



Cite this: *Phys. Chem. Chem. Phys.*,
2015, 17, 25100

Anomalous system-size dependence of electrolytic cells with an electrified oil–water interface

Marise Westbroek,^{*ab} Niels Boon^c and René van Roij^a

Manipulation of the charge of the dielectric interface between two bulk liquids not only enables the adjustment of the interfacial tension but also controls the storage capacity of ions in the ionic double layers adjacent to each side of the interface. However, adjusting this interfacial charge by static external electric fields is difficult since the external electric fields are readily screened by ionic double layers that form in the vicinity of the external electrodes. This leaves the liquid–liquid interface, which is at a macroscopic distance from the electrodes, unaffected. In this study we show theoretically, in agreement with recent experiments, that control over this surface charge at the liquid–liquid interface is nonetheless possible for macroscopically large but finite closed systems in equilibrium, even when the distance between the electrode and interface is orders of magnitude larger than the Debye screening lengths of the two liquids. We identify a crossover system-size below which the interface and the electrodes are effectively coupled. Our calculations of the interfacial tension for various electrode potentials are in good agreement with recent experimental data.

Received 21st May 2015,
Accepted 26th August 2015

DOI: 10.1039/c5cp02945g

www.rsc.org/pccp

1 Introduction

The ion distribution in the vicinity of charged surfaces in a liquid electrolyte is a classic and important topic within physical chemistry. This field goes back to at least the 1910s when Gouy¹ and Chapman² identified the existence of a diffuse ionic cloud in the vicinity of a charged surface. This ionic cloud with a net charge exactly opposite to that of the surface has a thickness (now called the Debye screening length) typically in the range of 1–1000 nm depending on the ion concentration and the dielectric constant of the electrolyte. This implies that the effect of a static external charge immersed in a bulk electrolyte is only noticeable at distances smaller than several Debye lengths; at larger distances the external charge is fully screened by its surrounding ionic cloud. Indeed, it is well known that the effective electrostatic interactions between colloidal particles stem from their overlapping ionic clouds, thereby setting the interaction range equal to the Debye length of the supporting electrolyte.³ The notion of ionic screening also implies that an electrolyte in between two planar electrodes can (in the absence of chemical reactions) only be manipulated by a static applied voltage if the electrode–electrode separation is of the order of the Debye length

or smaller; macroscopic electrode separations, *e.g.* on the centimetre scale, much larger than any typical Debye length, lead to two fully screened decoupled electrodes sandwiching a bulk electrolyte that is insensitive to the applied static voltage (time-dependent voltages in which ionic clouds need to be built up can have a much longer range). The nature of the distribution of ions in the vicinity of electrified oil–water interfaces has received a lot of recent attention,^{4–8} with theoretical analyses mostly focusing on specific ion and correlation effects that go beyond the mean-field level of the traditional Poisson–Boltzmann theories. The present work, by contrast, takes a different perspective and concentrates on the surprisingly strong influence of the (at first sight macroscopic) electrode–electrode separation and the statistical ensemble (canonical *versus* grand canonical) within which the ions are treated. In order to focus on the key idea, we do not include any ion and correlation effects, except for a phenomenological Born self-energy, in this work, although these effects will play a role in a quantitative analysis of the experiments.

Building on the notion of ionic screening, one would at first sight also expect that a planar interface between two demixed bulk electrolytes (*e.g.* oil and water) sandwiched by two planar electrodes in the geometry of an electrolytic cell cannot be manipulated by the applied voltage if both electrodes are at a macroscopic distance from the interface. Recent experiments, however, challenge this expectation. It was shown that oil–water interfaces, which in the absence of any external potential exhibit two back-to-back ionic double layers due to a repartitioning of the ions,^{9–11} can actually be electrified by ‘remote’

^a Institute for Theoretical Physics, Centre for Extreme Matter and Emergent Phenomena, Leuvenlaan 4, 3584 CE Utrecht, The Netherlands

^b Royal School of Mines, Imperial College, Prince Consort Road, London SW7 2BP, UK. E-mail: mjw13@imperial.ac.uk; Tel: +44 (0)7881983074

^c Department of Materials Science and Engineering, Northwestern University, Evanston, Illinois 60208, USA

external electrodes.^{12,13} In particular, it was shown that the oil–water surface tension could be modified by applying a voltage across electrodes separated from the interface by several centimetres, while the Debye lengths are orders of magnitude smaller.¹³

In the present article we will provide a theoretical explanation of the experimental observations by extending the classical Gouy–Chapman solution of the Poisson–Boltzmann equation to include two electrodes, an oil–water interface, and four ionic species each with their own affinity for oil and water as described by a Born self energy difference between an ion in oil and water. The mechanism that we will describe in this work does not rely on the possible occurrence of (steady-state) ion currents between the electrodes, yet follows entirely from thermodynamic equilibrium in the presence of an applied electric field. Before embarking on a detailed theoretical analysis, we first consider an extreme case that qualitatively illustrates the possible emergence of a large (macroscopic) length scale in this problem. Imagine a demixed oil–water system with two hydrophilic ion species that cannot penetrate into the oil and two hydrophobic ion species that cannot penetrate into the water. The impossibility of ion migration implies that both phases are constrained to be charge neutral, not only in bulk but even if they are put in contact in a macroscopic electrolytic cell of the type cathode–water–oil–anode. Upon the application of a voltage between the cathode and the anode, the cathode will be screened by an excess of hydrophilic cations and the anode by an excess of the hydrophobic anions. However, global neutrality of the individual volumes of water and oil causes the formation of a back-to-back double layer of ionic charge at the oil–water interface, with an excess of hydrophilic anions at the waterside of the interface and an excess of hydrophobic cations at oil side. The neutrality constraint imposes the magnitude of these oil–water ionic excess charges to be identical to that on the electrodes. In other words, in this limiting case the charge of the oil–water interface can be perfectly tuned by the applied voltage across the electrodes, even at macroscopic distances from the interface. By contrast, if at least one of the ionic species is ‘sufficiently’ soluble in both oil and water, then the neutrality constraint only applies to the oil–water system as a whole: ionic excess charge can migrate from one electrode to the other, thereby leaving the oil–water interface unaffected (if the Debye lengths are much smaller than the cell-size). These two extreme cases give rise to the expectation of a crossover from a microscopic to a macroscopic length scale. We will show below that this length scale is of the order of $(|\sigma|/\rho)\exp(|f|)$ with ρ a typical salt concentration and $|f|$ the magnitude of the smallest Born self energy of the four ionic species (in units of the thermal energy $k_B T$). Note that $e\sigma$ is a particle density of the electrodes; the surface charge density is given by $\pm e\sigma$. Clearly $|\sigma|/\rho$ is a microscopic length scale, but with $|f|$ varying from order unity up to 20–30 the exponential dependence on $|f|$ gives rise to a wide range of lengths, strictly speaking microscopic but easily exceeding any realistic macroscopic system size. In cases that this new length scale exceeds the system size, the macroscopic

system is anomalously ‘small’ such that ‘remote’ electrodes can modify the oil–water interface statically.

