Layer effects on the magnetic textures in magnets with local inversion asymmetry

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Magnets with broken local inversion symmetries are interesting candidates for chiral magnetic textures, such as skyrmions and spin spirals. The property of these magnets is that each subsequent layer can possess a different Dzyaloshniskii-Moriya interaction (DMI) originating from the local inversion symmetry breaking. Given that new candidates of such systems are emerging, with the Van der Waals crystals and magnetic multilayer systems, it is interesting to investigate how the chiral magnetic textures depend on the number of layers and the coupling between them. In this article, we model the magnetic layers with a classical Heisenberg spin model where the sign of the DMI alternates for each consecutive layer. We use Monte Carlo simulations to examine chiral magnetic textures and show that the pitch of magnetic spirals is influenced by the interlayer coupling and the number of layers. We observe even-odd effects in the number of layers where we observe a suppression of the spin spirals for even layer numbers. We give an explanation for our findings by proposing a net DMI in systems with strongly coupled layers. Our results can be used to determine the DMI in systems with a known number of layers and for new technologies based on the tunability of the spiral wavelength.

I. INTRODUCTION

The role of electronic devices in society is ever increasing, and there is a need to make them smaller and faster, whereas keeping a low-power consumption. However, the current technologies are reaching their limits since the information density cannot be increased much further. Therefore, new technologies need to be developed. One of the most promising new technologies for data processing and storage are magnetic systems with chiral textures, such as chiral magnetic domain walls and skyrmions [1–5]. Their chiral and topological properties make for sturdy textures which can become extremely small, this makes them suitable for applications. An example of such a design is the skyrmion-racetrack memory, which is a promising route for fast and energy efficient memory and processing devices [6–8].

At the moment, a plethora of systems is known to host skyrmionic textures, such as the chiral magnet MnSi which hosts so-called Bloch skyrmions and ultrathin ferromagnetic films which typically host Néel skyrmions [9–17]. These thin magnetic films are formed by stacking multiple layers of different metals, and the order of these layers determine their magnetic properties. Furthermore, a new class of suitable materials is emerging: The Van der Waals crystals. These crystals consists of two dimensional layers of one atom thick, stacked on top of each other via Van der Waals bonds [18,19]. Two-dimensional layers can be exfoliated from bulk materials, such as graphite, hexagonal boron nitride and CrI_3 [18,20,21]. Because of the freedom to stack different kinds of materials, the end product is tunable and can be formed such that the desired properties are present in the end product with virtually

no strain since the weak interlayer bonds make them less sensitive to lattice mismatch problems.

In this article, we demonstrate how a local DMI arising from a local inversion asymmetry can give rise to chiral structures even in materials with global inversion symmetry. DMI is an interaction formed when strong spin-orbit coupling and broken inversion symmetry are present. An example of such symmetry breaking is the interface between two different materials, such as Co and Pt [22,23]. The DMI is also referred to as antisymmetric exchange since the interaction picks up a minus sign when exchanging two spins. Because of this property, the interaction leads to chiral magnetic textures. One example of chiral magnetic textures is spirals with a preferred turning sense [either clockwise (CW) or counterclockwise (CCW)] which are formed by DMI in the absence of fields and anisotropies. Here, we note that a local DMI can arise in crystal possessing global inversion symmetry, but which show a local inversion asymmetry (as drawn in Fig. 1). This allows for a DMI term to be nonzero locally whereas averaging out when the complete infinite crystal is taken into account This is analogous to the "hidden spin-polarization" effect that occurs because of local inversion symmetry breaking and was elucidated in Ref. [24] and experimentally verified in Van der Waals crystals [25–28]. We are interested in magnets where this local DMI has an alternating nature of its sign in subsequent layers. Especially, we are interested in materials with (anti)ferromagnetic coupling between the layers. To comply with this condition, Van der Waals crystals need to have bulk inversion symmetry, layer inversion asymmetry, magnetism, and high spin-orbit coupling. An example of a Van der Waals material meeting these criteria is Fe_3GeTe_2 [19], which
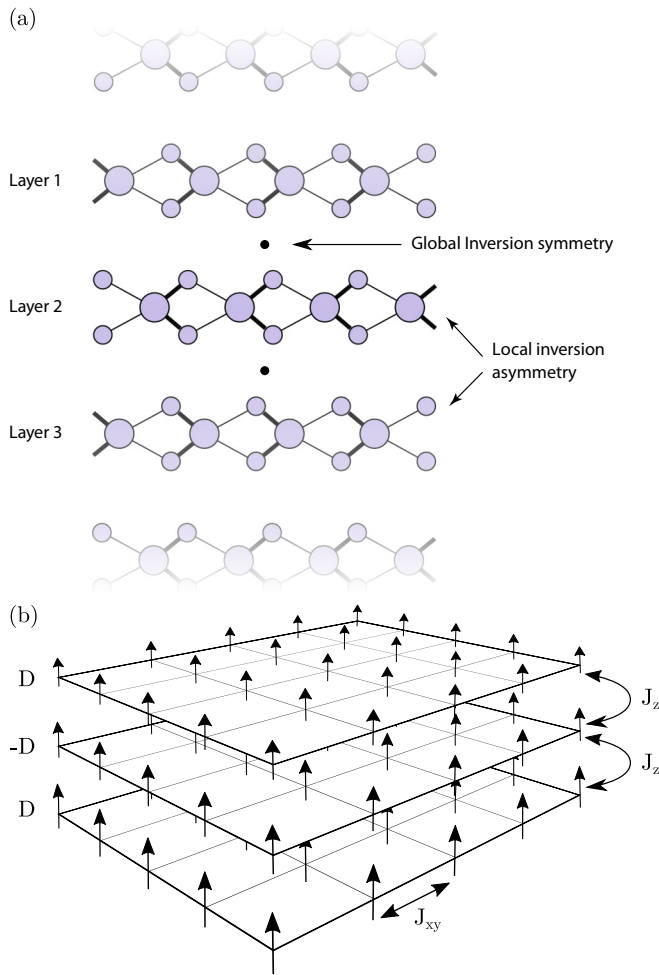
(a)

