

# On the Issue of Reinstatement in Argumentation

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## Abstract

Dung’s theory of abstract argumentation frameworks [8] led to the formalization of various argument-based semantics, which are actually particular forms of dealing with the issue of reinstatement. In this paper, we re-examine the issue of semantics from the perspective of postulates. In particular, we ask ourselves the question of which (minimal) requirements have to be fulfilled by any principle for handling reinstatement, and how this relates to Dung’s standard semantics. Our purpose is to shed new light on the ongoing discussion on which semantics is most appropriate.

## 1 Introduction

Dung’s abstract theory of formal argumentation [8] has been a guide for researchers in the field of formal argumentation and nonmonotonic logic for more than ten years. During this period, a significant amount of work has been done on proof procedures for Dung’s various argument-based semantics [16, 4], as well as on concrete argumentation formalisms (such as [14, 9, 5] based on Dung’s theory).

One specific issue that has received relatively little attention is the nature of reinstatement. Although reinstatement as a principle is not totally uncontroversial [10], the current consensus among many researchers in formal argumentation and nonmonotonic logic is that reinstatement of arguments is an essential feature of defeasible reasoning (as is for instance expressed in [12]). Dung provides several approaches for dealing with reinstatement, like stable semantics, preferred semantics, complete semantics and grounded semantics. Our contribution is not to criticize Dung’s theory but rather to strengthen it. In particular, we ask ourselves the question: “Why do these semantics actually make sense?”

In previous work, we have stated a number of postulates which, in our view, every argumentation formalism should satisfy [3]. In the current paper, we will follow the same approach and state some simple and intuitive properties for dealing with the issue of reinstatement (section 3). We then show how these properties are satisfied by Dung’s standard semantics and how the differences between the various semantics could be viewed (section 4). We also show that a careful examination of reinstatement postulates reveals a semantics not currently known (section 4.8). Based on this discussion, we then share some thoughts on which type of semantics is most appropriate (section 5).

## 2 Dung’s Standard Semantics

A central notion in Dung’s theory of abstract argumentation [8] is that of an argumentation framework, which is defined as follows.

**definition 1 (argumentation framework).** *An argumentation framework is a pair  $(Args, def)$  where  $Args$  is a set of arguments and  $def \subseteq Args \times Args$ .*

We say that argument  $A$  *defeats* argument  $B$  iff  $A$  *def*  $B$ . The shorthand notation  $A^+$  and  $A^-$  stands for, respectively, the set of arguments defeated by  $A$  and the set of arguments that defeat  $A$ .

**definition 2 (defense / conflict-free).** Let  $A \in \text{Args}$  and  $\mathcal{A} \subseteq \text{Args}$ .

- We define  $A^+$  as  $\{B \mid A \text{ def } B\}$  and  $\mathcal{A}^+$  as  $\{B \mid A \text{ def } B \text{ for some } A \in \mathcal{A}\}$ .
- We define  $A^-$  as  $\{B \mid B \text{ def } A\}$  and  $\mathcal{A}^-$  as  $\{B \mid B \text{ def } A \text{ for some } A \in \mathcal{A}\}$ .
- $\mathcal{A}$  defends an argument  $A$  iff  $A^- \subseteq \mathcal{A}^+$ .
- $\mathcal{A}$  is conflict-free iff  $\mathcal{A} \cap \mathcal{A}^+ = \emptyset$ .

In the following definition,  $F(\mathcal{A})$  stands for the set of arguments that are acceptable (in the sense of [8]) with respect to  $\mathcal{A}$ .

**definition 3 (acceptability semantics).** Let  $\mathcal{A}$  be a conflict-free set of arguments and let  $F : 2^{\mathcal{A}} \rightarrow 2^{\mathcal{A}}$  be a function such that  $F(\mathcal{A}) = \{A \mid A \text{ is defended by } \mathcal{A}\}$ .