2 Poisson–Boltzmann theory of an electrified oil–water interface

2.1 Gouy–Chapman theory for a single electrode

Before considering the actual system of interest in this study, the electrified oil–water interface as illustrated in Fig. 1, we remind ourselves of the simpler problem of a single planar electrode in contact with a half-space of a 1:1 electrolyte, treated within Poisson–Boltzmann theory for point ions. Assuming lateral translational invariance, and denoting the perpendicular distance to the electrode by $z > 0$, we wish to calculate the electrostatic potential $\Psi(z)$ and equilibrium concentration profiles of the cations and anions $\rho_+(z)$ and $\rho_-(z)$, respectively. Setting the potential far from the electrode to zero, $\Psi(\infty) = 0$, and denoting the bulk ion concentration by ρ , so that $\rho_+(\infty) = \rho_-(\infty) \equiv \rho$ by bulk neutrality, we relate the ion distributions to the electric potential for $z > 0$ via the Boltzmann distribution $\rho_{\pm}(z) = \rho \exp[\mp \phi(z)]$ with the dimensionless potential $\phi(z) = e\Psi(z)/k_B T$. Here e is the proton charge, T the temperature, and k_B the Boltzmann constant. The two Boltzmann distributions are complemented by the Poisson equation $\phi''(z) = -4\pi\lambda_B[\rho_+(z) - \rho_-(z) + \sigma\delta(z)]$ for $z \geq 0$, where a prime denotes a derivative with respect to z , where $\lambda_B = e^2/\epsilon k_B T$ is the Bjerrum length (in Gaussian units) of the solvent in terms of its

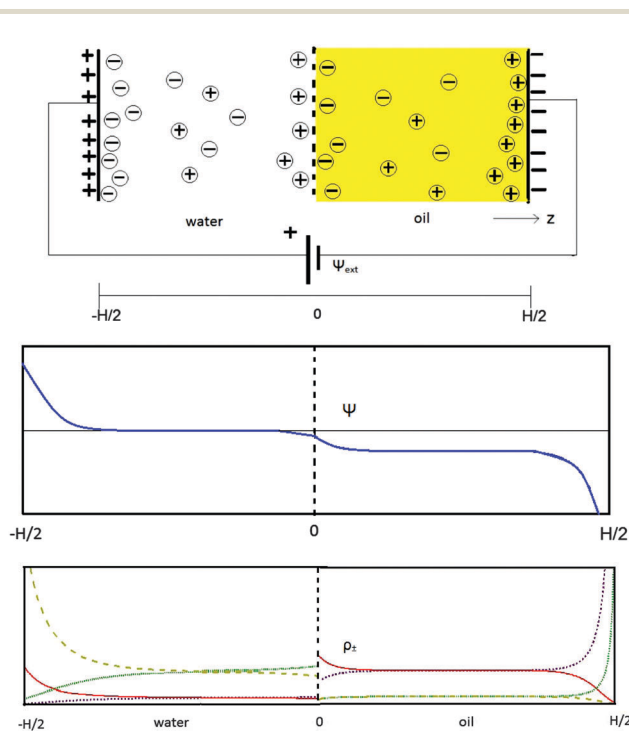


Fig. 1 Model: closed system containing an electrified oil–water interface, and typical electrostatic potential and density profiles for two different salts. Cations experience a high potential at the left electrode due to the positive surface charge; their concentration is therefore low at $z = -H/2$ (green and purple lines). The opposite is true for the anions (green and yellow lines).

relative dielectric constant ϵ , and where the surface charge density in the plane $z = 0$ of the electrode is given by $e\sigma$. Combining these results gives the Poisson–Boltzmann equation with its boundary conditions

$$\begin{aligned}\phi''(z) &= \kappa^2 \sinh \phi(z); \\ \phi(\infty) &= 0; \\ \phi'(0^+) &= -4\pi\lambda_{\text{B}}\sigma,\end{aligned}\quad (1)$$

where the screening parameter is defined as $\kappa^2 = 8\pi\lambda_{\text{B}}\rho$. This closed set of equations can be solved analytically to yield^{1,2,15}

$$\phi(z) = 2 \log \left[\frac{1 + \gamma \exp(-\kappa z)}{1 - \gamma \exp(-\kappa z)} \right], \quad (2)$$

where the integration constant is given by

$$\gamma = \frac{\sqrt{(2\pi\lambda_{\text{B}}\kappa^{-1}\sigma)^2 + 1} - 1}{2\pi\lambda_{\text{B}}\kappa^{-1}\sigma}. \quad (3)$$

Note that $-1 < \gamma < 1$, that $\gamma \propto \sigma$ in the linear screening (low surface charge) regime $|\sigma| \ll \sigma^* \equiv (\pi\lambda_{\text{B}}\kappa^{-1})^{-1}$, and that $|\gamma|$ approaches unity in the strongly nonlinear screening limit (high surface charge) $|\sigma| \gg \sigma^*$. The dimensionless potential $\phi(z)$ of eqn (2) and the associated ion distributions $\rho_{\pm}(z) = \rho \exp[\mp \phi(z)]$ describe the well-known diffuse ionic screening cloud of typical thickness κ^{-1} (the Debye length) in the vicinity of the electrode. In the present context we are interested in the cation and anion adsorptions, *i.e.* the excess number of ions per unit electrode area, defined by $\Gamma_{\pm} \equiv \int_0^{\infty} dz(\rho_{\pm}(z) - \rho)$. It follows from eqn (2) and (3) that

$$\Gamma_{\pm} = \frac{\mp 4\rho}{\kappa} \frac{\gamma}{1 \pm \gamma}. \quad (4)$$

One checks that $\Gamma_+ - \Gamma_- + \sigma = 0$, such that charge neutrality is satisfied. We note, however, that the total ion adsorption $\Gamma_+ + \Gamma_- = \sigma^*/(\gamma^{-2} - 1)$ depends nontrivially on the total surface charge: it is vanishingly small in the linear-screening regime but grows with increasing surface charge to become of the same order as σ^* if $\gamma \simeq 0.5$, and it diverges in the limit of highly charged surfaces (where the underlying assumption of point ions breaks down. This limit is not of concern in this study).

