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# CO<sub>2</sub> activation and dissociation on the low miller index surfaces of pure and Ni-coated iron metal: a DFT study†

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We have used spin polarized density functional theory calculations to perform extensive mechanistic studies of CO<sub>2</sub> dissociation into CO and O on the clean Fe(100), (110) and (111) surfaces and on the same surfaces coated by a monolayer of nickel. CO2 chemisorbs on all three bare facets and binds more strongly to the stepped (111) surface than on the open flat (100) and close-packed (110) surfaces, with adsorption energies of  $-88.7 \text{ kJ mol}^{-1}$ ,  $-70.8 \text{ kJ mol}^{-1}$  and  $-116.8 \text{ kJ mol}^{-1}$  on the (100), (110) and (111) facets, respectively. Compared to the bare Fe surfaces, we found weaker binding of the CO2 molecules on the Ni-deposited surfaces, where the adsorption energies are calculated at +47.2 kJ mol<sup>-1</sup>, -29.5 kJ mol<sup>-1</sup> and -65.0 kJ mol<sup>-1</sup> on the Ni-deposited (100), (110) and (111) facets respectively. We have also investigated the thermodynamics and activation energies for CO2 dissociation into CO and O on the bare and Ni-deposited surfaces. Generally, we found that the dissociative adsorption states are thermodynamically preferred over molecular adsorption, with the dissociation most favoured thermodynamically on the close-packed (110) facet. The trends in activation energy barriers were observed to follow that of the trends in surface work functions; consequently, the increased surface work functions observed on the Ni-deposited surfaces resulted in increased dissociation barriers and vice versa. These results suggest that measures to lower the surface work function will kinetically promote the dissociation of CO<sub>2</sub> into CO and O, although the instability of the activated CO<sub>2</sub> on the Ni-covered surfaces will probably result in CO<sub>2</sub> desorption from the nickel-doped iron surfaces, as is also seen on the Fe(110) surface.

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#### 1. Introduction

CO<sub>2</sub> conversion is desirable as it can provide a source of renewable fuels and other carbon-based products that are currently obtained from fossil fuels. However, CO<sub>2</sub> reduction to useful hydrocarbons is still industrially challenging and its use in technological processes is therefore limited. The challenges and prospects of CO<sub>2</sub> conversion have been reviewed extensively.<sup>1-6</sup> Even though CO<sub>2</sub> conversion under sustainable conditions is still a challenge,<sup>6</sup> it is known to be converted under ambient conditions in biological systems, *e.g.* carbon-monoxide dehydrogenases enzymes containing Fe and Ni active sites.<sup>7,8</sup>

Single crystal heterogeneous transition metal catalysts have received much attention for potential  ${\rm CO_2}$  conversion. From the

early 1980s onwards, several experimental studies have been undertaken to understand the behavior of CO2 on transition metal surfaces; these studies have been compiled in two reviews. 9,10 In general, except for a few late transition metals such as Fe, Ni, and Cu, CO2 was found not to be activated on clean transition metal surfaces, except when promoted by alkali metals. Electron transfer from the surface to the LUMO of CO2 to form an activated  $CO_2^{-\delta}$  species is the key step to  $CO_2$ reduction on catalytic surfaces, which was found to be affected by the temperature, the presence of promoters, the surface morphology and surface defects. Despite these many experimental studies, the energetics of CO2 reduction over iron surfaces are still not well understood. Although the extent of CO2 activation has been investigated computationally on various low Miller index surfaces of Cu, 11,12 Ni 3 and Co 4 as well as its dissociation and hydrogenation, 15-21 this is not the case for the Fe facets, where there is no detailed computational study to complement the extensive experimental work. 22-27

Under the same experimental conditions, at 300 K, CO<sub>2</sub> activation and dissociation and sequential CO dissociation were reported on Fe(111), but no interaction was observed on

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the Fe(110) facet. 22-24 Bent CO2 as a precursor to dissociation has also been reported between 160-180 K<sup>25</sup> and at 130 K<sup>26</sup> on Fe(111). Hess et al.,26 using high resolution electron loss spectroscopy (HREELS) studies, observed a weakly bound unstable linear CO2 mode and two stable bent CO2 modes on the (111) facet. CO2 dissociation starts at 130 K and CO dissociation at about room temperature. Nassir and Dwyer<sup>27</sup> first reported on the activation of CO<sub>2</sub> on the (100) facet at a slightly lower energy than on the (111) surface and concluded from their results that both the (111) and (100) surfaces behaved in a similar reactive manner compared to the unreactive (110) facet. Using temperature programmed desorption (TPD) they observed stable  $C_s$  and  $C_{2v}$  bent  $CO_2$  adsorption modes compared to linear CO2 on the surface, two sequential C-O dissociations and a stable CO intermediate, whereas low energy electron diffraction (LEED) analysis indicated the hollow site as the preferred CO<sub>2</sub> adsorption site. Activation was observed on Fe(100) at 110 K, leading to dissociation at 300 K, CO dissociation at 723 K and carbon desorption at 973 K. Recombination of atomic carbon and oxygen of dissociated CO species at elevated temperatures was also reported at 927 K. These experimental studies and other theoretical studies on Ni, Cu and Co show that apart from the type of metal, CO<sub>2</sub> activation is also affected by the surface morphology.

Earlier theoretical works have reported spontaneous CO2 activation on the low Miller indices of iron and the energetics to dissociate CO2 species on the (100) and (111) surfaces but not on the (110) surface. 28-33 A recent DFT study has shown that nickel deposition on iron surfaces increased the work function of the (100) and (111) facets but reduced the work function of the most stable and close-packed (110) surface.<sup>34</sup> This result suggests that Ni monolayer deposition may affect the thermodynamics and/or kinetics of CO2 adsorption and dissociation. To understand fully the role of the surface structure and composition in the energetics of CO2 dissociation on the Ni-deposited Fe surfaces, here we have calculated the adsorption energies, activation energy barriers and geometric structures of reactants, products, and transition states of the process of CO2 dissociation on bare Fe surfaces and compared them with those on the same surfaces coated with a monolayer of nickel.

