

## FEASIBILITY OF PHOTOVOLTAIC-THERMOELECTRIC HYBRID SYSTEMS

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**ABSTRACT:** Outdoor performance of photovoltaic (PV) modules suffers from elevated temperatures. Conversion efficiency losses of up to about 25% can result, depending on the type of integration of the modules in the roof. Cooling of modules would therefore enhance annual PV performance. Instead of module cooling we propose to use the thermal waste by attaching thermoelectric (TE) converters to the back of PV modules, to form a PV-TE hybrid module. Due to the temperature difference over the TE converter additional electricity can be generated. Employing present day thermoelectric materials with typical figure of merits ( $Z$ ) of  $0.004 \text{ K}^{-1}$  at 300 K may lead to efficiency enhancements of up to 23% for roof integrated PV-TE modules, as is calculated by means of an idealized model. The annual energy yield would increase by 14.7%-11%, for two annual irradiance and temperature profiles studied, i.e., for Malaga, Spain, and Utrecht, the Netherlands, respectively. As new TE materials are being developed, efficiency enhancements of up to 50% and annual energy yield increases of up to 24.9% may be achievable. The developed idealized model, however, is judged to overestimate the results by about 10% for practical PV-TE hybrids.

**Keywords:** Modelling; Solar cell; Thermoelectric converter; Energy performance.

## 1 INTRODUCTION

Outdoor performance of photovoltaic (PV) modules or panels suffers from the high temperatures reached under high irradiation conditions in combination with the negative temperature coefficient of efficiency. Depending on integration type temperatures of panels can reach 60-80 °C, resulting in a loss in efficiency of about 20%, see, e.g., Drews [1]. Cooling of the PV panels would enhance their (annual) performance. However, active cooling systems based on either air or water do not only need electric power to operate the cooling system but also waste the transferred heat into the environment. The latter is also the case for passive cooling systems that do not require electric power as input. In contrast to such systems, thermoelectric (Peltier) cooling elements attached to the back of a PV panel could make use of the either heated air or water. This is particularly interesting for concentrated PV concepts. Cooling of PV cells under concentrated sunlight has been reviewed by Royné *et al.* [2].

It has been reported that the heat produced in the PV panel can be used for heating of water, thereby cooling the PV panel. Such a micro combined heat and power ( $\mu$ CHP) unit usually is denoted as a PVT (PV-Thermal) panel [3], and the total efficiency of a PVT panel is larger than the sum of the efficiencies of a separate PV panel and a solar thermal collector on a per unit area basis.

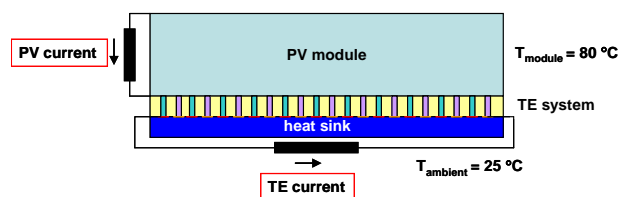
The temperature difference with ambient temperature can be used to generate additional power using the thermoelectric (TE) effect, so to reach a larger overall efficiency of a so-called PV-TE hybrid system [4-7]. In this way, waste heat is extracted by cooling, but as the cooling medium may rise in temperature, the conversion efficiency may be limited [8]. Other applications for TE power generation are numerous, see, e.g., [9, 10]. The amount of additional TE power is determined by the so-called figure of merit ( $Z$ ) of the TE material and the temperature difference over the TE module. The figure of merit  $Z$  depends on material parameters, i.e., Seebeck coefficient  $S$  [V/K], thermal conductivity  $\kappa$  [W/cmK], and electrical resistivity  $\rho$  [ $\Omega\text{cm}$ ], and is defined as  $Z = S^2\kappa/\rho$  [ $\text{K}^{-1}$ ] [11]. Usually the product of the figure of merit and temperature is quoted for a particular material, and present day materials have values of  $ZT \sim 1$  [7]. To increase the figure of merit, a good TE material, both  $n$ - and  $p$ -type doped material, is required to have a large Seebeck coefficient, high thermal conductivity, and low electrical resistivity [12].