2.2 Open electrified oil–water interface

From the single planar interface discussed so far we now extend our study and consider an electrolytic cell viewed as three coupled planar interfaces, as illustrated in Fig. 1. The cell is bounded by two planar electrodes at a distance H from each other in the planes $z = \pm H/2$, and it is filled with two equal volumes of immiscible electrolytes forming an interface in the plane $z = 0$. The two electrolytes will be referred to as “water” ($-H/2 < z < 0$) and “oil” ($0 < z < H/2$), which are both assumed to be structureless dielectric liquids fully characterized by their relative dielectric constants ϵ_{w} and ϵ_{o} , respectively, which in turn determine the Bjerrum lengths $\lambda_{\text{B}}^{\text{w}}$ in water and $\lambda_{\text{B}}^{\text{o}}$ in oil. In order to compare our results with the experiments of ref. 13, we will take $\lambda_{\text{B}}^{\text{w}} = 0.72$ nm and $\lambda_{\text{B}}^{\text{o}} = 5.43$ nm throughout this work. We consider two salts, yielding four

different ion species, which we assume all to be monovalent here. The difference of the ionic solvation free energy between oil and water is for each individual ion species denoted by $k_{\text{B}}Tf_{\alpha\pm}$, with $\alpha = \{1, 2\}$, such that $f_{\alpha\pm} > 0$ for hydrophobic ion species and $f_{\alpha\pm} < 0$ for hydrophilic ion species. In line with the point-like nature of the ions and the sharp planar interface between water and oil at $z = 0$, we define the external potential for the ion species $\alpha\pm$ as

$$V_{\alpha\pm}(z) = \begin{cases} 0 & \text{if } z < 0 \\ k_{\text{B}}Tf_{\alpha\pm} & \text{if } z > 0, \end{cases} \quad (5)$$

where the zero of solvation free energy is chosen in the water phase. We are interested in the relation between the imposed potential difference $\Delta\Psi$ between the two electrodes and the salt concentration in the electrolytes on the one hand, and the resulting electrode charge densities $+e\sigma$ at $z = -H/2$ and $-e\sigma$ at $z = +H/2$, the ion concentration profiles $\rho_{\alpha\pm}(z)$, and the dimensionless electrostatic potential $\phi(z)$ for $z \in [-H/2, H/2]$ on the other hand. It turns out to be convenient, however, to use σ as a control variable, and to calculate $\Delta\Psi$.

We will consider macroscopically large cells with two well-defined bulk states, one in the vicinity of $z = -H/4$ in the water phase between the electrode–water interface and the water–oil interface, and the other in the vicinity of $z = +H/4$ in the oil phase between the water–oil interface and the oil–electrode interface. Asymptotically far from both the electrodes and the water–oil interface, the ion concentration profiles $\rho_{\alpha\pm}(z)$ and the dimensionless electrostatic potential $\phi(z)$ take constant bulk values. It is convenient to gauge the electrostatic potential in bulk water at zero, so $\phi(-H/4) = 0$, and to use the ionic bulk concentrations in water, denoted by $\rho_{\alpha\pm}(-H/4) \equiv \rho_{\alpha\pm}^{\text{w}}$, as control variables. Using the ionic bulk concentrations $\rho_{\alpha\pm}^{\text{w}}$ as control variables implies a grand-canonical treatment of the ions, and in this sense the system is regarded as “open”. Bulk neutrality imposes that $\sum_{\alpha} (\rho_{\alpha+}^{\text{w}} - \rho_{\alpha-}^{\text{w}}) = 0$. Note that, while bulk neutrality is required within the grand-canonical treatment, charge can accumulate at at both electrodes as well as at the interface, and separate phases are not necessarily charge neutral. With these definitions, the Boltzmann distribution of the ions throughout the cell takes the form

$$\rho_{\alpha\pm}(z) = \rho_{\alpha\pm}^{\text{w}} \exp[\mp \phi(z) - V_{\alpha\pm}(z)/k_{\text{B}}T], \quad (6)$$

which in the bulk oil phase leads to bulk ion concentrations $\rho_{\alpha\pm}(H/4) \equiv \rho_{\alpha\pm}^{\text{o}}$ given by

$$\rho_{\alpha\pm}^{\text{o}} = \rho_{\alpha\pm}^{\text{w}} \exp[\mp \phi_{\text{D}} - f_{\alpha\pm}]. \quad (7)$$

Here the so-called Donnan potential of the bulk oil phase, $\phi_{\text{D}} \equiv \phi(H/4)$, follows from the neutrality condition in the bulk oil, $\sum_{\alpha} (\rho_{\alpha+}^{\text{o}} - \rho_{\alpha-}^{\text{o}}) = 0$, which can be rewritten as

$$\phi_{\text{D}} = \frac{1}{2} \log \left(\frac{\sum_{\alpha} \rho_{\alpha+}^{\text{w}} \exp(-f_{\alpha+})}{\sum_{\alpha} \rho_{\alpha-}^{\text{w}} \exp(-f_{\alpha-})} \right). \quad (8)$$

Note that eqn (8) only holds for monovalent ions. The numerator in the logarithm contains a sum over all cation species and the denominator sums over all anionic species.

With the (neutral) bulk oil state completely specified in terms of the bulk water state and the self-energy parameters f_x in eqn (7) and (8), we are now ready to describe the three interfaces. By writing the Poisson equation as $\phi''(z) = -4\pi\lambda_B^{w,o} \sum_x (\rho_{x+}(z) - \rho_{x-}(z))$, where one should take λ_B^w for $-H/2 < z < 0$ and λ_B^o for $0 < z < H/2$, and introducing the screening constants $\kappa_w^2 = 4\pi\lambda_B^w \sum_x (\rho_{x+}^w + \rho_{x-}^w)$ and $\kappa_o^2 = 4\pi\lambda_B^o \sum_x (\rho_{x+}^o + \rho_{x-}^o)$, one can write the resulting Poisson-Boltzmann equation as

$$\phi''(z) = \begin{cases} \kappa_w^2 \sinh \phi(z) & \text{if } z < 0 \\ \kappa_o^2 \sinh(\phi(z) - \phi_D) & \text{if } z > 0, \end{cases} \quad (9)$$

with boundary conditions on the interfaces at $z = \pm H/2$ and at $z = 0$, and with appropriate asymptotic bulk states at $z = \pm H/4$, given by

$$\begin{aligned} \phi'(-H/2) &= -4\pi\lambda_B^w\sigma; \\ \phi(-H/4) &= 0; \\ \phi(0^-) &= \phi(0^+); \\ \varepsilon_w\phi'(0^-) &= \varepsilon_o\phi'(0^+); \\ \phi(H/4) &= \phi_D; \\ \phi'(H/2) &= -4\pi\lambda_B^o\sigma. \end{aligned} \quad (10)$$

Here 0^\pm is short for the limit to $z = 0$ from below ($-$) or from above ($+$). Typically, H is orders of magnitude larger than either of the two Debye lengths κ_w^{-1} and κ_o^{-1} , such that $H/4$ can be seen as an asymptotic “infinite” distance from electrodes and/or the oil-water interface. The solution of this set of equations can therefore be written as follows, in analogy with eqn (2):

$$\phi(z) = \begin{cases} 2\log \left\{ \frac{1 + \gamma_w \exp \left[-\kappa_w \left(z + \frac{H}{2} \right) \right]}{1 - \gamma_w \exp \left[-\kappa_w \left(z + \frac{H}{2} \right) \right]} \right\}, & \text{if } z \in \left[\frac{-H}{2}, \frac{-H}{4} \right]; \\ 2\log \left\{ \frac{1 + C_w \exp(\kappa_w z)}{1 - C_w \exp(\kappa_w z)} \right\}, & \text{if } z \in \left[\frac{-H}{4}, 0 \right]; \\ 2\log \left\{ \frac{1 + C_o \exp(-\kappa_o z)}{1 - C_o \exp(-\kappa_o z)} \right\} + \phi_D, & \text{if } z \in \left[0, \frac{H}{4} \right]; \\ 2\log \left\{ \frac{1 + \gamma_o \exp \left[\kappa_o \left(z - \frac{H}{2} \right) \right]}{1 - \gamma_o \exp \left[\kappa_o \left(z - \frac{H}{2} \right) \right]} \right\} + \phi_D, & \text{if } z \in \left[\frac{H}{4}, \frac{H}{2} \right]. \end{cases} \quad (11)$$