## 2. Computational details

All calculations were carried out using the generalized gradient approximation (GGA) within the spin-polarized density functional theory (DFT) method with a plane-wave basis set and ultra-soft pseudopotentials, as described within the Quantum ESPRESSO Package, which performs fully self-consistent DFT calculations to solve the Kohn-Sham equations. The Perdew, Burke, Ernzerhof (PBE) GGA exchange-correlation functional was employed. The Fermi-surface effects were treated by the smearing technique of Fermi-Dirac, using a smearing parameter of 0.003 Ry in all calculations. The energy convergence threshold defining self-consistency of the electron density was set to  $10^{-6}$  eV and that defining the mixing factor for self-consistency to 0.2. The graphics of the atomic structures were prepared using the XCrysDen software.

The various low Miller index surfaces were created from the optimized bulk using the METADISE39 code. Surfaces were described using a slab model, where periodic boundary conditions are applied to the central super-cell so that it is reproduced periodically throughout space. Super-cells large enough to prevent lateral interactions between adsorbates were employed, such that adsorbates (molecular and dissociated species) are more than 5 Å away from their periodic images. Super-cells of the  $p(3 \times 3)$  (100) surface, the  $p(2 \times 2)$  (110) surface and the  $p(3 \times 2)$  (111) surface were employed for both adsorption and dissociation studies, representing CO<sub>2</sub> surface coverages of 1/9, 1/8 and 1/6 respectively. The surface coverage is defined as the number of adsorbed CO<sub>2</sub> molecules relative to the number of metal atoms in the topmost layer of each surface. The Brillouin zone was sampled using a Monkhorst-Pack<sup>40</sup> k-point mesh of  $(9 \times 9 \times 9)$  for the bulk material and  $(3 \times 3 \times 1)$ ,  $(5 \times 5 \times 1)$  and  $(3 \times 5 \times 1)$  mesh k-points for the (100), (110) and (111) surface calculations, respectively. A vacuum region of 12 Å perpendicular to each surface was tested to be sufficient to avoid interactions between periodic slabs. An energy cut-off of 40 Ry (544 eV) and a charge density cut-off of 320 Ry (4354 eV) for the expansion of the plane-wave basis set were found to be adequate for converging the total energy of the bulk iron to 1 meV.

Following convergence tests, the (110), (100) and (111) slabs were built to thicknesses of 4, 5 and 6 layers, respectively, whose settings are sufficient to converge the surface energies of the facets.34 The top layer of iron is replaced with nickel in the nickel-deposited surfaces resulting in a total surface coverage. In all calculations, the top 3 layers and adsorbates were allowed to relax explicitly and the bottom layers were fixed at their bulk equilibrium position to mimic the bulk material. The amount of charge gained by the CO<sub>2</sub> molecule from each surface was calculated using the Löwdin scheme. 41 The transition state structures were searched using the climbing image nudged elastic band (CI-NEB) method<sup>42</sup> and transition state structures were located as the structure with the highest energy along the reaction coordinate, characterised by one and only one imaginary frequency. The reaction energy  $(\Delta E)$  is calculated as the total energy difference between the final state and the reactants. Energy barriers are also calculated as the total energy difference between the transition state and the reactants. London dispersion interactions were not accounted for in the present study, as recent periodic DFT calculations of the water gas shift reaction on Cu(321) show that including dispersion terms does not change the qualitative picture of the overall reaction, maintaining both the rate determining step and the predominant route. However, we do expect that the dispersion contributions may make a difference to the stability of the CO2 molecules, intermediates or products on the different Fe surfaces. 43

#### 3. Results and discussion

# 3.1 Adsorption sites, modes and strengths of CO<sub>2</sub> on bare and Ni-deposited Fe surfaces

We first explored the preferred  $CO_2$  binding sites (Fig. 1) and different modes of binding on the bare Fe(100), (110) and (111)

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facets and later introduced nickel to the surfaces at the most preferred adsorption modes. The initial adsorption sites investigated included the top, bridge and hollow sites as well as the sub-layer top site (shallow top), the sub-sub-layer top site (deep top) and the sub-layer bridge site (shallow bridge) on the (111) surface, as indicated in Fig. 1.

For each adsorption structure, energy minimizations were carried out until convergence within 1 meV per cell was achieved. The lowest-energy CO<sub>2</sub> adsorption structures on the bare and Ni-deposited surfaces are presented in Fig. 2 and 3, respectively (the remaining binding modes and calculated binding energies are given in the ESI,† Fig. S1-S3 and Table S1).