(b)

FIG. 1. Schematics of (a) a bulk crystal with a global inversion symmetry whereas showing local inversion asymmetry and (b) the model used in our simulations. Here, the arrows are Heisenberg spins and can rotate freely in three dimensions, J_{xy} is the intralayer coupling, J_z is the interlayer coupling, and D is the DMI.

belongs to the space-group $P6_3/mmc$ [29] in its bulk form and point-group D_{3h} in its monolayer form [30]. The condition of local inversion asymmetry in a globally inversion symmetric system can also be obtained in sputtered metallic thin films, such as Ta/Co/Pt/Co/Ta systems making it even easier to perform such DMI engineering [31].

In this article, we discuss how a locally nonzero DMI influences magnetic textures. We show what different textures form and find that these chiral textures occurring in the system are influenced by the stacking of the layers. The resulting spin spiral wavelength and their turning sense are affected by the interlayer coupling relative to the DMI. Furthermore, we find that the number of layers influences the wavelength of the spin spirals in the system, and an even-odd effect is found for the number of layers in the system. The tunability of the spin spirals suggests that skyrmions will also be tunable in their size. The tunability of the spin spiral wavelength and turning sense demonstrate the potential of DMI engineering for new magnetic devices. Moreover, since spin spiral systems can develop skyrmions upon applied magnetic fields, our results also serve as a basis for the design of skyrmionic devices.

The remainder of this paper is organized as follows. In Sec. II, we discuss our model and how the simulations are performed. After this, we show results of our simulations in Sec. III, where we focus on the phase diagram, wavelength, and turning sense found in the system with an odd number of layers. This is compared in Sec. III to systems with an even number of layers. Finally, we conclude with an outlook in Sec. IV.

II. MODEL AND METHOD

To model a stack of coupled ferromagnetic layers, we describe them with a classical Heisenberg spin model. Each layer is modeled by equally spaced spins on a square lattice. This is performed for simplicity and is a decent approximation since we are modeling temperatures far below the Curie temperature and are interested in smooth textures, such as spin spirals. The layers are placed right on top of each other as shown in Fig. 1(b), and each layer has an alternating sign for the DMI strength. We assume that the leading interactions within the layers are ferromagnetic nearest-neighbor exchange and DMI. The leading interaction between the layers is assumed to be nearest-neighbor exchange varying from the ferromagnetic to the antiferromagnetic regime. We note that these conditions are met for various Van der Waals crystals as well as for metallic thin-film heterostructures with Ruderman-Kittel-Kasuya-Yosida (RKKY) coupled layers.