- $\mathcal{A}$  is admissible iff  $\mathcal{A} \subseteq F(\mathcal{A})$ .
- $\mathcal{A}$  is a complete extension iff  $\mathcal{A} = F(\mathcal{A})$ .
- $\mathcal{A}$  is a grounded extension iff  $\mathcal{A}$  is the minimal (w.r.t. set-inclusion) complete extension.
- $\mathcal{A}$  is a preferred extension iff  $\mathcal{A}$  is a maximal (w.r.t. set-inclusion) complete extension.
- $\mathcal{A}$  is a stable extension iff  $\mathcal{A}$  is a preferred extension that defeats every argument in  $\text{Args} \setminus \mathcal{A}$ .

Note that there is only one grounded extension. It contains all the arguments which are not defeated, as well as that arguments which are directly or indirectly defended by non-defeated arguments.

### 3 Reinstatement Labellings

The issue of quality postulates, or axioms, has recently received some attention in the field of formal argumentation and non-monotonic logic [3, 2]. An interesting question is whether one can also quality postulates for dealing with the reinstatement of arguments. Although the reinstatement has to a great extent been studied by Dung [8], the issue of which postulates have to be satisfied in order for a specific criterion for reinstatement to make sense has received relatively little attention.

One possible approach would be to start labelling the arguments in an argumentation framework. We distinguish three labels: “in”, “out” and ”undec” (undecided).

**definition 4.** Let  $(\text{Args}, \text{def})$  be a Dung-style argumentation framework. An AF-labelling is a (total) function  $\mathcal{L} : \text{Args} \rightarrow \{\text{in}, \text{out}, \text{undec}\}$ . We define  $\text{in}(\mathcal{L})$  as  $\{A \in \text{Args} \mid \mathcal{L}(A) = \text{in}\}$ ,  $\text{out}(\mathcal{L})$  as  $\{A \in \text{Args} \mid \mathcal{L}(A) = \text{out}\}$  and  $\text{undec}(\mathcal{L})$  as  $\{A \in \text{Args} \mid \mathcal{L}(A) = \text{undec}\}$ .

In a *reinstatement labelling*, an argument is “in” iff all its defeaters are “out” and an argument is “out” if it has a defeater that is “in”, as is stated in the following definition.

**definition 5.** Let  $\mathcal{L}$  be an AF-labelling. We say that  $\mathcal{L}$  is a reinstatement labelling iff it satisfies the following:

- $\forall A \in \text{Args} : (\mathcal{L}(A) = \text{out}) \equiv \exists B \in \text{Args} : (B \text{ def } A \wedge \mathcal{L}(B) = \text{in})$  and
- $\forall A \in \text{Args} : (\mathcal{L}(A) = \text{in}) \equiv \forall B \in \text{Args} : (B \text{ def } A \supset \mathcal{L}(B) = \text{out})$ .

The above definitions can be illustrated using the argumentation frameworks in figure 1. In the leftmost argumentation framework, there exists just one reinstatement labelling ( $\mathcal{L}_1$ ) with  $\mathcal{L}_1(A) = \text{in}$ ,  $\mathcal{L}_1(B) = \text{out}$ ,  $\mathcal{L}_1(C) = \text{in}$ . In the middle argumentation framework, there exist three reinstatement labellings ( $\mathcal{L}_2, \mathcal{L}_3, \mathcal{L}_4$ ) with  $\mathcal{L}_2(D) = \text{in}$ ,  $\mathcal{L}_2(E) = \text{out}$ ,  $\mathcal{L}_3(D) = \text{out}$ ,  $\mathcal{L}_3(E) = \text{in}$ ,  $\mathcal{L}_4(D) = \text{undec}$  and  $\mathcal{L}_4(E) = \text{undec}$ . In the rightmost argumentation framework, there exists just one reinstatement labelling ( $\mathcal{L}_5$ ) with  $\mathcal{L}_5(F) = \text{undec}$ .

Notice that definition 5 can actually be seen as a *postulate*, as it specifies a restriction on an AF-labelling. It turns out that different kinds of reinstatement labellings correspond with different kind of Dung-style semantics. This is explored in the remainder of this paper.

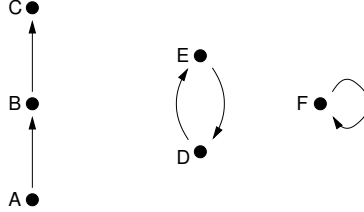


Figure 1: Three argumentation frameworks.