For the Fe(100) surface calculations, a  $p(3 \times 3)$  super-cell was employed for the CO2 adsorption and dissociation reactions, similar to earlier calculations. <sup>28,29</sup> The super-cell is made up of nine surface atoms and five atomic layers. The lowest-energy CO<sub>2</sub> adsorption configuration at the Fe(100) surface was calculated at the hollow site in the  $C_{2v}$  mode, where the  $CO_2$  molecule binds through the carbon and two oxygen atoms (Fig. 2a), releasing an energy of 88.7 kJ mol<sup>-1</sup> upon adsorption (Table 1). The adsorption energies of the other stable adsorption configurations are calculated at -62.7 kJ mol<sup>-1</sup> for CO<sub>2</sub> adsorption at the bridge site, -53.7 kJ mol<sup>-1</sup> for the  $C_s$  mode at the hollow site, -15.4 kJ mol<sup>-1</sup> for CO<sub>2</sub> adsorption at the top Fe site, and  $-2.0 \text{ kJ mol}^{-1}$  for linearly physisorbed CO<sub>2</sub> (ESI,† Fig. S1b-d). The calculated adsorption energies and structural parameters of the lowest-energy structure are similar to those reported in earlier investigations. 28,29 Glezakou et al. 28 also obtained the hollow- $C_{2v}$  structure as the preferred  $CO_2$ activated mode on the Fe(100) surface with an adsorption energy of -69.9 kJ mol<sup>-1</sup>, when they studied CO<sub>2</sub> corrosion pathways using spin-polarized DFT and norm-conserving pseudopotentials. Later, Liu et al., 29 employing spin-polarized DFT and projected augmented wave pseudopotentials, also reported the hollow- $C_{2v}$  structure as the preferred structure with an adsorption energy of  $-61.9 \text{ kJ mol}^{-1}$ . Recently, Nie et al. have similarly obtained the hollow- $C_{2v}$  structure, with a binding energy of -91.66 kJ mol<sup>-1</sup> with the DFT-GGA calculation using projected augmented wave pseudopotentials. These results are consistent with our binding energy of  $-88.7 \text{ kJ mol}^{-1}$  at the Fe(100) surface, where the small difference could be attributed to the differences in pseudopotentials employed. On the Ni-deposited Fe(100) surface (Fig. 3a), the binding site and mode of CO2 adsorption remain the same as on the bare Fe(100) surface, but the adsorption becomes unstable with an endothermic energy of +47.2 kJ mol<sup>-1</sup>. This drastic change in binding strength from  $-88.7 \text{ kJ mol}^{-1}$  to  $+47.2 \text{ kJ mol}^{-1}$  could

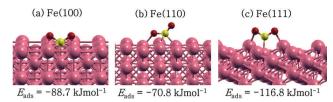


Fig. 2 Stable CO<sub>2</sub> adsorption modes on the Fe (100), (110), and (111) surfaces. Colour code: Fe = pink, C = yellow and O = red.

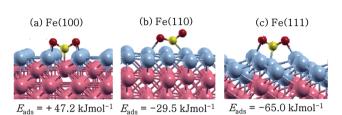


Fig. 3 Preferred CO<sub>2</sub> adsorption site on the nickel monolayer covered Fe (100), (110) and (111) surfaces. Colour code: Fe = pink, Ni = blue, C = yellow, and O = red.

at least in part be attributed to the higher electronegativity of nickel, resulting in less electron transfer into the CO2 moiety, as nickel is observed to bind adsorbates less strongly compared to iron. 13,30 For the pure fcc nickel metal, the CO<sub>2</sub> binding energy was calculated to be -7.7 kJ mol<sup>-1</sup> at the Ni(100) surface. 13

For the CO<sub>2</sub>-Fe(110) complexes, a  $p(2 \times 2)$  super-cell made up of eight top atoms and four atomic layers was employed for the CO<sub>2</sub> adsorption and dissociation reactions. As on the Fe(100) surface, several possible sites and modes of adsorption of CO<sub>2</sub> including bridge- $C_{2v}$ , hollow- $C_{2v}$  and hollow- $C_{s}$  configurations were explored on the Fe(110) surface in order to predict the lowest-energy structure. The hollow- $C_s$  structure (Fig. 2b) was calculated to be the preferred CO<sub>2</sub> adsorption mode on the Fe(110) surface, with an adsorption energy of  $-70.8 \text{ kJ mol}^{-1}$ . This structure is energetically more stable than the hollow- $C_{2v}$  structure (ESI,† Fig. S2b) and the bridge-C<sub>2v</sub> structure (ESI,† Fig. S2c) which released adsorption energies of -46.8 kJ mol<sup>-1</sup> and 45.6 kJ mol<sup>-1</sup>, respectively. The lowest-energy hollow-C<sub>s</sub> structure (Fig. 2b) was previously reported by Wang et al. 30 on Fe(110), where they used a five atomic-layered slab to obtain an adsorption energy of  $-65.9 \text{ kJ mol}^{-1}$  (Table 2), consistent with -70.8 kJ mol<sup>-1</sup> obtained in this work. On the nickel-deposited Fe(110) surface, CO2 remains at the preferred hollow site (see Fig. 3b), but the binding energy is reduced from  $-70.8 \text{ kJ} \text{ mol}^{-1} \text{ to } -29.5 \text{ kJ} \text{ mol}^{-1} \text{ due to weak interactions}$ 

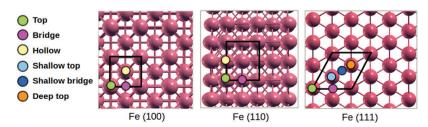


Fig. 1 Top, bridge and hollow starting adsorption sites on the Fe (100), (110) and (111) facets.