We describe the Hamiltonian H with separate terms for the intra- and interlayer terms,

$$H = H_{\text{intra}} + H_{\text{inter}}. \tag{1}$$

The interactions within the layers are expressed as follows:

$$H_{\text{intra}} = -J_{xy} \sum_{\alpha=1}^{N} \sum_{\mathbf{r}} \mathbf{S}_{\mathbf{r}}^{\alpha} \cdot \left(\mathbf{S}_{\mathbf{r}+\hat{\mathbf{x}}}^{\alpha} + \mathbf{S}_{\mathbf{r}+\hat{\mathbf{y}}}^{\alpha} \right)$$
$$+ \sum_{\alpha=1}^{N} (-1)^{\alpha-1} D \sum_{\mathbf{r}} \left(\mathbf{S}_{\mathbf{r}}^{\alpha} \times \mathbf{S}_{\mathbf{r}+\hat{\mathbf{x}}}^{\alpha} \cdot \hat{\mathbf{y}} - \mathbf{S}_{\mathbf{r}}^{\alpha} \times \mathbf{S}_{\mathbf{r}+\hat{\mathbf{y}}}^{\alpha} \cdot \hat{\mathbf{x}} \right), \tag{2}$$

where J_{xy} is the intralayer coupling, D is the Dzyaloshinskii-Moriya interaction, $\mathbf{S}_{\mathbf{r}}^{\alpha}$ is the spin at position $\mathbf{r}$ in layer $\alpha = 1, 2, \ldots$ and $\hat{\mathbf{x}}$ and $\hat{\mathbf{y}}$ are the unit vectors in the the x and y directions, respectively. The number of layers is denoted with N and the $(-1)^{\alpha}$ term regulates the alternating DMI sign in the system. The interactions between the layers are described by

$$H_{\text{inter}} = -J_z \sum_{\alpha=1}^{N} \sum_{\mathbf{r}} \mathbf{S}_{\mathbf{r}}^{\alpha} \cdot \mathbf{S}_{\mathbf{r}}^{\alpha+1},$$

where J_z is the intralayer coupling.

To investigate the ground state of this model, we use Monte Carlo simulations. We begin the simulation by taking a random spin configuration at a high temperature. Then, we use the Metropolis algorithm to thermalize the system [32,33]. This algorithm picks a random spin and proposes a new semi-random direction. This new direction is such that the average acceptance ratio is 50%, which is determined from the energy difference between the new and the old spin configuration:
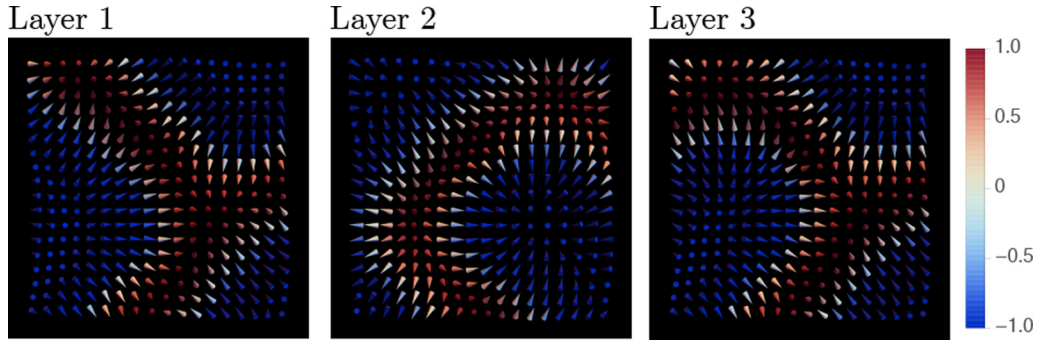
FIG. 2. Snapshot of a 32×32 cut out of a three-layer 128×128 spin system with $J_z/J_{xy} = 0.10$ and $D/J_{xy} = 0.50$. The color red indicates that a spin is pointing upwards and blue downwards. Spin spirals are clearly visible, and the sign of the DMI has a clear effect on the turning sense [counterclockwise for layers 1 and 3 and clockwise for layer 2].

ΔE. The acceptance probability $\mathcal{P}$ is then $\mathcal{P} = \exp(\Delta E/k_B T)$ if $\Delta E < 0$ or $\mathcal{P} = 1$ in all other cases. Finally, we accept or reject this new direction with a probability of 0.5. When the system is fully thermalized, we decrease the temperature and repeat this thermalization and lowering of the temperature until the temperature gets close to zero and approaches the ground state. We start our simulations at $k_B T/J_{xy} = 10$, where k_B is the Boltzman constant and T is the temperature. To this end, the temperature is lowered by a factor of 0.95 until $k_B T/J_{xy} = 0.01$.

III. RESULTS FOR ODD NUMBER OF LAYERS

For low temperatures, we expect that magnetic textures will form in the ferromagnet. The DMI leads to the formation of a chiral spiral inside the layer and, depending on the sign of the DMI, the turning sense of the spiral should be different in each subsequent layer. The size of the spiral should be influenced by the relative strength between the DMI and the intralayer coupling terms (D/J_{xy}). We performed simulations for varying parameters of DMI (D/J_{xy}) and interlayer coupling (J_z/J_{xy}), and systems with sizes varying between

32×32 spins and 256×256 spins. We find that the systems thermalize and form a stable state where a clear chiral spiral pattern is visible. In Fig. 2, we show snapshots of such a system with chiral spirals. We performed simulations for a varying number of layers, and, in this part of the article, we will discuss systems with an odd number of layers. The even number of layer systems are discussed later in Sec. III.

