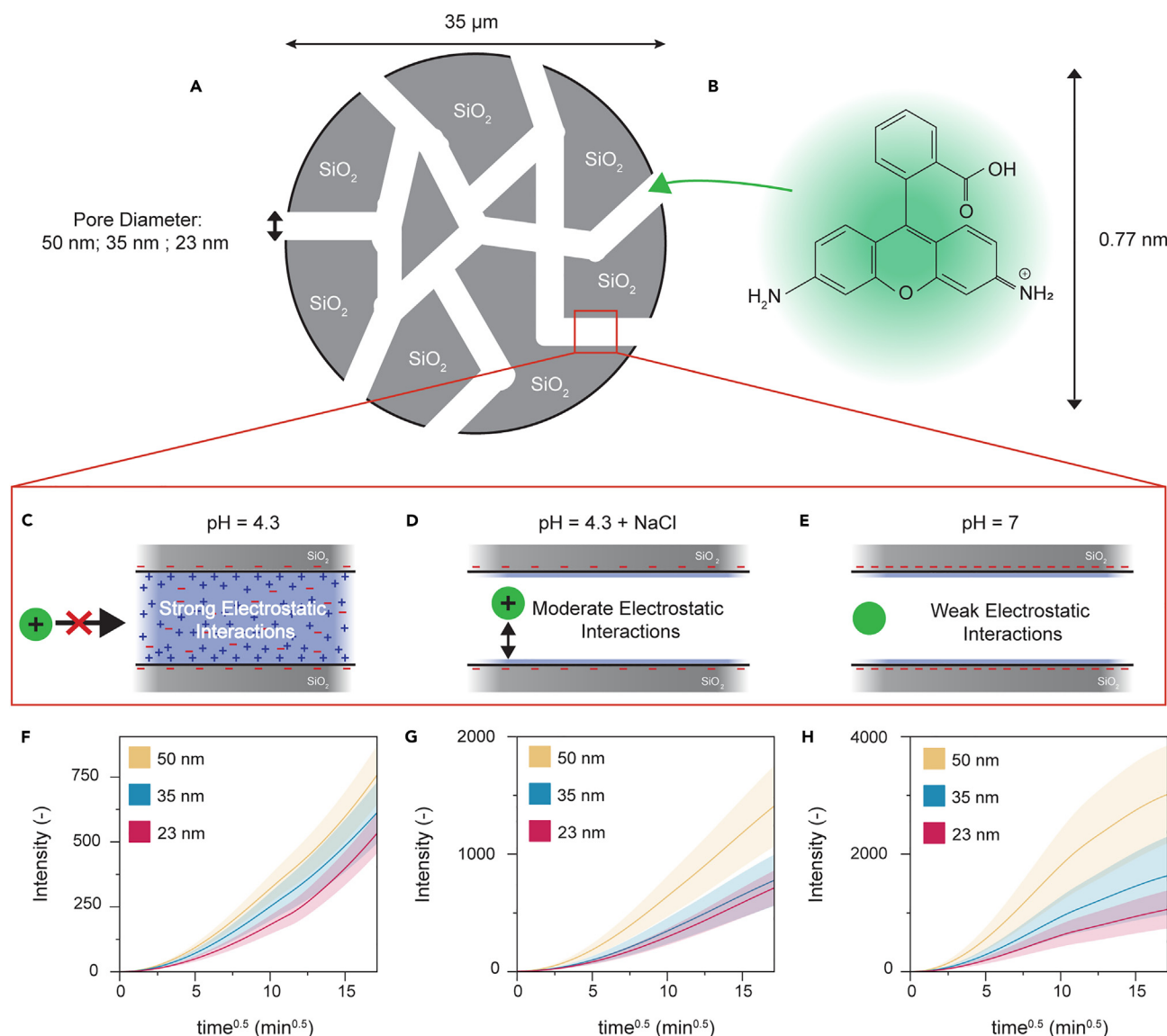


Figure 5. Schematic of electrostatic interactions and uptake curves results in silica particles with various pore sizes and solution conditions