Table 1 Adsorption energy and structural parameters of CO<sub>2</sub> adsorbed on Fe (100), (110) and (111) surfaces

Surface	Structure	$E_{\rm ads}/{\rm kJ~mol^{-1}}$	C-O(1), C-O(2)/Å	$O-C-O/^{\circ}$	Fe-C/Å	Fe-O(1), Fe-O(2)/Å	$\sum q/e$
Fe(100)	Bare Fe (hollow- $C_{2v}$ )	-88.7	1.35	119.29	2.15	2.08	-0.08
	Ni-covered (hollow- $C_{2v}$ )	47.2	1.32	121.4	2.10	2.12	-0.07
	Glezakou et al. <sup>28</sup>	-69.9	1.35	117.8	2.11	2.08, 2.05	_
Fe(110)	Bare Fe (hollow- $C_s$ )	-70.8	1.36, 1.23	126.98	1.98	2.04, 2.53	-0.06
	Ni-covered (hollow- $C_s$ )	-29.5	1.29, 1.24	132.2	1.98	2.08, 2.23	-0.05
	Wang et al. 30	-65.9	1.35, 1.22	128.00	1.96	2.01	_
Fe(111)	Bare Fe (bridge- $C_{2v}$ )	-116.8	1.30	122.3	1.98	1.96	-0.06
		-65.0	1.27	127.8	1.90	1.98, 1.97	-0.05
	Ni-covered (bridge- $C_{2v}$ ) Li and Ho <sup>31</sup>	-107.1	1.29	122.3	1.96	1.96	_

between  $CO_2$  and the interacting Ni atoms, which results in less electron transfer to the adsorbate. Compared to the bare Fe(110) surface, where the  $CO_2$  molecule was adsorbed in 4-fold coordination, at the Ni-covered (110) surface, the  $CO_2$  molecule is 2-fold coordinated to the Ni atoms, which explains the weaker adsorption energy calculated for the Ni-covered surface.

On the Fe(111) surface, a  $p(3 \times 2)$  super-cell was employed for both CO<sub>2</sub> adsorption and dissociation. We have explored several initial guess CO2 structures adsorbed at bridge, shallow top, shallow bridge and deep top adsorption sites in order to determine the lowest-energy structure. Shown in Fig. 2c is the lowest-energy CO<sub>2</sub> adsorption structure identified at the Fe(111) surface, the other stable structures calculated are shown in the ESI, † Fig. S3. In the lowest-energy bridge- $C_{2v}$  structure (Fig. 2c), the carbon atom binds at the shallow top site and the oxygen atoms bind at the top bridge site, releasing an adsorption energy of -116.8 kJ mol<sup>-1</sup> (see Table 1). Compared to the bridge-C2v structure, positive adsorption energy energies of 27.1 kJ mol<sup>-1</sup> and 1.7 kJ mol<sup>-1</sup> were calculated for the top- $C_{2v}$ structure (ESI,† Fig. S3a) and the slanted linear CO2 structure (ESI,† Fig. S3b), respectively. The vertical linear structure at the top Fe site (ESI,† Fig. S3c) released only a small adsorption energy of -1.1 kJ mol<sup>-1</sup>. These adsorption energies suggest that the  $C_{2v}$  bent and linear vertical modes are stable  $CO_2$ structures on the surface, as reported in earlier experimental work. The bridge- $C_{2v}$  structure was also previously predicted to be the bent adsorption mode of CO<sub>2</sub> at the Fe(111) surface; Ho and co-workers used spin polarised density functional theory to study CO2 hydrogenation to formate and then its dissociation on Fe(111). 31,32 They reported an adsorption energy of -107.1 kJ mol<sup>-1</sup> for CO<sub>2</sub> adsorption, which compares well with our result of  $-116.8 \text{ kJ} \text{ mol}^{-1}$ . On the Ni-deposited Fe(111) surface, CO2 remains at the bridge shallow site (see Fig. 3c), with the binding strength reduced from  $-116.8 \text{ kJ} \text{ mol}^{-1} \text{ to } -65.0 \text{ kJ} \text{ mol}^{-1}$ , in agreement with the observed reduced charge transfer from the surface to the CO2 moiety.

Generally,  $CO_2$  is more stable in the  $C_8$  mode on the close-packed (110) surface, whereas, as also suggested by experiment, the more open (100) and (111) surfaces behave almost alike, with CO2 adsorbing in the  $C_{2v}$  mode. The  $C_{s}$  adsorption mode reduces the coordination number (to two instead of three) as well as surface interactions and charge transfer between CO2 and the (110) surface, due to the high surface atom density and crowding at the hollow site on the close-packed (110) face. The trend in the adsorption energies shows that CO2 adsorption is most favoured on the open and least stable surfaces in the order (111) > (100) > (110), i.e.  $-116.8 \text{ kJ mol}^{-1} > -88.7 \text{ kJ mol}^{-1} > -70.8 \text{ kJ mol}^{-1}$ . This finding is consistent with the work of O'Shea et al. 14 on cobalt metal surfaces, who observed that CO2 interacts and binds most strongly to the most open low Miller index (110) surface of fcc Co metal. Ni deposition on the Fe surfaces is found to drastically reduce the adsorption strength of CO2, with the adsorption even becoming endothermic at the Ni-deposited (100) surface. The observed trend for CO2 adsorption on the Ni-deposited surfaces is  $(100) +47.2 \text{ kJ mol}^{-1} < (110) -29.5 \text{ kJ mol}^{-1} < (111)$ -65.0 kJ mol<sup>-1</sup>, with the binding least favoured on Fe(100), where the adsorbed CO<sub>2</sub> interacts primarily with the iron beneath the nickel layer at the hollow site. The molecular binding energies of CO2 on pure Ni (fcc) were reported to be  $-7.7 \text{ kJ mol}^{-1}$  at Ni(100),  $-37.6 \text{ kJ mol}^{-1}$  at Ni(110) and +29.9 kJ mol<sup>-1</sup> at Ni(111) surfaces, respectively, <sup>13</sup> where adsorption is endothermic on one of the surfaces of nickel. The endothermic binding energies of CO2 on Ni(111) and Nidoped Fe(100) seem to suggest that the CO2 moiety prefers to be free rather than binding to these surfaces. The electronic contributions to the observed differences in the reactivity of the bare Fe surfaces to the Ni-deposited surfaces towards CO<sub>2</sub> activation are discussed in the next section.