A. Phases and phase diagram

The magnetic structures in our systems will be determined by the competition among the three terms in the model: The intralayer coupling, which favors the alignment of the spins inside the layer, the DMI, which leads to a chiral spiral inside of the layer, and the interlayer coupling, which favors the (anti-)alignment of the spins between the layers.

Our simulations show six prominent magnetic phases. The first two phases are the fully polarized phases where the interlayer exchange is dominant, i.e., $|J_z|/J_{xy} \gg D/J_{xy}$. Here, no magnetic structure appears, all spins are always aligned inside the layer. For a negative interlayer exchange J_z, the layers are antiferromagnetically (AFM) oriented with respect to each other, this is in contrast with a positive interlayer exchange where the layers are oriented ferromagnetically (FM). A cartoon of this is shown in Fig. 3(a) Ia for $J_z > 0$ and Ib for $J_z < 0$. The next two phases, phases IIa and IIb, are obtained by increasing the DMI and magnetic spirals start to form. Here, the DMI term is non-negligible when compared to J_z. We have observed this for all finite nonzero values of D/J_{xy}. Since the interlayer coupling is still fairly large compared to the DMI in this phase, the system behaves, such as the complete system possesses a single "net" DMI value, and all spirals have the same turning sense as is shown in Fig. 3(a) IIa and IIb. Important to note, here, is that the system we consider in this section is still inversion asymmetric due to the odd number of layers which does allow for a net DMI to be present. Furthermore, the sign of the interlayer coupling J_z determines the relative orientation of the layers, here, as well. The difference is shown in Fig. 3 IIa for FM and IIb for AFM orientation between the layers. The last two phases are where the DMI is dominant and since the sign of the DMI is alternating, the turning sense of the spirals is also alternating in subsequent layers. As is drawn in Fig. 3(a) IIIa and IIIb. Here, the interlayer exchange is only present to regulate the relative
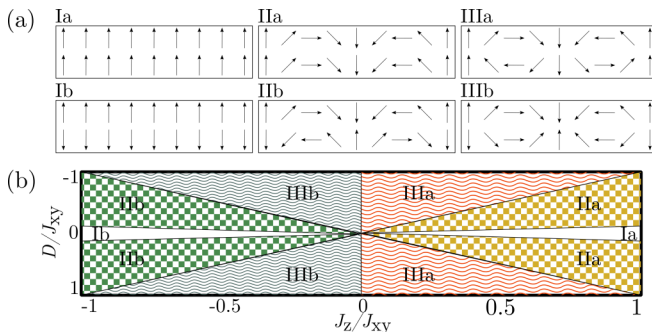

FIG. 3. (a) Cartoon of two coupled spin layers corresponding to the phases described above. (b) Phase diagram of an odd multilayer system. Phases Ia and Ib correspond to the FM and AFM polarized phases, respectively, phases IIa (FM) and IIb (AFM) to the interlayer coupling dominant phase and phases IIIa (FM) and IIIb (AFM) to the DMI dominant phase. The phase diagram is determined with help from the second layer of a five layers system with 256×256 spins with a DMI between 1 and -1 and a J_z/J_{xy} between 1 and -1.
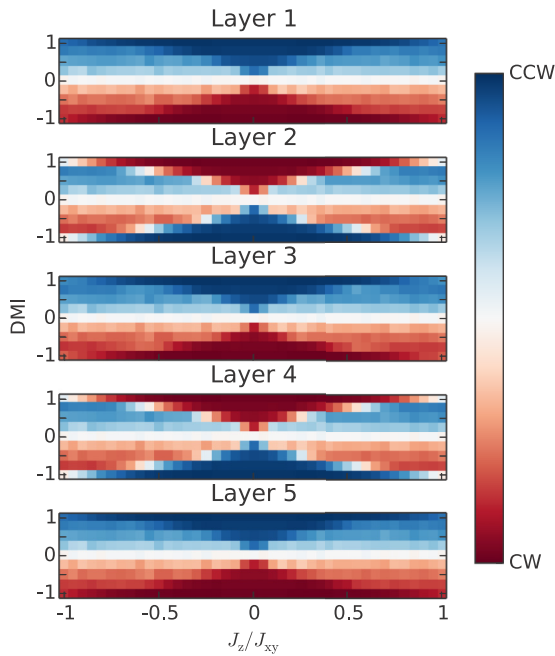
FIG. 4. Average turning sense in each layer. To calculate this average turning sense each spin is given a value of ± 1 corresponding to the orientation with respect to their neighboring spin, finally an average of all these values is calculated. A value of $+1$ corresponds to a CW turning sense and -1 to a CCW turning sense. This is plotted for five layers of 256×256 spins with a DMI between 1 and -1, and a J_z/J_{xy} between 1 and -1.