The integration constants γ_w and γ_o are fixed by the boundary conditions at $z = \pm H/2$, and are analogous to the integration constant for the single-electrode case, eqn (3), given by

$$\gamma_w = \frac{\sqrt{(2\pi\lambda_B^w\kappa_w^{-1}\sigma)^2 + 1} - 1}{2\pi\lambda_B^w\kappa_w^{-1}\sigma}; \quad (12)$$

$$\gamma_o = \frac{\sqrt{(2\pi\lambda_B^o\kappa_o^{-1}(-\sigma))^2 + 1} - 1}{2\pi\lambda_B^o\kappa_o^{-1}(-\sigma)}. \quad (13)$$

The integration constants C_w and C_o follow from the two continuity conditions at $z = 0$ (eqn (10)), such that

$$C_w = \frac{\kappa_o + \exp(\phi_D)\kappa_o + 2\exp\left(\frac{\phi_D}{2}\right)\kappa_w\frac{\varepsilon_w}{\varepsilon_o}}{\kappa_o(\exp(\phi_D) - 1)} - \frac{2\sqrt{k}}{\kappa_o(\exp(\phi_D) - 1)}; \quad (14)$$

$$C_o = \frac{\kappa_w\frac{\varepsilon_w}{\varepsilon_o} + \exp(\phi_D)\kappa_w\frac{\varepsilon_w}{\varepsilon_o} + 2\kappa_o\exp\left(\frac{\phi_D}{2}\right)}{\kappa_w(\exp(\phi_D) - 1)} - \frac{2\sqrt{k}}{\kappa_w(\exp(\phi_D) - 1)}; \quad (15)$$

with

$$k = \exp(\phi_D) \left(\kappa_o^2 + \kappa_w^2 \left(\frac{\varepsilon_w}{\varepsilon_o} \right)^2 + 2\kappa_o\kappa_w\frac{\varepsilon_w}{\varepsilon_o} \cosh\left(\frac{\phi_D}{2}\right) \right).$$

The dimensionless charge density σ is imposed on the left electrode.

We have obtained the closed-form expression for $\phi(z)$ as represented by eqn (11) in terms of the bulk ion concentrations $\rho_{x\pm}^w$ in the water phase, the energy differences $k_B T f_{x\pm}$, and the electrode charge densities $\pm e\sigma$. The ionic concentration profiles follow explicitly from insertion of $\phi(z)$ into the Boltzmann distribution of eqn (6). Moreover, two emerging electrostatic quantities can be deduced from our results. The first is the voltage $\Delta\psi$ between the electrodes, which is given by

$$\Delta\psi = \frac{k_B T}{e} (\phi(-H/2) - \phi(H/2)). \quad (16)$$

The second quantity is the apparent surface charge density $e\sigma' \equiv e \int_{-H/4}^0 dz \sum_x (\rho_{x+}(z) - \rho_{x-}(z))$ at the water-side of the interface, which by global neutrality is the opposite of the apparent surface charge density at the oil-side of the interface. Using the Poisson equation and applying the Gauss law, we find

$$\sigma' = \frac{\phi'(0^-)}{4\pi\lambda_B^w} = \left(= \frac{\phi'(0^+)}{4\pi\lambda_B^o} \right). \quad (17)$$

Moreover, for later reference we will also calculate the adsorption $\Gamma_{x\pm}^{ab}$ of cation/ion species x to the a-b interface, where a-b can refer to the electrode-water (e-w), the water-oil (w-o), or the oil-electrode (o-e) interface. In line with eqn (4) we now find

$$\begin{aligned} \Gamma_{x\pm}^{ew} &= \frac{\mp 4\rho_{x\pm}^w \gamma_w(\sigma)}{\kappa_w (1 \pm \gamma_w(\sigma))}; \\ \Gamma_{x\pm}^{ow} &= \frac{\mp 4\rho_{x\pm}^w \gamma_w(\sigma')}{\kappa_w (1 \pm \gamma_w(\sigma'))} + \frac{\mp 4\rho_{x\pm}^o \gamma_o(\sigma')}{\kappa_o (1 \pm \gamma_o(\sigma'))}; \\ \Gamma_{x\pm}^{oe} &= \frac{\mp 4\rho_{x\pm}^o \gamma_o(-\sigma)}{\kappa_o (1 \pm \gamma_o(-\sigma))}, \end{aligned} \quad (18)$$

which with eqn (12) gives analytic expressions in terms of the control variables.

For fixed ion concentrations in bulk water, and for fixed surface charge density on the electrodes $\pm e\sigma$ we have thus found explicit results for the voltage $\Delta\Psi$ between the electrodes, the Donnan potential $\Psi_D = (k_B T/e)\phi_D$ between water and oil, the ion concentrations $\rho_{\alpha\pm}^o$ in the bulk oil phase, the degree of charge separation σ' at the oil–water interface and the ion adsorption at the three interfaces of the cell. Note that for convenience we use σ as a control variable with a resulting voltage $\Delta\Psi$ that we calculate, although we could have reversed this by fixing $\Delta\Psi$ and calculating the resulting electrode charge σ , a procedure that would be closer to the experimental reality. However, the one-to-one relation between voltage and charge renders both alternatives equivalent.

2.3 Closed electrified water–oil interface

Interestingly, for fixed $f_{\alpha\pm}$ our analysis of the open system above also reveals that the Donnan potential ϕ_D as defined in eqn (8) only depends on the set of concentrations $\rho_{\alpha\pm}^w$ in bulk water, and not on the cell size H or the electrode charge density σ . The same holds for the ion concentrations $\rho_{\alpha\pm}^o$ in bulk oil given in eqn (7), for the integration constants C_w and C_o in eqn (14), and hence also for the interfacial surface charge density σ' . In other words, for fixed $\rho_{\alpha\pm}^w$ all thermodynamic and electrostatic properties of the “electrified” oil–water interface are independent of the electrode separation, charge, and voltage. This independence is easy to understand qualitatively if one realizes that the electrode charge is completely screened beyond a few Debye lengths κ_w^{-1} and κ_o^{-1} , which are assumed to be much smaller than the cell size H . However, in the experiments of ref. 13 it is argued that the properties of a water–oil interface can be tuned significantly by applying a voltage, even if H is in the centimetre regime and the Debye lengths in the nanometre regime, *i.e.* in a regime where the assumption of asymptotically large H should be perfectly valid. The present theory can only explain the tunable electrified water–oil interface if the electrode charging process affects the bulk ion concentrations. This seems unlikely at first sight, in view of the macroscopic (cm-range) size of the cell. However, below we will show that charging the electrodes while treating the ions either canonically or grand-canonically makes a qualitative difference. We will identify a new length scale H^* , of the order of $\sigma \exp(|f|)/\rho^w$, which can be of order mm-m for typical self-energies $|f| = \min_{\alpha\pm}\{|f_{\alpha\pm}|\} \simeq 10\text{--}20$, typical electrode charges $\sigma \simeq \text{nm}^{-2}$, and typical salt concentrations $\rho_{\alpha\pm}^w \simeq \text{mM-M}$. Only for $H \gg H^*$ is the system size large enough for the charging process of the electrodes to be viewed as grand canonical in the ions. For smaller cells a canonical treatment turns out to be appropriate. For that reason we now consider a closed system with fixed numbers $N_{\alpha\pm}$ of cations/anions of species α .