#### 3.2 Electronic properties and vibrational frequency analyses

The activation of  $CO_2$  was found to be characterized by charge transfer from the iron slab to the activated moiety, where the

Table 2 The symmetric  $(\nu_3)$ , asymmetric  $(\nu_{as})$  and bending  $(\nu_b)$  vibrational frequencies of CO<sub>2</sub> adsorbed on the low-miller index Fe surfaces

Vib. mode	Linear CO <sub>2</sub>	Fe(100)	Fe/Ni(100)	Fe(110)	Fe/Ni(110)	Fe(111)	Fe/Ni(111)
$ u_{\rm s}/{\rm cm}^{-1} $ $ u_{\rm as}/{\rm cm}^{-1} $ $ u_{\rm b}/{\rm cm}^{-1} $	$1300.0 (1351.2)^{10}$	846.1	923.5	810.3	940.6	1006.7	1078.4
	$2105.7 (2396.4)^{10}$	1112.1	1112.4	1505.8	1506.0	1246.4	1436.3
	$700.0 (672.2)^{10}$	750.3	748.2	733.5	730.5	750.3	739.0

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extent of  $CO_2$  activation, measured from the elongation of the C–O bond, is found to be proportional to the extent of charge transfer. Indeed a plot of the C–O bond distance against the charge gained by the  $CO_2$  adsorbed in the lowest-energy structures at the different surfaces (Fig. 4) shows a linear correlation between the amount of charge transfer and the extent of  $CO_2$  activation. The order of the C–O bond activation is Fe(100) > Fe/Ni(100) > Fe(111) > Fe(110) > Fe/Ni(110) > Fe/Ni(111), which is thus the same as the order for the amount of charge gained by the  $CO_2$  molecule. Compared to the bare Fe surfaces, we observed a smaller degree of charge transfer from the Ni-deposited surfaces to the  $CO_2$ , which is consistent with the weaker binding and shorter C–O bonds calculated at the Ni-surfaces than on the bare Fe surfaces.

Although we observed that on a particular facet stronger binding corresponds to more charge transfer, the same cannot be said across the various facets. Whereas we would expect the (111) surface to activate CO<sub>2</sub> to the highest degree, due to its largest CO<sub>2</sub> binding energy, we observed, however, that CO<sub>2</sub> activation is most pronounced on the (100) facet, the surface with the lowest work function. Similarly, Wang et al. 30 did not find a strong correlation between CO2 activation and binding strength across different transition metals (first row TM) and therefore attributed the strength of interaction to both the extent of activation and the d-band centre of the metal. We have also observed that for different surface structures of the same material or composition, the binding energy does not correlate with, or does not solely define, the extent of activation. Our study suggests that the extent of activation should be attributed to the extent of electron transfer.

Vibrational analyses of all the adsorption structures yielded no imaginary frequencies, showing that these structures are local minima. Table 2 summarises the three distinct high-frequency vibrational frequencies, which correspond to the symmetric ( $\nu_s$ ) and asymmetric ( $\nu_a$ s) stretching modes and the ( $\nu_b$ ) bending mode for CO<sub>2</sub> adsorbed in the most stable adsorption configuration on each surface. For the lowest-energy adsorption structure on

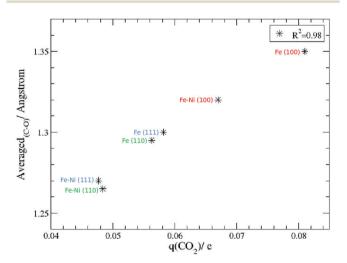


Fig. 4 Amount of charge gained by CO<sub>2</sub> and the extent of C-O activation.

the Fe(100) surface (Fig. 3a), the  $\nu_s$ ,  $\nu_{as}$ , and  $\nu_b$  modes can be assigned to 846.1 cm<sup>-1</sup>, 1112.1 cm<sup>-1</sup> and 750.3 cm<sup>-1</sup>, respectively. For the most stable adsorption geometry at the Fe(110) surface (Fig. 3b),  $\nu_s$ ,  $\nu_{as}$ , and  $\nu_b$  were assigned to 810.3 cm<sup>-1</sup>, 1505.8 cm<sup>-1</sup> and 733.5 cm<sup>-1</sup>, respectively. On the Fe(111) surface, the  $\nu_{\rm s}$ ,  $\nu_{\rm as}$ , and  $\nu_b$  modes for the lowest-energy adsorption structure (Fig. 3c) can be assigned to 1006.7 cm<sup>-1</sup>, 1246.4 cm<sup>-1</sup> and 750.3 cm<sup>-1</sup>, respectively. We note that on all three surfaces there is a significant redshift of the  $\nu_{\rm s}$  and  $\nu_{\rm as}$  modes, compared with the values (1300.0 and 2105.7 cm<sup>-1</sup>) of a free CO<sub>2</sub> molecule, whereas the bending modes are blue-shifted. The significant red-shifts in the stretching modes show that the CO<sub>2</sub> molecule is activated, which is consistent with the calculated elongated C-O bonds and bent <OCO angles. The C-O stretching vibrational frequencies of CO2 adsorbed on the deposited surfaces are less red- and blue-shifted compared to the bare Fe surfaces, which indicates lesser CO2 activation on these nickel-modified surfaces than on the bare Fe surfaces.

#### 3.3 CO<sub>2</sub> dissociation on bare and Ni-deposited Fe surfaces

We next sought to determine the preferred dissociation site of  $CO_2$  ( $CO_2 \rightarrow CO + O$ ). The reaction energy ( $\Delta E$ ) is calculated as the total energy difference between the final state (*i.e.* slab with both CO + O adsorbed on it) and the reactants (*i.e.* isolated slab + isolated  $CO_2$ ). To this end, the inter-nuclear C-O bond distance was increased beyond the C-O bonding distance and the dissociated oxygen atom was placed at various sites on the surface *i.e.* top, bridge and hollow sites (see Fig. 1). For each adsorption structure, energy minimizations were carried out until convergence within 1 meV per cell was achieved. Several initial sites were explored on each surface for the dissociated CO and O fragments in order to determine the most stable adsorption sites and structures.