## 4 Labellings versus Semantics

We now define two functions that, given an argumentation framework, allow a set of arguments to be converted to a labelling and vice versa. The function  $\text{Ext2Lab}_{(Args, def)}$  takes a set of arguments (sometimes an extension) and converts it to a labelling. The function  $\text{Lab2Ext}_{(Args, def)}$  takes an AF-labelling and converts it to a set of arguments (sometimes an extension). Notice that as an AF-labelling is defined as a function (definition 4), which in its turn is essentially a relation, it is possible to represent the labelling as a set of pairs.

In the following definition, the resulting AF-labelling does not yet need to satisfy the properties of a reinstatement labelling as stated in definition 5.

**definition 6.** Let  $(Args, def)$  be an argumentation framework,  $\mathcal{A} \subseteq Args$  and  $\mathcal{L} : Args \longrightarrow \{\text{in}, \text{out}, \text{undec}\}$  a labelling function. We define  $\text{Ext2Lab}_{(Args, def)}(\mathcal{A}) = \{(A, \text{in}) \mid A \in \mathcal{A}\} \cup \{(A, \text{out}) \mid \exists A' \in \mathcal{A} : A' \text{ def } A\} \cup \{(A, \text{undec}) \mid A \notin \mathcal{A} \wedge \neg \exists A' \in \mathcal{A} : A' \text{ def } A\}$ . We define  $\text{Lab2Ext}_{(Args, def)}(\mathcal{L}) = \{A \mid (A, \text{in}) \in \mathcal{L}\}$ .

When the associated argumentation framework is clear, we sometimes simply write  $\text{Ext2Lab}$  and  $\text{Lab2Ext}$  instead of  $\text{Ext2Lab}_{(Args, def)}$  and  $\text{Lab2Ext}_{(Args, def)}$ .

### 4.1 Reinstatement labellings without restrictions

It is interesting to notice that a reinstatement labelling coincides with Dung's notion of a complete extension. This is stated by the theorems 1 and 2.

**theorem 1.** Let  $(Args, def)$  be an argumentation framework and let  $\mathcal{L}$  be a reinstatement labelling. Then  $\text{Lab2Ext}(\mathcal{L})$  is a complete extension.

*Proof.* Let  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$ . We now prove that  $\mathcal{A}$  is a complete extension, that is,  $F(\mathcal{A}) = \mathcal{A}$ . For this, we prove two things.

1.  $\mathcal{A} \subseteq F(\mathcal{A})$

Let  $A \in \mathcal{A}$ . Then  $\mathcal{L}(A) = \text{in}$ . The fact that  $\mathcal{L}$  is a reinstatement labelling means that each defeater  $B$  of  $A$  is labeled **out**. This again means (still by the fact that  $\mathcal{L}$  is a reinstatement labelling) that each such  $B$  has a defeater (say  $C$ ) that is labeled **in**. By definition of **Lab2Ext**, it holds that  $C \in \mathcal{A}$ . This means that for each defeater  $B$  of  $A$ , there is a  $C \in \mathcal{A}$  that defeats  $B$ . Therefore,  $A \in F(\mathcal{A})$  ( $A$  is defended by  $\mathcal{A}$ ).

2.  $F(\mathcal{A}) \subseteq \mathcal{A}$

Let  $A \in F(\mathcal{A})$ . Then each  $B$  that defeats  $A$  is defeated by some  $C \in \mathcal{A}$  means by definition of **Lab2Ext** that  $C$  is labeled **in** by  $\mathcal{L}$ . The fact that  $\mathcal{L}$  is a reinstatement labelling means that  $B$  is labeled **out**. This again means that  $A$  is labeled **in**. Therefore, by definition of **Lab2Ext**,  $A \in \mathcal{A}$ .