Various thermoelectric materials exist, and based on the

figure of merit value at a certain temperature are used in a number of applications with a specific temperature range. For example, the material lead telluride (PbTe) is used at temperatures between 600 and 800 K. At higher temperatures (800-1300 K) silicon germanium (SiGe) alloys are used, while at lower temperatures (200-400 K) bismuth telluride (BiTe) is preferred [7, 11, 13]. For all these materials and temperature ranges it holds that  $ZT$  is around 1. New developments, especially in the direction of low-dimensional thermoelectric materials [14], have led to higher values of  $ZT \sim 1.5-4$  for various types of (quantum dot) superlattices, as reviewed in [15], where a range of  $ZT \sim 1.5-2.5$  is reported for a temperature of 300 K. Silicon nanowires of 20-300 nm in diameter have recently been reported to have  $ZT \sim 0.6$  at 300 K [16] and  $ZT \sim 1$  at 200 K [17]. With a further reduction of diameter, it is expected that  $ZT$  can be larger than 1 at 300 K [16], which would make silicon as a cheap and abundant material an excellent candidate for future TE devices [18]. Note that for a BiTe nanowire a  $ZT$  of 14 was estimated already [19].

## 2 SYSTEM LAYOUT

A schematic overview of the proposed system layout is depicted in Fig. 1. To the back side of the PV module a series of thermoelectric converters is attached. The heat generated in the PV module is converted to electricity by a series of  $n$ - and  $p$ -type thermoelectric converters, which are mounted on an appropriate heat sink. At high irradiation and high ambient temperatures, and depending on the type of integration, the module temperature can reach values of 80 °C or larger. The temperature difference thus maximally is about 50-60 °C, therefore low-temperature TE materials are to be deployed, i.e. with  $ZT \geq 1$  at 300 K.



**Figure 1:** Schematic drawing of the studied configuration. A plastic layer containing QDs is applied on top of a solar cell. Absorption of incident light and emission lead to a modified spectrum incident on the solar cell.

### 3 MODEL

#### 3.1 Assumptions

Incident solar irradiation is converted by the PV module with efficiency  $\eta_{PV}$ . The remaining heat flux is assumed to be available to the TE module, and is converted with efficiency  $\eta_{TE}$ . Thus, the heat flux through the module sides and front cover but especially radiation loss through the front cover are not taken into account. The total amount of generated power then is

$$P_{PVTE} = P_{PV} + P_{TE} = \eta_{PV}G + (1 - \eta_{PV})G\eta_{TE} \quad (1)$$

and the efficiency of the hybrid PVTE system is written as

$$\eta_{PVTE} = \eta_{PV} + (1 - \eta_{PV})\eta_{TE} \quad (2)$$

In the following we will show that all efficiencies depend on irradiance  $G$ .

#### 3.2 PV simulation model

The PV module performance is modelled assuming constant maximum power point (MPP) operation. A simple parametric model for the efficiency  $\eta_{MPP}(G, T_M)$  as a function of irradiance  $G$  and module temperature  $T_M$  is used, see [1]. The effect of temperature on efficiency is modelled using a linear temperature dependence, with temperature coefficient  $\alpha$ :

$$\eta_{MPP}(G, T_M) = \eta_{MPP}(G, 25) \cdot (1 + \alpha(T_M - 25)) \quad (3)$$

and the efficiency  $\eta_{MPP}(G, T_M)$  at  $T_M = 25^\circ\text{C}$  (standard test condition, STC) is given as

$$\eta_{MPP}(G, 25) = a_1 + a_2G + a_3 \ln(G) \quad (4)$$

with  $a_1$ ,  $a_2$ , and  $a_3$  module specific parameters.

The four parameters can in principle be determined from data sheets provided by manufacturers of PV modules, or from fitting measured efficiency data as a function of irradiance. In this paper we use constants derived from measurements of a multi-crystalline silicon module:  $a_1 = 0.1894$ ,  $a_2 = -0.04163 \text{ m}^2/\text{W}$ ,  $a_3 = 0.02158$ ,  $\alpha = -0.4 \text{ \%}/\text{K}$  [20].