On the bare Fe(100) surface, we found that the hollow site was the preferred adsorption site for both CO and O (see Fig. 5a and Table 3). The adsorption of both CO and O at the hollow sites released an adsorption energy of  $-179.9~\rm kJ~mol^{-1}$ , whereas for the co-adsorption of oxygen at the bridge site with CO at the hollow site, an adsorption energy of  $-143.7~\rm kJ~mol^{-1}$  was released. Our results are consistent with those of Glezakov *et al.*, who reported a co-adsorption energy of  $-126.0~\rm kJ~mol^{-1}$  for CO and O at the hollow sites using the projected augmented wave pseudopotentials.<sup>28</sup> On the nickel-deposited Fe(100) surface (Fig. 6a), the CO moves from the most table hollow site to the bridge site. The co-adsorption energy released reduced drastically from  $-179.9~\rm kJ~mol^{-1}$  to  $-0.7~\rm kJ~mol^{-1}$ , partly due to the change

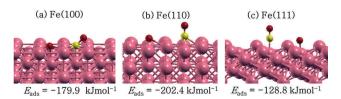


Fig. 5 Co-adsorption structures of CO + O s on the Fe (100), (110) and (111) surfaces.

Table 3 Co-adsorption energies and structural parameters of CO + O on Fe (100), (110) and (111) surfaces

Surface	Nature	O-Binding site	CO-Binding site	$E_{ m ads}/{ m kJ~mol^{-1}}$	C-O(1)/Å	C-O(2)/Å	Fe-CO/Å	Fe-O/Å
Fe(100)	Bare Fe Ni-doped	Hollow Hollow	Hollow Bridge	$-179.9 \\ -0.7$	1.31 1.18	3.02 3.91	2.10 1.90	2.10 2.01
Fe(110)	Bare Fe Ni-doped	Hollow Hollow	Hollow Hollow	-202.4 $-114.6$	1.21 1.19	3.97 4.65	1.97 1.94	1.85 1.87
Fe(111)	Bare Fe Ni-doped	Shallow top Shallow bridge	Shallow top Shallow bridge	$-128.8 \\ -52.4$	1.20 1.19	3.90 3.01	1.78 1.84	1.88 1.84

in the binding site and weaker binding, as observed even for bare nickel surfaces when compared to bare iron surfaces. The bridge site shows more affinity for the adsorbate as the electron density is reduced at the hollow site due to an increased gap between nickel atoms (as a result of their smaller size) and higher nickel electronegativity.

On the Fe(110) surface, we found the hollow sites to be the preferred adsorption sites for both CO and O species after geometry optimisations (Fig. 5b). The co-adsorption energy was calculated at -202.4 kJ mol $^{-1}$  as shown in Table 3. Compared to the Fe(100) surface, the CO molecule was adsorbed in an upright configuration at the Fe(110) surface. No stable structure was obtained for O at a top or bridge site, as it moved to the hollow site during energy minimization. On the Ni-deposited Fe(110) surface, the hollow sites remained the preferred binding sites for CO and O (Fig. 6b), but the co-adsorption energy of (CO + O) reduced from -202.4 kJ mol $^{-1}$  to -114.6 kJ mol $^{-1}$ . Here again, we see that the nickel reduces the binding strength due to the higher electronegativity of nickel compared to iron. The CO bond is also less activated, *i.e.* being 1.19 Å compared to 1.21 Å on the bare surface due to less electron transfer (see Table 3).

On the Fe(111) surface, we found the preferred adsorption sites for both CO and O at the shallow top sites, with an exothermic adsorption energy of -128.8 kJ mol $^{-1}$  (Fig. 5c and Table 3). On the Ni-deposited Fe(111) surface (Fig. 6c), the co-adsorption of CO and O was calculated at -52.4 kJ mol $^{-1}$  compared to -128.8 kJ mol $^{-1}$  calculated on the bare Fe(111). On the clean Fe surfaces, we observed that (CO + O) binds most strongly to the facet, where CO<sub>2</sub> binds least strongly, with the (CO + O) binding energies following the trend (110) > (100) > (111). On the Ni-deposited surfaces, the observed trend is (100) < (111) < (110), which suggests that the (CO + O) species bind more strongly to the close-packed (110) surface than the more opened (111) surface. This scenario was also observed on

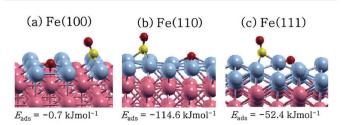


Fig. 6 CO + O initial and final adsorption modes on the nickel monolayer covered Fe (100), (110) and (111) surfaces.

the low Miller index surfaces of nickel,  $^{13}$  where Ni(110), the most open facet, binds CO<sub>2</sub> most strongly but only weakly binds CO + O. The molecular and dissociative (CO + O) binding energies of CO<sub>2</sub> were reported at -7.7 and -116.7 kJ mol $^{-1}$  at Ni(100); -37.6 and -69.5 kJ mol $^{-1}$  at Ni(110); +29.9 and -51.1 kJ mol $^{-1}$  at Ni(111) surfaces, respectively. These results suggest that (CO + O) binds most strongly to the surface with the highest work function, due to the strong affinity of the surface for electrophiles like oxygen.