orientation of the layers. The snapshot in Fig. 2 is taken in the DMI dominant phase (IIIa), an counterclockwise turning sense is visible in layers 1 and 3 and a clockwise turning sense in layer 2. In Fig. 3(b), we plot the phase diagram where these three phases occur for different values of DMI and interlayer coupling.

In Fig. 4, we show the average turning sense for a system with five layers. We determined this turning sense by looking at the average value of turning direction between two neighboring spins C_{TS}, which we defined by

$$C_{TS} = \text{Sgn}[(\mathbf{S_r} \times \mathbf{S_{r+\hat{x}}}) \cdot \hat{y}],$$

where our reference vector $\hat{y} = (0, 1, 0)$, is the unit vector along y. A positive C_{TS} corresponds to a CW orientation between the spins, and negative C_{TS} corresponds to a CCW orientation. The total average value of all turning directions gives an indication of how the spiral is oriented in the layer on average. In Fig. 4, the fully polarized phases Ia and Ib are clearly visible as the white region where $D/J_{xy} = 0$ and no turning sense is present. For increased DMI, a nonzero average turning sense is visible, corresponding to phases IIa and IIb. In each subsequent layer, the turning sense has the same direction. Increasing the DMI even further, we find phases IIIa and IIb, and this is clearly visible in Fig. 4. There is a stronger turning sense, and each subsequent layer switches the turning sense following the sign of the DMI. In layers 2 and 4, a right (left) turning sense is found for a negative (positive) value of D/J_{xy} instead of a left (right) turning sense.

The only difference between ferromagnetic ($J_z > 0$) and antiferromagnetic ($J_z < 0$) interlayer couplings is is the relative orientation of the layers. For the rest, all plots in Fig. 4(b) are symmetric around J_z/J_{xy}. We can explain this from looking at Fig. 4(a) IIa and IIb, here, we see that the ferromagnetic coupled layers have aligned spirals, and the antiferromagnetic coupled layers have antialigned spirals. This difference can be described as a phase shift between the spirals of half a wavelength. Furthermore, for Fig. 4(a) IIIa, the spins pointing perpendicular to the layer are aligned between the layers, but due to the alternating nature of the DMI, the parallel pointing spins are antialigned. In Fig. 4(a) IIIb the opposite is true: The perpendicular spins are antialigned, but the parallel spins are not. This contrast makes that there is no noticeable energy difference between the ferromagnetic and the antiferromagnetic cases.

B. Wave vector

In this section, we will focus on the wave vector of the spirals found in phase IIa/b and IIIa/b. The wave vector is defined by the number of cycles a spiral forms per spin and is determined by the ratio of DMI and intralayer exchange coupling. A higher ratio leads to a shorter spiral period and, thus, a larger wave vector. We expect that the competition between the DMI and the interlayer coupling has significant effects on the spirals since two coupled spirals with different turning senses cannot be coupled such that all spins are aligned. In Fig. 3(a) III, it is visible that the interlayer coupling between the two spirals gives a different energy contribution per spin: A favorable energy contribution for the vertically aligned spins and an unfavorable one for the horizontal antialigned spins. It is impossible to shift the spirals relative to each other such that the interlayer coupling is favorable for all spins. The wave vector will be the largest where the interlayer coupling is not present. Here, with $J_z/J_{xy} = 0$, the wave vector is the same as a single layer system and goes to zero where the interlayer coupling is much larger than the DMI.

In Fig. 5, we show the wave vector for constant DMI, D/J_{xy} ranging from 0 to 1, and varying interlayer exchange. A big variation in the wave vector is found between small and large interlayer exchanges. The wave vector for the large interlayer exchange is around one-fifth the size of the wave vector for the small interlayer exchange. The drop off between these two cases corresponds to the phase transition in the phase diagram between phases IIa/b and IIIa/b. Thus, we see that phase IIa/b has a larger wave vector than phase IIIa/b. Also, here, there is no clear distinction visible between the ferromagnetic and the antiferromagnetic interlayer couplings. To examine the distance between the different cases of D/J_{xy} in Fig. 5, we plot the wave-vector dependence on the DMI for different values of interlayer coupling J_z/J_{xy} in Fig. 6. Here, we see that the relation between DMI and wave vector without any interlayer coupling is linear, but for increasing interlayer coupling, this linearity is not found since the wave vector is dependent on the different phases of the system.