Denoting the total surface area of an electrode by A , such that the volume of the cell is AH , we can write

$$N_{\alpha\pm} = \frac{AH}{2}\rho_{\alpha\pm}^w + \frac{AH}{2}\rho_{\alpha\pm}^o + A(\Gamma_{\alpha\pm}^{ew} + \Gamma_{\alpha\pm}^{ow} + \Gamma_{\alpha\pm}^{oc}), \quad (19)$$

where we note that $\rho_{\alpha\pm}^o$ and all $\Gamma_{\alpha\pm}^{\text{ab}}$ are explicitly known in terms of the set of bulk water concentrations $\{\rho_{\alpha\pm}^w\}$. In other words, the right hand side of eqn (19) is an explicit function of these variables,

and hence we can view eqn (19) as a closed set of equations to calculate $\rho_{\alpha\pm}^w$ for given $N_{\alpha\pm}$ at fixed A and H .

We will focus on the specific case of an inorganic (hydrophilic) salt (*e.g.* NaCl) and an organic (hydrophobic) salt, corresponding to $\alpha = 1$ and $\alpha = 2$ respectively. We assume complete dissociation and therefore set $N_{1+} = N_{1-} = AH\rho_1$ and $N_{2+} = N_{2-} = AH\rho_2$, where ρ_1 and ρ_2 are the (imposed) overall concentration of the inorganic and organic salt in the cell, respectively. By inserting these definitions into eqn (19) the dependence on the surface area A cancels, and we can apply standard numerical root finding procedures to calculate the four unknown bulk water concentrations $\rho_{\alpha\pm}^w$ for fixed ρ_1 , ρ_2 , σ , H , and $f_{\alpha\pm}$.

3 Numerical results

The relation between σ' and σ is useful in understanding the response of the system to charging the electrodes. We will distinguish between two limiting cases, referred to as the canonical and the grand-canonical limit. The grand-canonical limit is attained when the oil–water interface is effectively decoupled from the electrodes by a sufficiently large distance $\frac{H}{2}$: σ' can be nonzero but does not depend on σ . By contrast, σ' can be manipulated one-to-one by σ in the canonical limit. For fixed self-energies $f_{\alpha\pm}$ and canonical bulk densities $\rho_\alpha = \frac{N_\alpha}{AH}$ we study the effects of the system size, characterized by the separation H between the two planar electrodes. Fig. 2 shows the relation between the oil–water charge σ' and σ for $H = 10^8, 10^9, 10^{10}$ and 10^{11} nm, for system parameters $f_{\alpha\pm} = (-22, -12, 12, 18)$ and $\rho_1 = 2.7$ mM; $\rho_2 = 10$ mM. The largest value of H clearly shows a relatively low interfacial charge σ' , that is, moreover, only weakly dependent on the electric charge.

For fixed values of ionic self-energy differences $f_{\alpha\pm}$ the crossover length H^* marks the transition between the canonical and the grand-canonical regime. We will determine the latter as the point

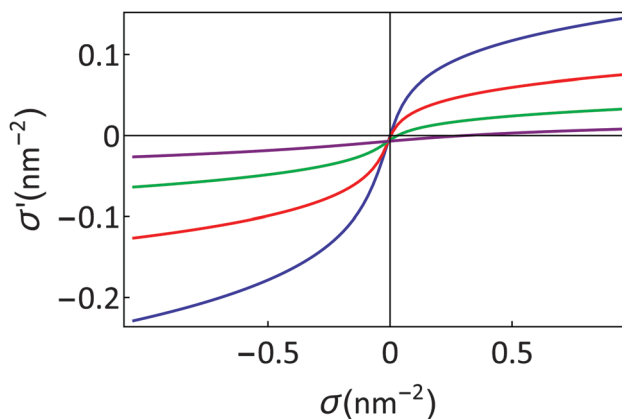


Fig. 2 The charge accumulation σ' at the interface, as defined in eqn (17) as a function of the electrode surface charge density σ for ionic self-energies $f_{\alpha\pm} = (-22, -12, 12, 18)$, for canonical inorganic and organic ion concentrations $\rho_1 = 2.7$ mM and $\rho_2 = 10$ mM. The flat curve corresponds to $H = 10^{11}$ nm; increasingly steeper graphs show $H = 10^{10}$, $H = 10^9$ and $H = 10^8$ nm, respectively.

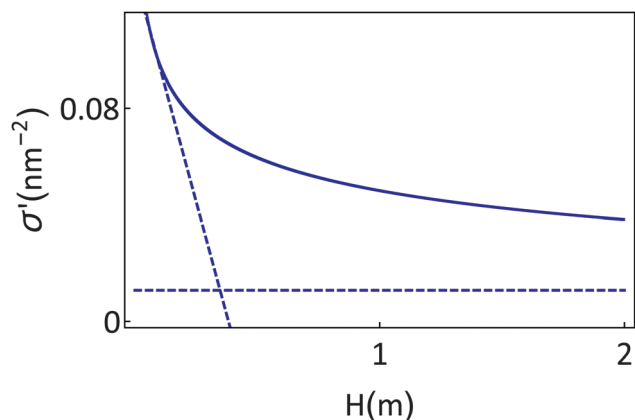


Fig. 3 The oil–water charge density σ' as a function of the electrode–electrode separation H (solid line) and its value in the limit of infinite H (dashed) for $\rho_1 = 2.7$ mM, $\rho_2 = 10$ mM, $\sigma = 0.3$ nm $^{-2}$ and $f_{\pm} = (-29.9, -22.9, 22.3, 21.2)$. The crossover length H^* is given by the value of H where the line tangent to the curve at small H and the limiting (grand-canonical) value of σ' intersect.

where the tangent line to $\sigma'(H)$ for small (≈ 100 nm) values of H equals the grand-canonical value of σ' , as is illustrated in Fig. 3.