□

**theorem 2.** *Let  $(Args, def)$  be an argumentation framework and let  $\mathcal{A}$  be a complete extension. Then  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling.*

*Proof.* In order to prove that  $\text{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling, we have to prove four things:

1.  $\forall A \in Args : (\mathcal{L}(A) = \text{out} \supset \exists B \in Args : (B def A \wedge \mathcal{L}(B) = \text{in}))$

Let  $A \in Args$  such that  $\mathcal{L}(A) = \text{out}$ . Then, according to the definition of **Ext2Lab**, the fact that  $\mathcal{L}(A) = \text{out}$  means that there is an  $A' \in \mathcal{A}$  that defeats  $A$ . And the fact that  $A' \in \mathcal{A}$  means that  $\mathcal{L}(A') = \text{in}$ .

2.  $\forall A \in Args : (\mathcal{L}(A) = \text{out} \subset \exists B \in Args : (B def A \wedge \mathcal{L}(B) = \text{in}))$

Let  $A \in Args$  be such that it has a defeater  $B$  labeled **in**. The fact that  $\mathcal{L}(B) = \text{in}$  means that  $B \in \mathcal{A}$  (**Ext2Lab**). By definition of **Ext2Lab**,  $\mathcal{L}(A) = \text{out}$ .

3.  $\forall A \in Args : (\mathcal{L}(A) = \text{in} \supset \forall B \in Args (B def A \supset \mathcal{L}(B) = \text{out}))$

Let  $A$  be an argument that is labeled **in**. The fact that  $\mathcal{L}(A) = \text{in}$  means that  $A \in \mathcal{A}$ . The fact that  $\mathcal{A}$  is a complete extension implies that it is an admissible set. That is,  $\mathcal{A}$  defeats every defeater of  $A$ . By the definition of **Ext2Lab**, this means that every defeater of  $A$  is labeled **out**.

4.  $\forall A \in Args : (\mathcal{L}(A) = \text{in} \subset \forall B \in Args (B def A \supset \mathcal{L}(B) = \text{out}))$

Let  $A \in Args$  be such that every defeater of  $A$  is labeled **out**. This means, by definition of **Ext2Lab**, that for every defeater  $B$  of  $A$  there is a  $C \in \mathcal{A}$  that defeats  $B$ . But as  $\mathcal{A}$  is a complete extension (everything that is defended by  $\mathcal{A}$  is already in  $\mathcal{A}$ ) this means that  $A \in \mathcal{A}$ . By definition of **Ext2Lab**, this means that  $A$  is labeled **in**.

□

The correspondence between reinstatement labellings and complete extensions is an important one. Theorem 1 and 2 have a central position in this paper and will be used in many subsequent proofs, sometimes even without explicitly mentioning them.

## 4.2 Reinstatement labellings with empty undec

Reinstatement labellings where **undec** is empty coincide with stable extensions. This is stated by the theorems 3 and 4.

**theorem 3.** *Let  $(Args, def)$  be an argumentation framework and let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{undec}(\mathcal{L}) = \emptyset$ . Then  $\text{Lab2Ext}(\mathcal{L})$  is a stable extension.*

*Proof.* Let  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$ . Now consider an arbitrary  $A \in \text{Args} \setminus \mathcal{A}$ . From the fact that  $\text{undec}(\mathcal{L}) = \emptyset$ , it follows that  $\mathcal{L}(A) = \text{out}$ . By definition, this means that  $A$  is defeated by an argument (say  $B$ ) labelled  $\text{in}$ . The fact that  $B$  is labelled  $\text{in}$  means that  $B \in \mathcal{A}$ . Therefore,  $A$  is defeated by some argument in  $\mathcal{A}$ . As this holds for any arbitrary  $A \in \text{Args} \setminus \mathcal{A}$ , it means that  $\mathcal{A}$  defeats any argument not in it. Thus,  $\mathcal{A}$  is a stable extension.  $\square$

**theorem 4.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and let  $\mathcal{A}$  be a stable extension. Then  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$  is a labelling such that  $\text{undec}(\mathcal{L}) = \emptyset$ .*

*Proof.* Let  $A \in \text{Args}$ . We distinguish two possibilities:

1.  $A \in \mathcal{A}$ . Then, by definition,  $\mathcal{L}(A) = \text{in}$ .
2.  $A \notin \mathcal{A}$ . As  $\mathcal{A}$  is a stable extension, this means that some argument in  $\mathcal{A}$  defeats  $A$ . This means that  $\mathcal{L}(A) = \text{out}$ .