Since the wave vector is influenced by finite-size effects, we used a finite-size scaling to determine the true wave vector. For this, simulations were preformed for systems with system size 64×64, 128×128, and 256×256, and we
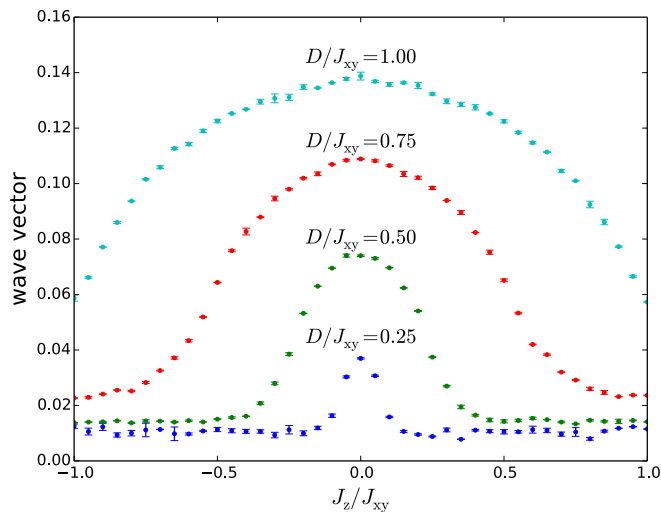
FIG. 5. Wave vector for various values of DMI plotted for a range of interlayer coupling for a five-layer system. A small wave vector corresponds to a larger spiral wavelength.

extrapolated the wave vector linearly in $1/L$. An example of a plot with different system sizes and the resulting true wave vector is shown in Fig. 8. In the inset, we show one of the data fits we used to determine the wave vector. The wave vector is determined as the average distance to the origin for all pixels in a two-dimensional Fourier transform that are more then five standard deviations above the mean of all pixels in a layer, divided by the system size.

C. Influence of the number of layers

We investigated the wave vector for systems with three, four, and five layers. In this section, we are focusing on systems with an odd number of layers only. See Fig. 7 for a comparison between two systems with three and five layers.
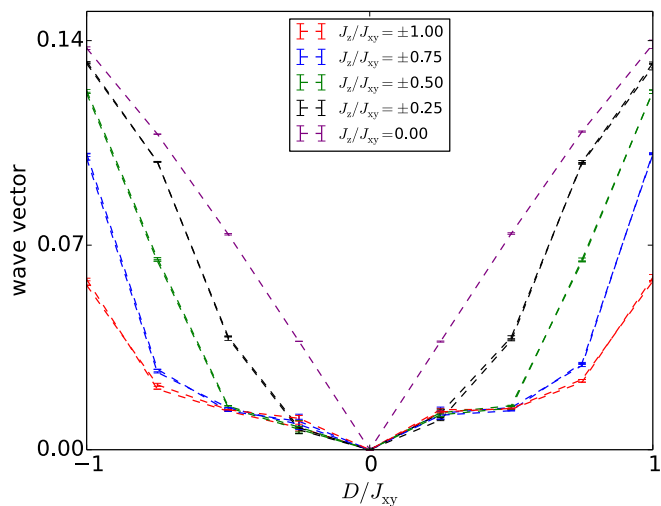

FIG. 6. Wave vector for various values of interlayer coupling plotted for a range of DMI for a five-layer system corresponding to Fig. 5. It is visible that the linear behavior of the wave vector is affected by the interlayer coupling.
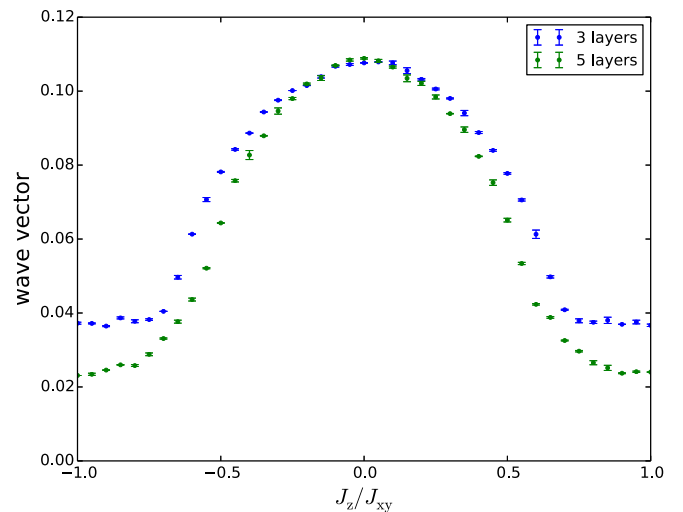

FIG. 7. Comparison of the wave vectors of a system with three layers and a system with five layers. Both layers are plotted for a DMI of $D/J_{xy} = 0.75$. A drop off between 2.6 and 3.2 is visible in the three-layered system and between 3.3 and 5.3 in the five-layered system.