In order to apply this model, the module temperature needs to be determined from the ambient temperature and irradiance, using the simplifying assumption that module temperature  $T_M$  to ambient temperature  $T_A$  difference is proportional to irradiance  $G$  [1]:

$$T_M = T_A + cG \quad (5)$$

The coefficient  $c$  is found to depend on the installation conditions, as shown in Table 1 (data from Sauer [21]).

#### 3.3 TE simulation model

The efficiency of a TE module can be expressed as [11]:

$$\eta_{TE} = \eta_{Carnot} \frac{\sqrt{1 + T_{avg}Z} - 1}{\sqrt{1 + T_{avg}Z} + \frac{T_A}{T_M}} \quad (6)$$

with the Carnot efficiency defined as:

$$\eta_{Carnot} = 1 - \frac{T_A}{T_M} \quad (7)$$

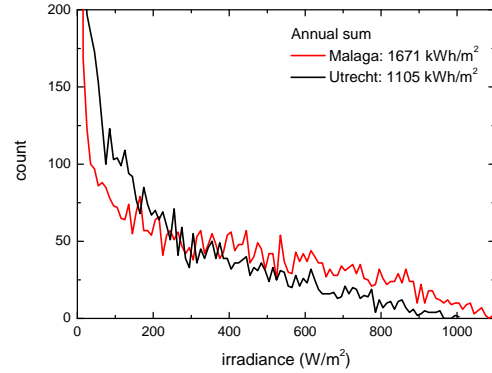
and the average temperature  $T_{avg}$  of the TE module as

$$T_{avg} = \frac{1}{2}(T_M + T_A) = T_A + \frac{1}{2}cG \quad (8)$$

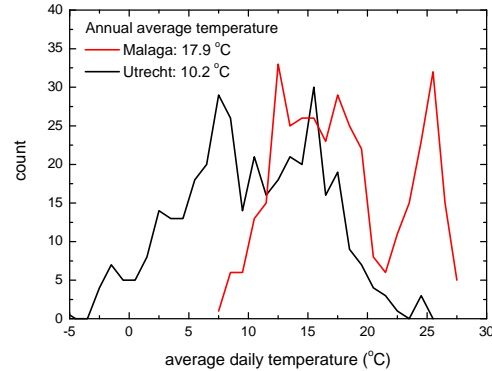
where we have used Eq. (5). The efficiency  $\eta_{TE}$  depends on  $Z$  and on operational temperatures  $T_M$  and  $T_A$ , and thus also depends on irradiance  $G$ .

#### 3.4 Annual performance

The annual performance of a PV-TE hybrid is now determined using the above equations and data sets of hourly averaged irradiances and daily averaged ambient temperatures. The annual amount of generated energy (in kWh) is calculated by summing the generated power (W) at each single hour. In order to show differences in climate, we have used datasets for the city of Utrecht, the Netherlands ( $52^\circ05' \text{ N}$ ,  $5^\circ08' \text{ E}$ ), and the city of Malaga, Spain ( $36^\circ43' \text{ N}$ ,  $4^\circ25' \text{ E}$ ). The latter city has higher temperatures and irradiances. Data are taken from the NASA SSE dataset [22], using the simulation tool HOMER [23]. Note that only average daily temperatures were available. The annual distributions of irradiance and temperature are shown in Fig. 2.



(a)



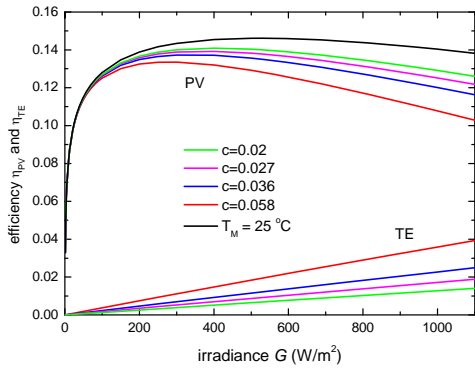
(b)

**Figure 2:** Frequency distribution of irradiance (a) and temperature (b) for the two locations Malaga and Utrecht.

4 RESULTS

4.1 PV efficiency

The efficiency of the PV module as a function of irradiance is shown in Fig. 3, for various temperatures. The STC condition  $T_M = 25^\circ\text{C}$  is shown in the top curve, and the efficiency of the PV module at  $1000 \text{ W/m}^2$  is 14.03 %. For different ways of module integration, as indicated in Table I, different module temperatures result for the same irradiance values, which in turn results in lower efficiency values. Consequently, the higher the coefficient  $c$ , the lower the efficiency. For example, at  $1000 \text{ W/m}^2$  the efficiency of the PV module is 10.78 %, as the module temperature is  $83^\circ\text{C}$  for  $c=0.058$  (roof integrated PV module). Note that for these calculations a constant ambient temperature of  $25^\circ\text{C}$  is used.