(A) Silica particles (diameter: 35 μm) with almost uniform pore-size distributions. Three pore sizes were used: 50, 35, and 23 nm. (B) Rh110 chemical structure. Rh110 has a hydrodynamic diameter of 0.77 nm and is positively charged when solved in water.⁷⁸ (C–E) Schematic of electrostatic interactions between Rh110 and the negatively charged pore walls under different conditions: (C) pH = 4.3, a cationic EDL overlap (blue shaded area) is present inside the pore, which repulses the Rh110(+); (D) pH = 4.3 and 0.01 M NaCl, increasing the ionic strength reduces the Debye length and creates a neutrally charged region within the pore that allows Rh110(+) to enter the pore more easily; and (E) pH = 7, the surface charge density of the pore walls is more negative. However, Rh110(\pm) is neutrally charged, so no main probe-wall electrostatic interactions are present. (F–H) Uptake curves corresponding to the conditions described in (C)–(E), respectively. Decreasing the electrostatic interactions has 2 effects on the uptake curves: it speeds up the process, and it also increases the differences between samples as the pore size gradually becomes more relevant (note the difference in the y axis scale).

respectively), which translate into different Debye lengths (26 nm in solution 1 and 3 nm in solutions 2 and 3) (supplemental experimental procedures section S6). On the other hand, solutions 2 and 3 have the same ionic strength (Debye length) but different pH. The solutions used in the experiments have a pH above the silica isoelectric point (pH \sim 2).⁷³ Therefore, the oxide surface hydroxyls are deprotonated, and the silica surface is negatively charged.⁷⁴ For all solutions, the uptake speed increased as a function of

pore size, and they all seem to be affected by external mass transfer, as they show a non-linear regime at low $t^{0.5}$ values (Figures 5F–5H). However, mass transfer varied dramatically for the different conditions. Solution 1 (pH = 4.3) displayed the slowest uptake, with its linearized curve not reaching an inflection point and showing only small differences between samples with different pore sizes (Figure 5F). The linearized uptake curve of solution 2 (pH = 4.3 and 0.01 M NaCl) reached the inflection point, showing moderate differences based on pore size (Figure 5G). Solution 3 (pH = 7) proved to be the fastest with respect to uptake and showed signs of saturation (i.e., the linearized uptake curve surpassed its inflection point) and the largest differences between the different porous silica samples (Figure 5H).

This behavior can be explained by the electrostatic interactions of the different systems: solution 1 (pH = 4.3) causes Rh110 and silica to be positively⁷⁰ and negatively charged,⁷³ respectively. Moreover, due to the low ionic strength of the system, an overlapping EDL (Debye length: 26 nm > r_{pore}) predominantly containing cations is formed in the vicinity of the pore walls, which interacts with the incoming Rh110(+) repulsively, slowing the diffusion process down (Figures 5C and 5F). Solution 2 (pH = 4.3 and 0.01 M NaCl), with higher ionic strength, results in a smaller Debye length (3 nm), leading to milder repulsive electrostatic interactions between the EDL and the guest molecules as well as faster mass transport (Figures 5D and 5G). Similar Debye length effects of pore diffusion have been reported previously.^{75–77} Solution 3 (pH = 7) has the same ionic strength as solution 2 (pH = 4.3 and 0.01 M NaCl) and therefore a comparable Debye length. Moreover, at pH = 7, while silica has a higher negative surface density,⁷² Rh110 forms zwitterions due to the deprotonation of the carboxyl group, and the amino group carries a positive charge.⁷⁰ Therefore, the guest-host electrostatic interactions are the lowest in this case, which results in a faster uptake and saturation (Figures 5E and 5H). As the strength of electrostatic interactions decreases (Figures 5C–5E), the pore size and structure become more dominant for the uptake process. This explains why we observe small, moderate, and large uptake differences between pore sizes in solutions 1, 2, and 3, respectively, in our experiments (Figures 5F–5H).