In both cases,  $\mathcal{L}(A) \neq \text{undec}$ . As this holds for any arbitrary  $A \in \text{Args}$ , it holds that  $\text{undec}(\mathcal{L}) = \emptyset$ .  $\square$

### 4.3 Reinstatement labellings with maximal in

Reinstatement labellings where  $\text{in}$  is maximal coincide with preferred extensions. This is stated by the theorems 5 and 6.

**theorem 5.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{in}(\mathcal{L})$  is maximal. Then  $\text{Lab2Ext}(\mathcal{L})$  is a preferred extension.*

*Proof.* Let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{in}(\mathcal{L})$  is maximal. Now, suppose that  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$  is not a preferred extension. Then, by definition of a preferred extension (Definition 3) there must be a complete extension  $\mathcal{A}'$  such that  $\mathcal{A} \subsetneq \mathcal{A}'$ . Let  $\mathcal{L}' = \text{Ext2Lab}(\mathcal{A}')$ . Then,  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ . But then  $\text{in}(\mathcal{L})$  would not be maximal. Contradiction.  $\square$

**theorem 6.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and let  $\mathcal{A}$  be a preferred extension. Then  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$  is a labelling such that  $\text{in}(\mathcal{L})$  is maximal.*

*Proof.* Let  $\mathcal{A}$  be a preferred extension and let  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$ . Now, suppose that  $\text{in}(\mathcal{L})$  is not maximal. Then there must be some reinstatement labelling  $\mathcal{L}'$  with  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ . Let  $\mathcal{A}' = \text{Lab2Ext}(\mathcal{L}')$ . Then  $\mathcal{A}'$  is a complete extension with  $\mathcal{A} \subsetneq \mathcal{A}'$ . But then  $\mathcal{A}$  would not be a preferred extension. Contradiction.  $\square$

### 4.4 Reinstatement labellings with maximal out

It is interesting to notice that, contrary to what one might expect, reinstatement labellings in which  $\text{out}$  is maximized coincide with preferred extensions, just like (as was proved in section 4.3) labellings in which  $\text{in}$  is maximized.

We start our proofs with two lemmas.

**lemma 1.** *Let  $\mathcal{L}$  and  $\mathcal{L}'$  be two reinstatement labellings. If  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$  then  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$ .*

*Proof.* Suppose  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ . This means two things:

1.  $\forall A \in \text{in}(\mathcal{L}) : A \in \text{in}(\mathcal{L}')$
2.  $\exists B \in \text{in}(\mathcal{L}') : B \notin \text{in}(\mathcal{L})$

We now prove the following two things:

- $\forall C \in \text{out}(\mathcal{L}) : C \in \text{out}(\mathcal{L}')$ .  
Let  $C \in \text{out}(\mathcal{L})$ . By the definition of a reinstatement labelling (Definition 5) this means that  $C$  is defeated by some  $A \in \text{in}(\mathcal{L})$ . But then, according to 1, it also holds that  $A \in \text{in}(\mathcal{L}')$ . This, by the definition of a reinstatement labelling, means that  $C \in \text{out}(\mathcal{L}')$ .
- $\exists D \in \text{out}(\mathcal{L}') : D \notin \text{out}(\mathcal{L})$ .  
Let  $B$  be an argument (taken from 2) such that  $B \in \text{in}(\mathcal{L}')$ . Then, according to the definition of a reinstatement labelling, it must also be the case that each defeater of  $B$  is labelled *out* in  $\mathcal{L}'$ , but there is some defeater of  $B$  that is not labelled *out* in  $\mathcal{L}$ . This means that  $\exists D \in \text{out}(\mathcal{L}') : D \notin \text{out}(\mathcal{L})$

□

**lemma 2.** *Let  $\mathcal{L}$  and  $\mathcal{L}'$  be two reinstatement labellings. If  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$  then  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ .*

*Proof.* Suppose  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$ . This means two things:

1.  $\forall A \in \text{out}(\mathcal{L}) : A \in \text{out}(\mathcal{L}')$
2.  $\exists B \in \text{out}(\mathcal{L}') : B \notin \text{out}(\mathcal{L})$

We now prove the following two things:

- $\forall C \in \text{in}(\mathcal{L}) : C \in \text{in}(\mathcal{L}')$   
Let  $C \in \text{in}(\mathcal{L})$ . By the definition of a reinstatement labelling (Definition 5) this means that every defeater of  $C$  is labelled *out* in  $\mathcal{L}$ . But then (according to 1) every defeater of  $C$  is also labelled *out* in  $\mathcal{L}'$ . This, by the definition of a reinstatement labelling, means that  $C$  is labelled *in* in  $\mathcal{L}'$ .
- $\exists D \in \text{in}(\mathcal{L}') : D \notin \text{in}(\mathcal{L})$   
Let  $B$  be an argument (taken from 2) such that  $B \in \text{out}(\mathcal{L}')$  and  $B \notin \text{out}(\mathcal{L})$ . Then, according to the definition of a reinstatement labelling, this means that some defeater of  $B$  is labelled *in* in  $\mathcal{L}'$ , but no defeater of  $B$  is labelled *in* in  $\mathcal{L}$ . This means that  $\exists D \in \text{in}(\mathcal{L}') : D \notin \text{in}(\mathcal{L})$ .

□

Using these two lemmas, we can now state and prove the main theorems.

**theorem 7.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{out}(\mathcal{L})$  is maximal. Then  $\text{Lab2Ext}(\mathcal{L})$  is a preferred extension.*

*Proof.* Let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{out}(\mathcal{L})$  is maximal. Now, suppose that  $\text{Lab2Ext}(\mathcal{L})$  is not a preferred extension. Then, by theorem 5,  $\text{in}(\mathcal{L})$  is not maximal. This means that there exists some  $\mathcal{L}'$  such that  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ . By lemma 1 this also means that  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$ . But then  $\text{out}(\mathcal{L})$  would not be maximal. Contradiction. □

**theorem 8.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and let  $\mathcal{A}$  be a preferred extension. Then  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$  is a labelling such that  $\text{out}(\mathcal{L})$  is maximal.*

*Proof.* Let  $\mathcal{A}$  be a preferred extension. Then, by theorem 6,  $\text{Ext2Lab}(\mathcal{A})$  is a labelling ( $\mathcal{L}$ ) such that  $\text{in}(\mathcal{L})$  is maximal. Now suppose that  $\text{out}(\mathcal{L})$  is not maximal. Then there exists some reinstatement labelling  $\mathcal{L}'$  with  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$  By lemma 2, this also means that  $\text{in}(\mathcal{L}) \subseteq \text{in}(\mathcal{L}')$ . But then  $\text{in}(\mathcal{L})$  would not be maximal. Contradiction. □

## 4.5 Reinstatement labellings with maximal undec

A reinstatement labelling where **undec** is maximal coincides with the grounded extension. This is stated by the theorems 9 and 10.

**theorem 9.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{L}$  be a reinstatement labelling such that  $\mathbf{undec}(\mathcal{L})$  is maximal. Then  $\mathbf{Lab2Ext}(\mathcal{L})$  is the grounded extension.*

*Proof.* (by contraposition) Suppose  $\mathbf{Lab2Ext}(\mathcal{L})$  is *not* the grounded extension ( $GE$ ). Then it must be a strict superset of the grounded extension (which, by definition, is the smallest complete extension). That is:  $GE \subsetneq \mathbf{Lab2Ext}(\mathcal{L})$ . Let  $\mathcal{L}' = \mathbf{Ext2Lab}(GE)$ . From  $GE \subsetneq \mathbf{Lab2Ext}(\mathcal{L})$  it follows directly that  $\mathbf{in}(\mathcal{L}') \subsetneq \mathbf{in}(\mathcal{L})$ . From lemma 1 it follows that  $\mathbf{out}(\mathcal{L}') \subsetneq \mathbf{out}(\mathcal{L})$ . Therefore, it holds that  $\mathbf{undec}(\mathcal{L}) \subsetneq \mathbf{undec}(\mathcal{L}')$ . But then  $\mathbf{undec}(\mathcal{L})$  would not be maximal.  $\square$