**Figure 3:** Efficiency of the PV module (marked ‘PV’) as a function of irradiance for various conditions that result in different module temperatures: STC condition ( $T_M = 25^\circ\text{C}$ ), and four different ways of module integration as represented by coefficient  $c$  (Eq. (5) and Table I). Efficiency of the TE module (marked ‘TE’) for the same four different ways of module integration.

**Table I:** Parameter  $c$  as a function of the integration type of PV system installation [1]

PV system installation	$c$
roof-integrated	0.058
on roof, small roof-module distance (<10 cm)	0.036
on roof, large roof-module distance (>10 cm)	0.027
free-standing cloudy	0.02

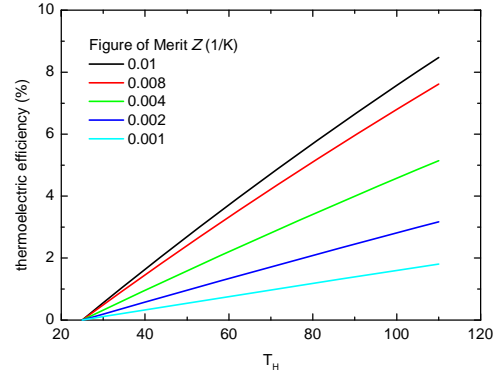
4.2 TE efficiency

The efficiency of the TE module as a function of irradiance is also shown in Fig. 3, now for a specific figure of merit of  $Z = 0.004 \text{ K}^{-1}$ , which is state-of-the-art for BiTe alloys [24]. Depending on the type of integration, the module temperature varies, which is reflected in the four TE efficiency curves. Consequently, the higher the coefficient  $c$ , the higher the TE module efficiency becomes. For example, at  $1000 \text{ W/m}^2$  the efficiency of the TE module is 3.20 % for  $c=0.058$ .

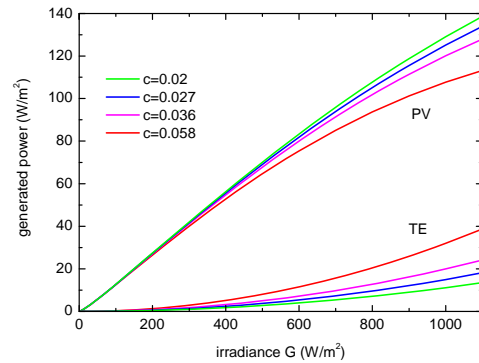
The effect of various values for the figure of merit is shown in Fig. 4. The larger  $Z$ , the higher the efficiency, which can amount to 6% or larger for module temperatures above  $80^\circ\text{C}$ .

4.3 PV-TE generated power

The efficiency of the PV-TE hybrid can now be calculated using Eq. (2), i.e., combining the above results. The generated PV and TE power is depicted in Fig. 5 as a function of irradiance, for the four integration types.



**Figure 4:** Variation of the thermoelectric efficiency as a function of temperature  $T_H$  for 5 values of the figure of merit  $Z$ . Note that  $T_L = 25^\circ\text{C}$ .



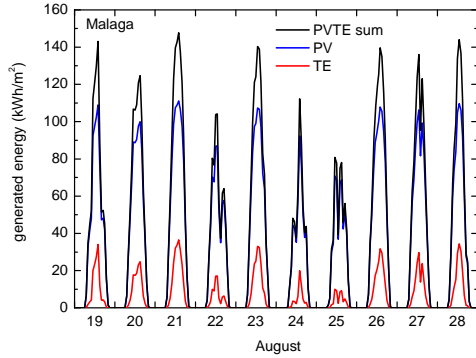
**Figure 5:** Generated PV and TE power as a function of irradiance for four different ways of module integration.