Crossover lengths for $(f_{1-}, f_{1+}, f_{2-}, f_{2+})$ of the forms $(-f, 0, 0, f)$, $(-f, 0, f, f)$ and $(-f, -f, f, f)$ are shown in Fig. 4, suggesting that $H^* \approx a \exp f$ in the latter case. This can be understood as follows: if all ion species have a strong preference for their native phase, then the majority of the ions will remain in that phase, e.g. $\rho_{1\pm}^w \approx 2\rho_1$ and $\rho_{2\pm}^o \approx 2\rho_2$. The small fraction that migrates from the native phase to the other phase is, following from eqn (7), described by $\rho_{1\pm}^o \approx 2\rho_1 \exp[\mp \phi_D - f_{1\pm}]$ and $\rho_{2\pm}^w \approx 2\rho_2 \exp[\pm \phi_D + f_{2\pm}]$. As we have seen before, the Donnan potential that enters here implicitly depends on these ion densities. However, as we are interested in the dependence of σ' on H for sufficiently small H , we may approximate ϕ_D assuming $\sigma' \approx \sigma$. Eqn (2) can be applied to find the electrostatic potential difference between the bulk water phase and the charged interface, as well as the electrostatic potential difference between the charged interface and the bulk oil phase. The sum of these contributions adds up to the Donnan potential, which for the parameters in Fig. 4 is $\phi_D \approx -2.6$. Charge neutrality dictates that the apparent charge of the interface is related to the number of ions that have migrated, $\sigma' \approx \sigma - \frac{H}{2}(-\rho_{1+}^o + \rho_{1-}^o + \rho_{2+}^w - \rho_{2-}^w)$. This approximation holds for the case that the double layers occupy only a small portion of both phases, which is increasingly accurate for $H \gg \kappa_w^{-1}$ and $H \gg \kappa_o^{-1}$. Although all four ion species migrate, they do so in different proportions. Those that are subject to a low self-energy penalty and/or those that lower their electrostatic energy upon crossing the barrier can be the dominant migrating species and will therefore have a decisive influence on σ' for small H . For the special case $(-f, -f, f, f)$ that we consider in Fig. 4, the process is governed by the cations that migrate from the water phase to the oil phase as well as the anions that migrate from the oil phase to the water phase. We therefore find $\sigma' \approx \sigma - H(\rho_1 + \rho_2) \exp(f - |\phi_D|)$, and thus

$$H^* \approx \frac{\sigma}{(\rho_1 + \rho_2)} \exp(f - |\phi_D|). \quad (20)$$

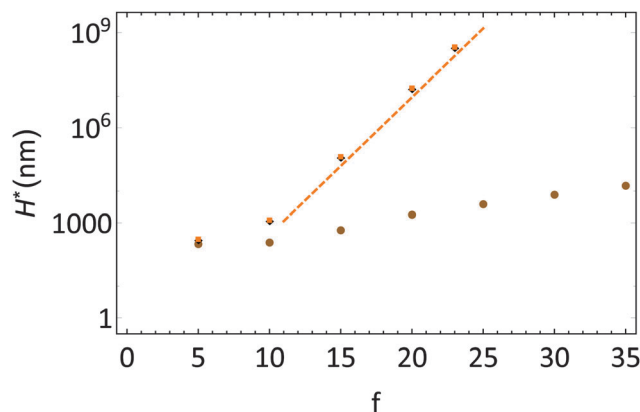


Fig. 4 Grand-canonical to canonical crossover electrode–electrode separation H^* as a function of the self-energy parameter f , for electrode charge density $\sigma = 0.3$ nm $^{-2}$ and $\rho_1 = \rho_2 = 1$ M. The upper curve signifies the set of self-energies $(-f, -f, f, f)$ and the two (almost indistinguishable) lower curves represent the two sets of self-energies $(-f, 0, f, f)$ and $(-f, 0, 0, f)$, which contain at least one ionic species without a preference for either phase. The theoretical approximation $H^* \approx 0.019 \exp(f)$ fit was added for the upper curve, for the range $|f| \geq 11$.

The dashed line in Fig. 4 represents this analytical approximation to H^* , demonstrating very good agreement with our numerical approach. We also include numerical data corresponding to the parameters sets $(-f, 0, f, f)$ and $(-f, 0, 0, f)$ in the figure, which turn out to be barely distinguishable from each other. Our results therefore indicate that the presence of one ion species without a preference for water or oil will affect the system in much the same way as two species with this zero self-energy difference, resulting in a decrease of the crossover length by orders of magnitude in both cases. The analytical approach that we described above cannot be applied to quantitatively estimate H^* for these cases, since some of the ion species have no preference for either phase. Nevertheless, it can be understood from e.g. eqn (20) that decreasing f to small values yields a dramatic decrease in H^* , which is in line with our observations.

The experiments of ref. 13 formed a direct motivation to study the electrolytic cell in more detail. An electrolytic cell of length $H = 4$ cm containing aqueous ($\epsilon_w = 78.54$) and organic ($\epsilon_o = 10.43$) electrolyte solutions is considered at $T = 294$ K. Sodium chloride was dissolved in water to produce a 10 mM solution. A solution of BTPPATPFB in DCE was prepared at a concentration of 5 mM. Because of the low dielectric constant of DCE only partial dissociation into BTPPA $^+$ and TPFB $^-$ occurs, producing an organic solution with a dissociated ionic concentration of 2.7 mM.¹³ The differences between the bulk values of the potentials of mean force (PMFs), which were modeled by molecular dynamics (MD) simulations, are given by¹⁶

$$(f_{\text{TPFB}^-}, f_{\text{BTPPA}^+}, f_{\text{Cl}^-}, f_{\text{Na}^+}) = (-29.9, -22.9, 22.3, 21.2).$$

In Fig. 5 we examine three parameter sets of the self-energies:

(1) $f_{\pm} = (-29.9, -22.9, 22.3, 21.2)$ (experimental values of the Gibbs free energies)

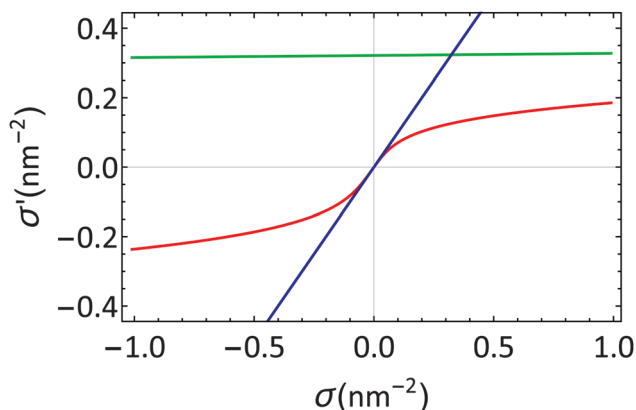


Fig. 5 Oil–water interface charge density σ' as a function of the electrode charge density σ for electrode separation $H = 4$ cm, contrasting $f_{x\pm} = (-29.9, 0, 0, 21.2)$ (green line: grand-canonical), $f_{x\pm} = (-29.9, -22.9, 22.3, 21.2)$ (red line: almost entirely canonical) and $f_{x\pm} = (-49.9, -42.9, 42.3, 41.2)$ (blue line: canonical). Canonical densities are $\rho_1 = 2.7$ mM (oily solution) and $\rho_2 = 5$ mM (aqueous solution).

(2) $f_{x\pm} = (-29.9, 0, 0, 21.2)$ (Gibbs free energies of transfer, where self-energies of BTPPA⁺ and Cl⁻ have been set to zero)

(3) $f_{x\pm} = (-49.9, -42.9, 42.3, 41.2)$ (Gibbs free energies after addition of 20: the canonical limit is appropriate for these self-energies).