It is visible that the drop off is larger for a larger number of layers. Examining the ratio between the long wavelength in the DMI dominant phase and the shorter wavelength in the interlayer coupling dominant phase, we find two effects. First, this ratio is roughly 3 for a system with three layers and around 5 for a system with five layers. Our hypothesis is that the sum of the DMI divided by the number of layers gives a net DMI for strong interlayer coupling. At $J_z/J_{xy} = 0$, the layers are completely decoupled and behave as individual
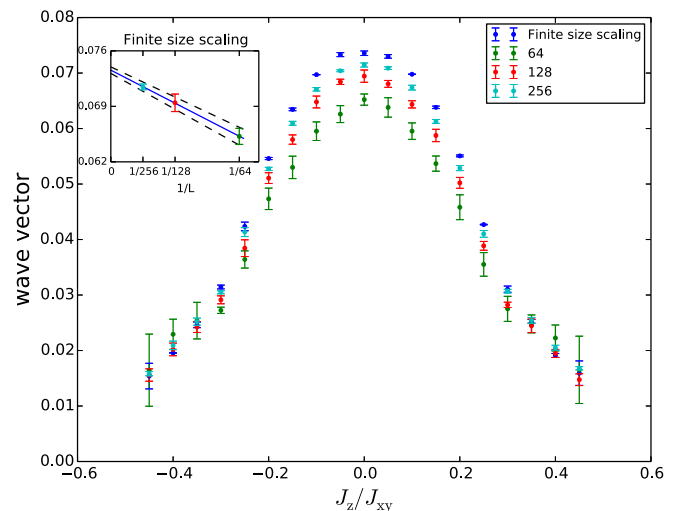

FIG. 8. Wave vector plotted against interlayer coupling J_z/J_{xy} for a system with four layers and a DMI of $D/J_{xy} = 0.50$. Different system sizes 64×64, 128×128, and 256×256 are plotted, and a finite-size scaling made with a linear fit in $1/L$ is added. The inset shows the finite-size scaling for $J_z/J_{xy} = 0$. Here, we only show the results smaller than $|J_z/J_{xy}| < 0.5$ since the finite-size scaling did not work above this value.

TABLE I. Table of the ratio between the wave number in the DMI dominating phase IIIa/b and the phase IIa/b in a three-layer system. Columns are for D/J_{xy} and rows for the different layers in a system. This is for a three-layer system. The ratio is determined for $J_z/J_{xy} = \pm 1$ and $J_z/J_{xy} = 0$. The results for $D/J_{xy} = \pm 1$ are omitted in this table because this strong the interlayer coupling must be stronger than the intralayer coupling to reach phase IIa/b.

D/J_{xy}	-0.75	-0.50	-0.25	0.25	0.50	0.75
Layer 1	2.88	2.96	2.66	2.82	3.14	2.88
Layer 2	3.00	3.04	2.69	2.75	3.24	3.01
Layer 3	2.91	2.95	2.60	2.74	3.13	2.89

layers. Here, the net DMI in each individual layer is exactly D/J_{xy}. As we increase J_z, the interlayer coupling leads to a "dilution" of the DMI, and, at very large interlayer coupling, the system behaves as a system with a single DMI value, given by the sum of the DMI in each individual layer divided by the number of layers. As the number of layers increases, the DMI gets divided by an increasing number, Therefore, leading to a decrease in the net total DMI and a reduction of the observed wave vector. Because of the alternating DMI, the total sum of the DMI is D leading to a net DMI $D_{net} = D/3$ for three layers and $D_{net} = D/5$ for five layers. This is only a rough approximation which works within 10% of the ratio. Second, the precise ratio of the layers themselves shows a pattern. There is a symmetry, the two outermost layers have the same ratio, whereas the inner layer has a different ratio. For example, in a five-layered system, the second and fourth layers have the same ratio, and there is a symmetry around the middle layer. This hints to a richer structure between the layers. We show the ratios in Table I and Table II for which we used a system with $J_z/J_{xy} = \pm 1$ for the wave vector of a interlayer coupling dominating phase and the values at $J_z/J_{xy} = 0$ as the DMI dominating phase.