Figure 6A shows the obtained accessibility index distribution for different particles and wall-probe electrostatic interactions. The accessibility was evaluated from the slope of the uptake curve inflection point tangent (Figure S8). It is worth mentioning that this analysis approach cannot be used if the first derivative of the uptake curve does not reach a maximum during the experiment (i.e., the curve has no inflection point). The experiments performed with solution 1 (pH = 4.3) do not meet this criterion and cannot be analyzed in this fashion. As qualitatively described by the uptake curves, the accessibility index decreases with pore size, and the differences are more pronounced for solution 3 (weak electrostatic interactions). The difference between 35 and 23 nm for solution 2 (moderate electrostatic interactions) falls within the error bar of the measurement. At pH = 7 (weak electrostatic interactions), however, the measurement remains sensitive to these differences. Therefore, by suppressing the probe-wall electrostatic interactions, it is possible to probe accessibility as dominated by the pore structure (pore size and shape). This becomes clear if one compares the accessibility index distribution at pH = 7 (Figure 6B) with the pore-size distribution obtained with N₂ physisorption (Figure 6C). Note that both distributions show a significant overlap of the 35 nm sample with both the 23 and the 50 nm samples. Further, the relative peak positions are similarly distributed with respect to each other.

To investigate the adsorption behavior of the system, the fluorescence of individual particles was measured and compared after 2 weeks of uptake to ensure that saturation was

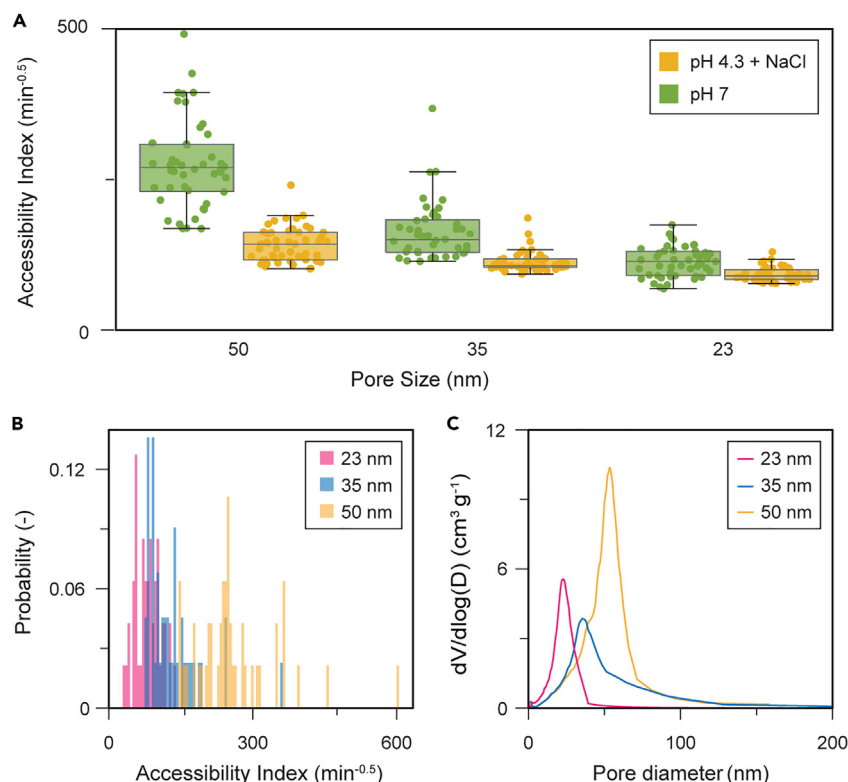


Figure 6. Comparing accessibility and pore-size distributions of silica particles

(A) Comparison of accessibility index distribution of silica particles with different pore sizes (50, 35, and 23 nm) obtained by performing the experiments with fluorescent solutions at different pH but with the same ionic strength. The number of particles analyzed is ~ 50 . At pH 7, the accessibility was higher, as there are less electrostatic interactions.