Fig. 5 shows that the set of experimental self-energy parameters (set 1) gives rise to an oil–water interfacial charge density σ' that can indeed be tuned throughout the interval $[-0.15, +0.12]$ nm⁻² by the electrode charge $\sigma \in [-0.3, +0.3]$ nm⁻², very strongly so in the small- σ regime $|\sigma| < 0.05$ nm⁻² where $\sigma' = \sigma$, and only weakly for larger σ where σ' approaches a saturation regime. The ability to tune σ' of parameter set 1 is to be contrasted by the behavior of set 2 with two ion species having a vanishingly small self-energy, which gives rise to a large interfacial charge density $\sigma' = +0.33$ nm⁻² that is, however, not at all tunable by the electrode charge σ . For set 3, with its additional $20k_B T$ of self-energy for all ionic species (which essentially prevents any ion migration to the unfavoured solvent), we see from Fig. 5 that perfect tuning is possible with $\sigma' = \sigma$ in the whole regime of σ that is considered.

The grand-canonical behaviour that is revealed by the self-energies of set 2 (for the present ion concentration and system size) in Fig. 5 is also observed for any self-energy set that contains at least one vanishing self-energy, since in such a case the presence/absence of this ‘transferable’ ion can take care of the screening of the electrodes, thereby decoupling the oil–water interface from the electrodes. We also find that a minimum value of about $|f_{x\pm}| > 20$ is needed for all ion species in order to be able manipulate σ' by σ to a degree comparable that of set 1.

4 Surface tension

In the experiments of ref. 13 the surface tension of the electrified oil–water interface was measured. Here we compare these

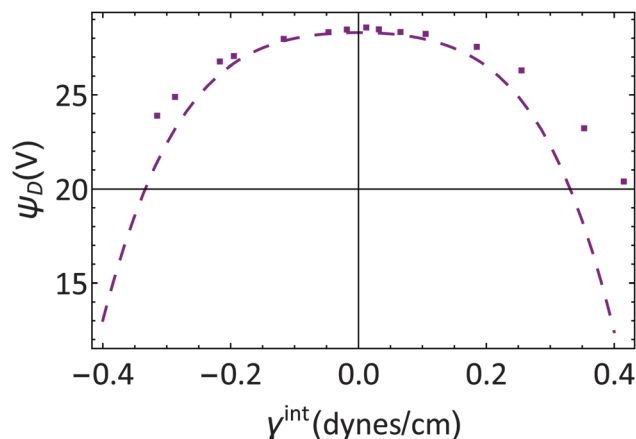


Fig. 6 The interfacial tension γ^{int} as a function of the Donnan potential in volts as derived from density functional theory (dotted line) and as measured at the oil–water interface of an electrolytic cell,¹⁴ for $f_{x\pm} = (-29.9, -22.9, 22.3, 21.2)$, $\rho_1 = 2.7$ mM, $\rho_2 = 10$ mM and electrode–electrode separation $H = 4$ cm. The experimentally imposed potential difference between bulk water and bulk oil is shifted by the potential of zero charge ($\Delta\phi^{\text{pzc}}$).¹⁴ An experimental constant of 28.3 dynes per cm was added to the results of the DFT in order to account for the bare oil–water tension.

measurements with our theoretical results. The interfacial tension γ^{int} as obtained from density functional theory reads

$$\begin{aligned} \gamma^{\text{int}}/k_B T = & \rho^{\text{w}} \int_{-H/4}^0 dz [\phi(z) \sinh(\phi(z)) - 2 \cosh(\phi(z)) + 2] \\ & + \rho^{\text{o}} \int_0^{H/4} dz [\tilde{\phi}(z) \sinh(\tilde{\phi}(z)) - 2 \cosh(\tilde{\phi}(z)) + 2] \\ & + \frac{1}{2} \sigma' \phi_{\text{D}}, \end{aligned} \quad (21)$$

where $2\rho^{\text{o/w}} = \rho_{1+}^{\text{o/w}} + \rho_{1-}^{\text{o/w}} + \rho_{2+}^{\text{o/w}} + \rho_{2-}^{\text{o/w}}$. A derivation of eqn (21) can be found in the Appendix.

Surface tension measurements¹³ and the interfacial tension as obtained here from density functional theory (DFT) are compared in Fig. 6. Experimentally, a potential difference $\Delta\phi^{\text{wo,cell}}$ between the electrodes is imposed. When no external voltage is applied, the potential differences between the three interfaces electrode–water, water–oil and oil–electrode add up to zero, but the potential difference between bulk water and bulk oil ϕ_{D} may well be nontrivial. This potential is translated over the offset potential of zero charge $\Delta\phi^{\text{pzc}}$: the potential between the bulk phases corresponding to zero charge accumulation at the interface. As a result, $\phi_{\text{D}} = 0$ corresponds to $\sigma' = 0$ in Fig. 6. The corresponding potential of zero charge is experimentally determined and in our approach we will use the charge on the left electrode σ as the tuning variable. We identify the interfacial tension γ^{int} at zero Donnan potential as the bare oil–water tension. Fig. 6 illustrates that the gathering of ions of opposite charge at either side of the interface decreases the interfacial tension. Moreover, qualitative agreement is found between experimental data and the Poisson–Boltzmann result in eqn (21) for small values of the potential difference ϕ_{D} between the bulk phases.

5 Conclusion

We have applied nonlinear Poisson–Boltzmann theory to a liquid–liquid interface within a closed system bounded by two electrodes with an adjustable electric potential. We have considered the solution of four ion species with different solvation free energies (self energies) and calculated the equilibrium distribution of the salts. It was found that both the solvation energies and the separation between the electrodes have a crucial effect on the electric charge accumulation of the interfacial layer. For small self energies and a macroscopic electrode–electrode distance, the external potential leaves the interface unaffected, whereas complete control over the surface can be gained for the conjugate combination. We have defined a crossover length H^* , that marks the transition between these extremes as a function of the solvation energies. We observe that an exponential relation exists between the distance H^* and the self energies, provided that all self energies are significant, *i.e.* $|f_{z\pm}| \gg 1$. These observations are in line with our analytical approximation, which relates H^* to the various system parameters. An expression for the charge-induced surface tension at the liquid–liquid interface was derived, which we found to be in reasonably good agreement with experimental data obtained by Laanait *et al.*¹³

Appendix A: derivation of eqn (21)