Coincidentally, as we will show in section 5, the sum of PV and TE generated power curves closely resembles the generated power as if the PV module would be at constant temperature of  $25^\circ\text{C}$  (STC).

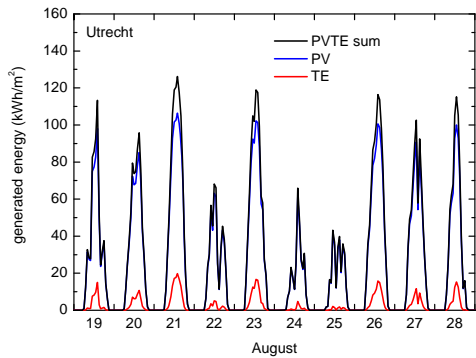
4.4 Annual performance

As the irradiance and temperature distributions for Malaga shows higher values than the ones for Utrecht, deploying PV-TE hybrids is expected to lead to a larger efficiency increase in Malaga compared to Utrecht. Figure 6 shows the generated energy for 10 days in August (19-28) for the cities of Malaga and Utrecht. The variation in irradiance is clearly reflected in PV generated energy and TE generated energy. The maximum relative contribution of TE generated energy to the total in this period of 10 days is 24.7% on August 21, the lowest maximum is 11.9% on August 25. For Utrecht maximum relative contributions are found of 15.7% and 4.5% on August 21 and 25, respectively.

The PV module deployed in Malaga would yield an annual amount of energy of 211.9 kWh. The TE converter would add an additional 31.1 kWh thus totalling 243.0 kWh. The generated energy by the TE converter thus enhances the PV annual energy yield by 14.7%. In case of Utrecht, the PV module would yield 147.4 kWh. Adding 16.1 kWh from the TE converter thus totals 163.6 kWh for the PV-TE hybrid, and the TE converter increases the PV annual energy yield by 11.0%. The higher PV yield for Malaga compared to Utrecht is related to higher irradiances at first order, as for higher



(a)



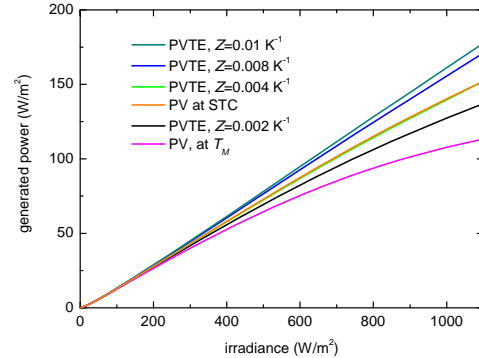
(b)

**Figure 6:** Generated PV, TE, and total energy for a 10-day period in August for the cities of (a) Malaga, Spain, and (b) Utrecht, the Netherlands.

irradiances also ambient temperatures are high. The energy generated by the TE converter in Malaga is about twice the amount of that in Utrecht. Note that the average ambient temperature in Malaga is substantially larger than in Utrecht.

## 5 FUTURE DEVELOPMENTS

Present maximum figure of merit values are  $ZT = 2.5$  as reported for a temperature of 300 K [15], or  $Z = 0.00833 \text{ K}^{-1}$ , while  $Z = 0.01 \text{ K}^{-1}$  is seen as realistically attainable. However, much more research is needed to explore and explain the observed increases in figure of merit values, especially for new nanomaterial classes such as superlattices and nanowires. If we assume that a future TE material would have a figure of merit of  $Z = 0.01 \text{ K}^{-1}$  at 300 K, thermoelectric efficiencies may be doubled, as can also be seen in Fig. 4. If this material is deployed in a PV-TE hybrid, the irradiance-dependent efficiency as shown in Fig. 7 would be attainable, i.e., for roof-integrated modules ( $c=0.058$ ). With respect to a PV module efficiency at  $1000 \text{ W/m}^2$  of 10.78% (at module temperatures of  $83 \text{ }^\circ\text{C}$ ), the PV-TE hybrid with  $Z = 0.01 \text{ K}^{-1}$  shows an efficiency of 16.11%, or 50% larger than for a PV module alone. For the present near-maximum value of  $Z = 0.008 \text{ K}^{-1}$  an PV-TE efficiency of 15.56% is reached, while for  $Z = 0.002 \text{ K}^{-1}$  (reported for silicon nanowires [16]) an efficiency of 12.73% can be reached. For comparison, also the efficiency of a PV module is shown, for a constant module temperature of  $25 \text{ }^\circ\text{C}$  (STC). The PV-TE efficiency curve for  $Z = 0.004 \text{ K}^{-1}$  (present today's maximum) per chance coincides with the STC one.