(B and C) The accessibility index distribution at pH = 7 (B) and the pore-size distribution (C) exhibit similarities in terms of relative peak positions and overlapping features. The pore-size distribution was determined through N_2 -physisorption measurements using Barrett-Joyner-Halenda (BJH) analysis of the desorption branch. The Brunauer-Emmett-Teller (BET) surface areas were ~ 523 (23 nm sample), ~ 439 (35 nm sample), and ~ 344 m^2/g (50 nm sample).

(C) The pore-size distributions obtained from N_2 physisorption.

reached (Figure 7). For all evaluated conditions, the same trend could be observed for the pore size: the equilibrium intensity, and therefore the equilibrium concentration, increases as the pore size decreases. All model particles have roughly the same total porosity ($\sim 30\%$). If the total porosity is constant, then the surface area available for adsorption decreases as a function of pore size. This explains why the amount of adsorbed Rh110 increases when particles with smaller pores are probed—intensity therefore directly correlates with surface area (BET results; [supplemental experimental procedures section S4](#)). Nevertheless, the amount of adsorbed Rh110 also seems to depend strongly on the conditions used for the experiment. Interestingly, when Rh110 is neutrally charged (pH = 7, solution 3), the saturation intensity values are the lowest, even though these conditions showed the fastest diffusion (Figures 5H and 6A). This can be explained by the weak attractive electrostatic interactions between the probe and the walls. On the other hand, in the case of solution 1 (pH = 4.3), Rh110 and the silica walls have opposite charges, which results in a higher amount of probe electrostatically adsorbed on the walls after reaching equilibrium. Despite the repulsive electrostatic interactions between the EDL and Rh110 that slow diffusion down (Figure 5F), after long time periods, the Rh110 molecules eventually cross the predominantly positively charged EDL and adsorb

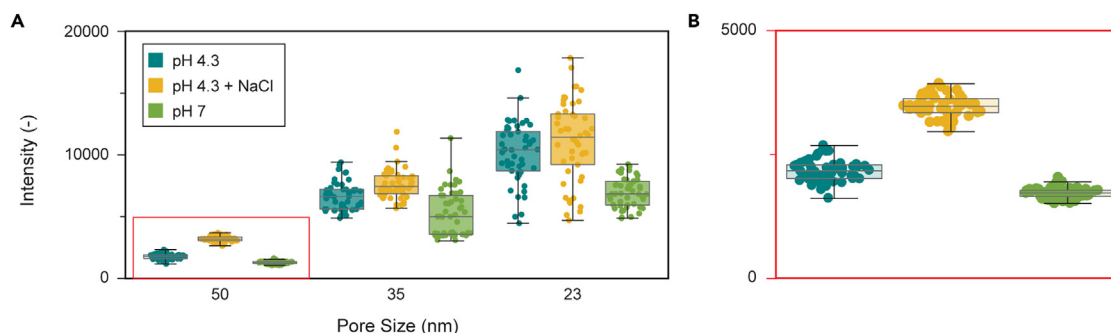


Figure 7. Fluorescent intensity distribution of silica particles after saturation in different solution conditions

(A) Distribution of mean fluorescent intensities of the silica model particles under different conditions after reaching saturation. Smaller pores result in higher saturation intensities, as they imply larger surface areas. At pH = 7, the equilibrium concentrations are the lowest since Rh110(\pm) is neutrally charged and less attracted to the silica walls. At pH 4.3, silica(–) and Rh110(+) have opposite charges resulting in higher saturation concentrations. Adding salt to the pH = 4.3 solution decreases the Debye length to the point where there is no EDL overlap. Pores connected through narrow bottlenecks with high EDL overlap become accessible, as the pore entrance is no longer fully occupied by positively charged ions. Therefore, the total accessible porosity increases compared to the case of pH 4.3. As a result, the available surface area and the saturation concentrations increase as well. (B) Zoomed-in image of red rectangle in (A). The boxplots display the median and the lower and upper quartiles as well as non-outlier minima and maxima.