We consider an open, non-electrified Coulombic system containing an organic and an inorganic salt, made of inorganic ions ($\alpha = 1$) and organic ions ($\alpha = 2$). If we assume two bulk phases and an interface at $z = 0$, the grand potential for this system may be written as

$$\begin{aligned} \Omega\{\{\rho_{z\pm}\}\}/k_B T &= \sum_{z\pm} A \int_{-H/2}^{H/2} dz \rho_{z\pm}(z) \\ &\times \left[\ln \left(\frac{\rho_{z\pm}(z)}{\rho_{z\pm}^w} \right) - 1 + \frac{V_{z\pm}(z)}{k_B T} \pm \frac{1}{2} \phi(z, \{\{\rho_{z\pm}\}\}) \right], \end{aligned} \quad (22)$$

where A denotes the surface area of the interface and V_α is defined as in eqn (5). We are primarily interested in the densities ρ_α , which are sensitive to the presence of electrodes. Functional differentiation of eqn (22) with respect to ρ_α yields the Boltzmann distributions eqn (6). The relative potential and bulk concentration in oil are respectively defined as:

$$\begin{aligned} \tilde{\phi}(z) &= \phi(z) - \phi_D; \\ \rho_{z\pm}^o &= \rho_{z\pm}^w \exp(\mp \phi_D - f_{z\pm}), \end{aligned} \quad (23)$$

where ϕ_D is the Donnan potential as given by eqn (8). We define the grand canonical potential for the interface as the contribution to expression (22) bounded by $-\frac{H}{4}$ and $\frac{H}{4}$. We distinguish between the water ($z < 0$) and oil ($z > 0$) phases, such that $\Omega/k_B T = \Omega_w/k_B T + \Omega_o/k_B T$. Substitution of eqn (6) and (23) into eqn (22) yields

$$\Omega_w/k_B T = A \int_{-H/4}^0 dz \left[\sum_{z\pm} \rho_{z\pm}^w \exp(\mp \phi(z)) \left(\mp \frac{\phi(z)}{2} - 1 \right) \right]; \quad (24)$$

$$\begin{aligned} \Omega_w/k_B T &= A \int_0^{H/4} dz \left[\sum_{z\pm} \rho_{z\pm}^w \exp(\mp \phi(z) - f_{z\pm}) \left(\mp \frac{\phi(z)}{2} - 1 \right) \right] \\ &= A \int_0^{H/4} dz \left[\sum_{z\pm} \rho_{z\pm}^o \exp(\mp \tilde{\phi}(z)) \left(\mp \frac{\phi(z) + \phi_D}{2} - 1 \right) \right]. \end{aligned} \quad (25)$$

Hence the Donnan potential makes a nontrivial contribution to the grand canonical potential (22) in the interfacial region. Whilst in the water phase we find

$$\Omega_w/k_B T = A \rho^w \int_{-H/4}^0 dz [\phi(z) \sinh(\phi(z)) - 2 \cosh(\phi(z))], \quad (26)$$

in the oil phase we obtain

$$\begin{aligned} \Omega_o/k_B T &= A \rho^o \int_0^{H/4} dz \left[\tilde{\phi}(z) \sinh(\tilde{\phi}(z)) - 2 \cosh(\tilde{\phi}(z)) \right] \\ &\quad - \frac{1}{2} A \int_0^{H/4} dz \left[\sum_z (\rho_{z+}(z) - \rho_{z-}(z)) \phi_D \right], \end{aligned} \quad (27)$$

where $2\rho^{o/w} = \rho_{1+}^{o/w} + \rho_{1-}^{o/w} + \rho_{2+}^{o/w} + \rho_{2-}^{o/w}$. Note that the integrand in eqn (26) reduces to -2 when the electrostatic potential reaches its vanishing bulk value. This also holds for the first integrand in eqn (27) when the electrostatic potential reaches the Donnan potential. By subtracting these bulk contributions we can identify the interfacial energy density,

$$\begin{aligned} \gamma^{\text{int}}/k_B T &= \rho^w \int_{-H/4}^0 dz [\phi(z) \sinh(\phi(z)) - 2 \cosh(\phi(z)) + 2] \\ &\quad + \rho^o \int_0^{H/4} dz [\tilde{\phi}(z) \sinh(\tilde{\phi}(z)) - 2 \cosh(\tilde{\phi}(z)) + 2] \\ &\quad + \frac{1}{2} \sigma' \phi_D, \end{aligned}$$

for which we have used that the charge density in the double layer on the oil side of the interface will exactly balance the charge

density of the interface, $\int_0^{H/4} dz \left[\sum_z (\rho_{z+}(z) - \rho_{z-}(z)) \right] = -\sigma'$.

Acknowledgements

This work is part of the D-ITP consortium, a programme of The Netherlands Organisation for Scientific Research (NWO), that is funded by the Dutch Ministry of Education, Culture and Science (OCW). We thank M. Schlossman for useful discussions and for providing his measurements of the interfacial tension.

References

- 1 M. Gouy, *J. Phys.*, 1910, **9**, 457.
- 2 D. L. Chapman, *Philos. Mag.*, 1913, **25**, 475.
- 3 J. Israelachvili, *Intermolecular and surface forces*, Academic Press, London, 2nd edn, 2006.

- 4 G. I. Guerrero-Garca, Y. Jinga and M. Olvera de la Cruz, Enhancing and reversing the electric field at the oil–water interface with size-asymmetric monovalent ions, *Soft Matter*, 2013, **9**, 6046–6052.
- 5 G. I. Guerrero-Garca and M. Olvera de la Cruz, Inversion of the Electric-Field at the Electrified Liquid-Liquid Interface, *J. Chem. Theory Comput.*, 2013, **9**(1), 1–7.
- 6 D. Michler, N. Shadidzadeh, M. Westbroek, R. van Roij and D. Bonn, Are Antagonistic Salts Surfactants?, *Langmuir*, 2015, **31**(3), 906–911.
- 7 D. Momotenko, C. M. Pereira and H. H. Girault, Differential capacitance of liquid/liquid interfaces of finite thickness: a finite element study, *Phys. Chem. Chem. Phys.*, 2012, **14**, 11268–11272.
- 8 H. Tamagawa, M. Sakurai, Y. Inoue, K. Ariga and T. Kunitake, Theoretical Study of Intermolecular Interaction at the Liquid-Water Interface, *J. Phys. Chem. B*, 1997, **101**(24), 4817–4825.
- 9 J. Zwanikken and R. van Roij, Destructed double layer and ionic charge separation near the oil-water interface, *Phys. Rev. Lett.*, 2007, **99**, 178301.
- 10 M. Bier, J. Zwanikken and R. van Roij, Liquid-Liquid Interfacial Tension of Electrolyte Solutions, *Phys. Rev. Lett.*, 2008, **101**, 046104.
- 11 M. E. Leunissen, J. Zwanikken, R. van Roij, P. M. Chaikin and A. van Blaaderen, Ion partitioning at the oil-water interface as a source of tunable electrostatic effects in emulsions with colloids, *Phys. Chem. Chem. Phys.*, 2007, **9**, 6405.
- 12 N. Laanait, *et al.*, Communications monovalent ion condensation at the electrified liquid-liquid interface, *J. Chem. Phys.*, 2010, **132**, 171101.
- 13 N. Laanait, *et al.*, Tuning ion correlations at an electrified soft interface, *Proc. Natl. Acad. Sci. U. S. A.*, 2012, **109**, 20326–20331.
- 14 N. Laanait, *et al.*, Tuning ion correlations at an electrified soft interface, supplementary information. retrieved from <http://www.pnas.org/content/early/2012/11/21>, 2012.
- 15 R. van Roij, *Physica A*, 2010, **389**, 4317.
- 16 Information provided by Mark L. Schlossman, private correspondence.