D. Results for even number of layers

When a thin ferromagnet with local inversion asymmetry has an even number of layers, the sum of the total DMI will

TABLE II. Table of the ratio between the wave number in the DMI dominating phase IIIa/b and the phase IIa/b in a five-layer system. Columns are for D/J_{xy}, and rows are for the different layers in a system. This is for a five-layer system. Our approximation of D_{net} breaks down at $D/J_{xy} = \pm 0.25$ where the ratios are much smaller. The ratio is determined for $J_z/J_{xy} = \pm 1$ and $J_z/J_{xy} = 0$. The results for $D/J_{xy} = \pm 1$ are omitted in this table because this strong the interlayer coupling must be stronger than the intralayer coupling to reach phase IIa/b.

D/J_{xy}	-0.75	-0.50	-0.25	0.25	0.50	0.75
Layer 1	4.47	4.65	3.37	3.25	5.21	4.57
Layer 2	4.65	4.77	3.38	3.34	5.31	4.60
Layer 3	4.56	4.68	3.40	3.29	5.28	4.59
Layer 4	4.66	4.77	3.37	3.27	5.34	4.63
Layer 5	4.51	4.64	3.44	3.24	5.21	4.51

be zero, i.e., D_{net} will be zero. Thus, in the ferromagnetic dominant phase, we expect to observe no spin spirals. This is, indeed, the case. In Fig. 8, we plot the wave vector of a system with four layers. In the DMI dominant phase, we still find spin spirals with a wave vector of 0.07 inverse lattice spacings, which is comparable to the odd layered case. However, in the interlayer coupling dominate phase, the wave vector drops to the predicted 0. Unfortunately, the finite-size scaling breaks down in this regime and gives noisy results, and to prevent confusion, we decided not to show the noisy results. To ensure that the wave vector is, indeed, zero, we examined qualitatively all snapshots of the systems where $|J_z/J_{xy}| < 0.5$. Here, we, indeed, see that no spin spirals are present in the interlayer dominating region. However, we observe localized spin textures, a region where the spins are oriented differently from the rest of the polarized system. These are formed by thermal fluctuations around the nucleation temperature and are stabilized by the DMI which is still present. This is a metastable state, but due to the higher number of local minima in the phase space, our Monte Carlo simulations do not reach the global minimum. By comparing these textures to uniform magnetized textures, we found that these artifacts have a higher energy and are, thus, not representative for the ground state. The error bars for these structure also indicate the volatility of these textures and indicate that they are not the ground state.

IV. CONCLUSION, DISCUSSION, AND OUTLOOK

In conclusion, we presented results on the behavior of spin textures in ferromagnets with a local inversion asymmetry between the layers which leads to alternating DMI for consecutive layers. We found strong effects for the chiral spiral textures originating from the DMI. Furthermore, we were able to distinguish three different phases: The polarized phase, the DMI-dominant phase, and the interlayer coupling-dominant phase. The interlayer coupling-dominant phase has shown different behaviors for the number of layers in a system by influencing the wavelength of the spirals and shown a strong difference between odd and even numbers of layers in a system.

In this paper, we used a minimal model. Future research can be focused to include additional magnetic effects known to influence textures, such as anisotropy, dipole-dipole interactions, and an external magnetic field. Although the finite-size scaling of our results gives a good indication of the expected wave number and a maximum system size of 256×256 spins is still efficient to simulate, more certainty in the wave number is possible with larger system sizes. More computations can also be used to test our hypothesis of the net DMI that occurs in coupled layers. A higher number of layers should continue the trend reported in this paper. Furthermore, the phase diagram in this paper gives a direction to where the different phases occur, a more detailed version can be achieved by simulations for more parameters. The small energy scales and high number of metastable states of chiral systems makes it difficult for Monte Carlo simulations to reach the ground state. By performing multiple simulations and finding comparable spin configurations, we are convinced

that our results are close to the ground state and are representative of the ground state itself.

Our results shown here demonstrate that rich magnetic structures can be obtained through local DMI engineering. First, as a useful method to measure the Dzyaloshinskii-Moriya interaction in Van der Waals ferromagnets or multilayer ferromagnets with a broken local inversion symmetry. When the number of layers and coupling between the layers is known, the DMI can be determined by looking at the spiral wave vector in the upper layer. Second, possible applications that need the ability to tune spiral wavelength or even completely turn off spin spirals. This can be achieved by changing the coupling between the layers, e.g., through applying pressure a Van der Waals material [34,35] or by changing the spacing layer in a RKKY-coupled metallic stack. Third, our results serve as a prelude to investigating skyrmions in Van der Waals magnets. Moreover, an addition of an external magnetic field should lead to the formation of skyrmions.

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