on the negatively charged pore walls. If the Debye length is reduced by adding salt (solution 2, pH = 4.3 + NaCl), then the interactions with the EDL are substantially reduced, and the uptake is accelerated (Figure 5G). Interestingly, the final amount of adsorbed species in this case is even larger than for solution 1 (pH = 4.3). We assume that this is because some regions of the pore space of the particles remain inaccessible when a large EDL is present. This would be the case for regions connected through narrow bottlenecks where the EDL overlap is the highest, impeding Rh110 from accessing the whole-particle void volume. Compared with N₂ physisorption, which provides a single BET surface area for an ensemble of particles, our method, on the other hand, delivers individual particle information. Furthermore, N₂ physisorption provides the accessible surface area under specific (inert) conditions, while our method can be applied under varying probe-host electrostatic interactions and is sensitive to them. This could be potentially exploited to determine the accessible surface area for a specific guest molecule (e.g., differently sized molecules within a catalyst particle). Moreover, the porous silica particles used in this study are, as mentioned above, commonly impregnated with metallocenes as active centers and used as olefin polymerization catalysts.⁷⁹ The chemosensitivity of our effective surface area measurements could be used to characterize silica support particles regarding their impregnation potential.

Conclusions

A novel analytical method to study the accessibility of individual porous particles in a high-throughput fashion was proposed and showcased using reference silica particles. From the conducted experiments, the following conclusions could be drawn: (1) particles from the same batch showed great heterogeneity in terms of accessibility and number of accessible adsorption sites, which could not have been resolved with traditional bulk analytical methods. (2) The probe-wall electrostatic interactions proved to be of paramount importance for mass transfer and adsorption within mesoporous materials. (3) Therefore, conditions where these interactions are suppressed were employed to probe particles' accessibility as dominated by porosity. The pore-size probing sensitivity of our approach was similar to the one obtained with N₂ physisorption. (4) Evaluating the saturation intensities proved to be suitable for studying surface area at the single particle level. Contrary to gas physisorption methods, where the results are independent of the surface chemistry, our method can be used to study the changes in accessible surface area as a function of the probe-host interactions, which could be used to study catalyst support

impregnation. (5) Two linearized uptake curve parameters were found to be relevant for this kind of experiment: the accessibility index and the saturation intensity. The y axis intercept, typically reported in mass-transfer studies, proved to be redundant, as it strongly correlated with the accessibility index. Our validated method should be used to conduct uptake experiments using different probes and complex porous materials. Moreover, modifications to the microfluidic device can be made in order to make it compatible with organic solvents, expanding the application to the use of hydrophobic dyes and particles.

EXPERIMENTAL PROCEDURES

Full experimental procedures are provided in the [supplemental information](#).

Resource availability

Lead contact

Further information and requests for resources should be directed to and will be fulfilled by the lead contact, Florian Meirer (f.meirer@uu.nl).

Materials availability

This study did not generate new unique reagents.

Data and code availability

All data reported in this study are available upon request from the lead contact.

SUPPLEMENTAL INFORMATION

Supplemental information can be found online at <https://doi.org/10.1016/j.checat.2023.100791>.

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AUTHOR CONTRIBUTIONS

Conceptualization, F.M., A.B., L.C., R.M.-G., and M.O.; investigation A.B., L.C., R.M.-G., and J.M.D.; formal analysis, A.B., L.C., and R.M.-G.; writing – original draft, A.B., L.C., and R.M.-G.; writing – review & editing, all authors; funding acquisition, B.M.W., F.M., M.O., and W.O.; supervision, B.M.W., W.O., M.O., and F.M.

DECLARATION OF INTERESTS

The authors declare no competing interests.

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