#### 3.4 Energy barriers to CO<sub>2</sub> activation and dissociation

Unlike the previous studies of  $CO_2$  dissociation energies on  $Fe(100)^{28}$  and  $Fe(111)^{32}$  that focused on the barriers leading to dissociation, we have calculated both the activation energies required for  $CO_2$  adsorption (activation) and dissociation by locating the transition state structures TS1 and TS2 between the stable states of the isolated, adsorbed and dissociated  $CO_2$  molecules on the various iron facets. The reaction energy profiles for  $CO_2$  dissociation on both the bare Fe and Ni-deposited surfaces are shown in Fig. 7, whereas the geometries of stationary point structures along the reaction coordinate are shown in the ESI,† Fig. S4–S6. All of the reported energies were corrected by the zero-point energy ( $\Delta ZPE$ ), calculated as the difference

between the zero point vibrational contributions,  $\left(\sum_{i=1}^{3n-6} \frac{h\nu_i}{2}\right)$ ,

of the final adsorbed  $CO_2$  and the initial gaseous  $CO_2$ , where h is Planck's constant and  $\nu$  is the vibrational frequency.

It can be seen from the energy profile that the CO<sub>2</sub> dissociation step on the facets is the rate-determining step. The rate depends on the barrier to C-O bond dissociation (TS2) and not to adsorption (TS1), which is highest on the bare (110) surface. Although the barrier to CO2 adsorption is rarely explored in the literature, it reveals additional information about the ease of transformation. The negative activation energy barriers (TS1) of  $-9.8 \text{ kJ mol}^{-1} \text{ and } -4.6 \text{ kJ mol}^{-1} \text{ on the Fe}(100) \text{ and Fe}(111)$ surfaces, respectively, suggest a barrier-less reaction to adsorb and activate CO2 on these surfaces. However, an energy barrier of 19.6 kJ mol<sup>-1</sup> has to be overcome to adsorb and activate CO<sub>2</sub> on the Fe(110) surface, indicating that CO2 will more easily desorb from the Fe(110) surface than adsorb and get activated. The energy barriers for dissociation from the activated state on the pure iron surfaces are calculated to be 40.3 kJ mol<sup>-1</sup>, 126.9 kJ  $\text{mol}^{-1}$  and 83.2 kJ  $\text{mol}^{-1}$  on the (100), (110) and (111) facets, respectively, with ZPE correction. The earlier reports of Glezakou et al.<sup>28</sup> on a dissociation energy barrier on the (100) facet of 47.3 kJ mol<sup>-1</sup> and Chen et al.<sup>32</sup> on the (111) facet of **PCCP** Paper

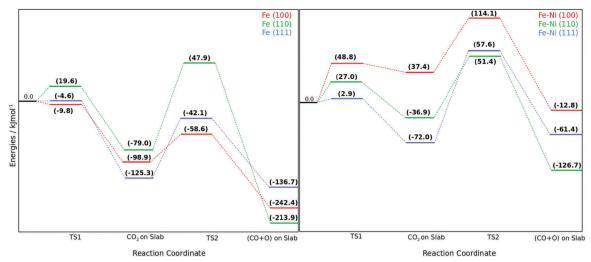


Fig. 7 Energy profile diagram for CO<sub>2</sub> activation and dissociation on the bare and Ni-doped Fe (100), (110) and (111) facets, with all energies corrected by the ZPE contribution

90.9 kJ mol<sup>-1</sup> agree well with our calculated values of 46.3 kJ mol<sup>-1</sup> and 85.6 kJ mol<sup>-1</sup>, respectively, without the zero-point vibrational energy corrections.

On the nickel-deposited surfaces, the barrier to dissociation is lowest on the (100) surface with a barrier of 76.7 kJ mol<sup>-1</sup>, followed by the (110) surface with a barrier of 88.3 kJ mol<sup>-1</sup>, and finally the (111) surface with a barrier of 129.6 kJ  $\text{mol}^{-1}$ . Compared to the bare Fe surfaces, the barriers leading to CO2 dissociation on the Ni-deposited surfaces increased by 36.4 kJ mol<sup>-1</sup> and 46.4 kJ mol<sup>-1</sup> on the (100) and (111) surfaces, respectively, but decreased by 38.6 kJ mol<sup>-1</sup> on the (110) surface. These results correspond to the increased work functions calculated at the (100) and (111) facets upon the deposition of a monolayer of nickel. The work functions on the various facets, i.e. the bare Fe(100), Fe(111), Fe(110) and nickel-coated Fe(100), Fe(111) and Fe(110) surfaces have been calculated to be 3.80, 3.86, 4.57, 4.29, 4.28 and 4.72 eV, respectively.34 Although the dissociated CO2 states are lower in energy than the molecularly adsorbed states, the barriers to be overcome in order to desorb CO2 from the Fe and Ni/Fe surfaces are generally lower than the barriers to dissociate the molecule

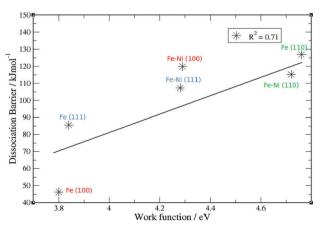
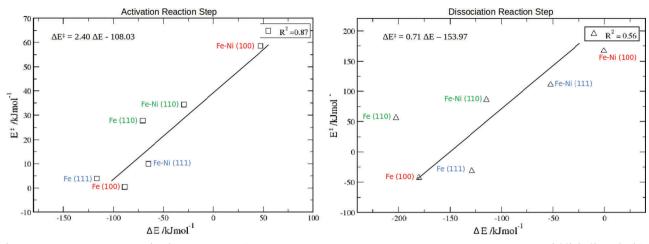