**Figure 7:** Generated PVTE power as a function of irradiance for four values of the figure of merit  $Z$ , and generated PV power as a function of irradiance at STC and actual module temperature  $T_M$  determined by irradiance level.

The annual performance of the future PV-TE hybrid deployed in Malaga with  $Z = 0.01 \text{ K}^{-1}$  would be enhanced to 264.6 kWh, which is 8.9% larger than for the PV-TE hybrid with  $Z = 0.004 \text{ K}^{-1}$ . In case of Utrecht, the annual performance would be enhanced to 174.8 kWh, or a 6.7% larger than the  $Z = 0.004 \text{ K}^{-1}$  PV-TE hybrid. Compared to a PV module alone a performance enhancement of 24.9% and 18.6% is calculated, for Malaga and Utrecht, respectively.

## 6 DISCUSSION

The model described above allows for a calculation of the maximum enhancement of efficiency as a result of adding a TE converter. Several losses are not considered, such as reflection losses, which typically amount to 5-10% for PV modules. Heat flux and radiation losses from the side and front cover are also not taken into account. Further, although it is yet unclear if such arrangement may be realized in practice, it is assumed that the back side temperature of the TE converter always equals the ambient temperature. This may not be the case: a higher back side temperature thus lowers the TE efficiency. As an example, if the temperature difference between front and back side would be lowered to 75% of its value (by enhancing the back side temperature), the TE efficiency at  $1000 \text{ W/m}^2$  and  $T_M = 83 \text{ }^\circ\text{C}$  would be lowered from 3.59% to 2.68% (or nearly 25% lower). While the TE efficiency is substantially lowered, the annual energy yield is affected to a much lesser extent, which is of course due to the relatively low (around 10%) contribution of TE generated energy to the total amount. The annual energy yield in case of Malaga is found to be lowered from 243.0 kWh to 235.2 kWh, or only 3.3% lower, while the contribution from the TE converter is reduced from 31.1 kWh to 23.3 kWh (25% reduction). For Utrecht, the annual energy yield is lowered from 163.6 kWh to 159.4 (2.6% lower). From the above we therefore estimate that the PV-TE efficiencies calculated by the simple and idealized model may in practice be substantially lower, but as the contribution of the TE converter to the total is relatively small, the generated power may be lower by about 10% only.

## 7 CONCLUSION

We have developed a simple model to determine the efficiency of a combined photovoltaic and thermoelectric converter, or PV-TE hybrid. The model is applied to certain types of integrated PV-TE hybrids. Results show that adding a TE converter to the backside of a PV module can lead to an

efficiency increase of 8-23 %, depending on the type of module integration, and assuming TE material with a typical present day figure of merit value of  $Z = 0.004 \text{ K}^{-1}$ . The annual performance of a PV-TE hybrid is modelled using two annual irradiance and temperature profiles, i.e., for Malaga, Spain, and Utrecht, the Netherlands, and is found to increase by 14.7% and 11%, for Malaga and Utrecht, respectively.

Future developments in TE material research may allow for figure of merit values of  $Z$  that approach  $Z = 0.01 \text{ K}^{-1}$ . These high- $Z$  materials would allow for an efficiency increase of up to 50%. The effect on annual performance is lower, but varies between 24.9% and 18.6% for the two cases studied.

The efficiency and performance enhancements are calculated using a simple, idealized model. Practical TE efficiencies are estimated to be 25% lower, while performance is less affected and are estimated to be about 10% lower.

## 8 ACKNOWLEDGEMENTS

We gratefully acknowledge Dejan Gajic, Jeroen Rodenburg, and Matthijs Vakar (Junior College Utrecht, the Netherlands) for enthusiastic exploratory work, and Nils Reich for critical reading of the manuscript. SenterNovem is acknowledged for financial support as part of the Dutch Nieuw Energie Onderzoek (New Energy Research) programme.

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