Fig. 8 Plot of work functions of Fe and Fe-Ni (100), (110) and (111) facets against kinetic energy barriers

into CO and O species, suggesting that the adsorbed CO<sub>2</sub> molecule may easily desorb from the surfaces rather than dissociate. On the Ni/Fe(100) and (111) surfaces, the activation energy barriers to dissociation of the CO2 molecule are even higher than the barriers to desorption, indicating that the activated CO2 moiety will either remain molecularly adsorbed or desorbed from these Ni/Fe surface rather than dissociated. A previous study<sup>29</sup> of CO<sub>2</sub> decomposition on (100) surfaces of fcc iron and nickel revealed an increased barrier to dissociation relative to the gaseous CO2, while the barrier from the activated to dissociated states showed that dissociation on Ni(100) was faster, with barriers of 51.0 kJ mol<sup>-1</sup> and 113.4 kJ mol<sup>-1</sup> on nickel and iron, respectively, although CO2 activation was more prominent on the iron facet. As shown in Fig. 8, we obtained a correlation between the work function and the activation energies required for CO2 dissociation, i.e. the higher the work function, the higher the energy barrier to dissociation from its activated state. The regression factor of 0.71 is relatively high and therefore suggests that the work function provides a reasonably accurate indication of the energy requirements for dissociation. The surfaces exhibiting relatively low work functions are more promising for CO<sub>2</sub> activation and dissociation as they favor electron transfer. However, the observed TS1 barriers indicate that CO2 dissociation is favoured only on the pure Fe(100) and Fe(111) surfaces, and not on the other surfaces investigated.

We have also plotted the activation energies for the activation and dissociation steps as a function of the reaction energy (Fig. 9) and derived the Brønsted-Evans-Polanyi (BET) relationship of the activation and dissociation steps of CO2 on the Fe and Ni/Fe surfaces. The BEP relationships are important to estimate reaction barriers on other metal surfaces for C-O bond activation and decomposition. As shown in the plot for the activation barriers  $(\Delta E^{\ddagger})$  and the reaction energies for both the activation and decomposition elementary steps for CO2 dissociation, a linear relationship is obtained, with regression factors of 0.87 and 0.56, respectively. This shows a stronger correlation for the activation step than for the decomposition step, and the

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The Brønsted-Evans-Polanyi (BET) relation; a plot of activation energies against reaction energies on bare and Ni-doped Fe (100), (110) and (111) facets.

BEP relationship has been developed to be  $\Delta E^{\ddagger} = 2.40\Delta E$  – 108.03 (kJ mol<sup>-1</sup>) for CO<sub>2</sub> activation and  $\Delta E^{\ddagger} = 0.71\Delta E - 153.97$ (kJ mol<sup>-1</sup>) for its dissociation.

#### 4. Summary and conclusions

CO<sub>2</sub> adsorption and dissociation were investigated on the lowindex (100), (110) and (111) surfaces of bcc Fe as well as their facets coated with a monolayer of Ni, using density functional theory calculations within the generalized gradient approximation (GGA-PBE) and exchange correlation functional. We have observed that the adsorption energy of CO<sub>2</sub> decreases in the order Fe(111) > Fe(100) > Fe(110) on the clean surfaces, which is consistent with previous studies. However, we have found that the co-adsorption energies of the dissociated products (CO and O) decrease in the reverse order: Fe(110) > Fe(100) > Fe(111). Nickel deposition favours  $CO_2$  adsorption in the order (111) > (110) > (100) and (CO + O) adsorption in the reverse order, except on the (100) facet where binding of adsorbates is not favoured. With the calculated energy barriers, the Brønsted-Evans-Polanyi (BEP) relationship was developed with the kinetic energy barriers and reaction energies for both CO2 activation and dissociation reaction steps. The energy barriers for dissociation of the CO<sub>2</sub> molecule into CO and O species were found to be generally higher than the energy barriers for the activation of the CO<sub>2</sub> molecule. The kinetic energy barriers leading to dissociated CO<sub>2</sub> products on the (100), (110) and (111) surfaces from the activated intermediate were calculated at 40.3 kJ mol<sup>-1</sup>, 126.9 kJ mol<sup>-1</sup> and 83.2 kJ  $\text{mol}^{-1}$ , respectively, which increase on (100) and (111) and reduce on (110) upon deposition of Ni, as shown in their work function alterations, with changes most pronounced on (111) > (100) > (110). The transition state barriers leading to activation and dissociation show that CO2 will prefer to desorb from the Fe(110) facet rather than form surface-bound dissociated species, in good agreement with the experimental results, where at 300 K no CO<sub>2</sub> decomposition was observed on the (110) surface compared to the (111) and (100) surfaces. Deposition of a monolayer of Ni on the Fe(110) facet reduces the rate-determining barriers leading to CO2 dissociation, but generally the unstable activated CO2 on the

various facets will desorb rather than dissociate. The zero point vibrational energy contributions were treated and the energy changes fell within a range of 6.9 to 62 kJ mol<sup>-1</sup>. The direct dissociation process is thermodynamically most favoured on the (110) facet before and after Ni deposition, considering that the activated intermediate is less stable and the dissociated product is most stable on this facet, thus favouring product formation. Thus, at high temperatures CO<sub>2</sub> dissociation into CO and O should be most favourable on the (110) facets. However, despite variations in the work functions of the iron facets upon Ni deposition, suggesting easier decomposition on (110) but not on the (100) and (111) surfaces, CO<sub>2</sub> decomposition is kinetically challenging on the Ni-doped surfaces, due to the instability of the activated CO<sub>2</sub> moiety. These findings indicate that, although reducing the work functions of iron surfaces through deposition of a second metal could enhance the kinetics of the direct dissociation of CO<sub>2</sub>, especially on the most stable and therefore possibly dominant Fe(110) facet, the thermodynamics remain challenging for CO<sub>2</sub> decomposition, probably resulting in CO<sub>2</sub> desorption from the nickel-doped iron surfaces before dissociation of the molecule into surface-bound species.

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