**theorem 10.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{A}$  be the grounded extension in this framework. Then  $\mathbf{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling where  $\mathbf{undec}(\mathcal{L})$  is maximal.*

*Proof.* Let  $\mathcal{A}' (\neq \mathcal{A})$  be an arbitrary complete extension. As the grounded extension is the smallest complete extension, it follows that  $\mathcal{A} \subsetneq \mathcal{A}'$ . Let  $\mathcal{L} = \mathbf{Ext2Lab}(\mathcal{A})$  and  $\mathcal{L}' = \mathbf{Ext2Lab}(\mathcal{A}')$ . From  $\mathcal{A} \subsetneq \mathcal{A}'$  it directly follows that  $\mathbf{in}(\mathcal{L}) \subsetneq \mathbf{in}(\mathcal{L}')$ . This also means (by lemma 1) that  $\mathbf{out}(\mathcal{L}) \subsetneq \mathbf{out}(\mathcal{L}')$ . Therefore, it holds that  $\mathbf{undec}(\mathcal{L}') \subsetneq \mathbf{undec}(\mathcal{L})$ . As this result holds for arbitrary  $\mathcal{A}' (\neq \mathcal{A})$  (and therefore also for arbitrary  $\mathcal{L}' (\neq \mathcal{L})$ ), it holds that  $\mathbf{undec}(\mathcal{L})$  is maximal.  $\square$

## 4.6 Reinstatement labellings with minimal in

A reinstatement labelling with minimal **in** coincides with the grounded extension. This is stated by the theorems 11 and 12.

**theorem 11.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{L}$  be a reinstatement labelling such that  $\mathbf{in}(\mathcal{L})$  is minimal. Then  $\mathbf{Lab2Ext}(\mathcal{L})$  is the grounded extension.*

*Proof.* Let  $\mathcal{L}$  be a reinstatement labelling such that  $\mathbf{in}(\mathcal{L})$  is minimal. Now, suppose  $\mathcal{A} = \mathbf{Lab2Ext}(\mathcal{L})$  is *not* the grounded extension. Then, according to the definition of the grounded extension (Definition 3) there must be some complete extension  $\mathcal{A}'$  with  $\mathcal{A}'$  with  $\mathcal{A}' \subsetneq \mathcal{A}$ . Let  $\mathcal{L}' = \mathbf{Ext2Lab}(\mathcal{A}')$ . Then  $\mathbf{in}(\mathcal{L}') \subsetneq \mathbf{in}(\mathcal{L})$ . But then  $\mathbf{in}(\mathcal{L})$  would not be minimal. Contradiction.  $\square$

**theorem 12.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{A}$  be the grounded extension in this framework. Then  $\mathbf{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling where  $\mathbf{in}(\mathcal{L})$  is minimal.*

*Proof.* Let  $\mathcal{A}$  be the grounded extension. Let  $\mathcal{L} = \mathbf{Ext2Lab}(\mathcal{A})$ . Now, suppose  $\mathbf{in}(\mathcal{L})$  is not minimal. Then there exists some  $\mathcal{L}'$  with  $\mathbf{in}(\mathcal{L}') \subsetneq \mathbf{in}(\mathcal{L})$ . Now, let  $\mathcal{A}' = \mathbf{Lab2Ext}(\mathcal{L}')$ . It now holds that  $\mathcal{A}' \subsetneq \mathcal{A}$ . But then  $\mathcal{A}$  would not be a grounded extension. Contradiction.  $\square$

## 4.7 Reinstatement labellings with minimal out

A reinstatement labelling with minimal **out** coincides with the grounded extension. This is stated by the theorems 13 and 14.

**theorem 13.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{L}$  be a reinstatement labelling such that  $\mathbf{out}(\mathcal{L})$  is minimal. Then  $\mathbf{Lab2Ext}(\mathcal{L})$  is the grounded extension.*

*Proof.* Let  $\mathcal{L}$  be a reinstatement labelling such that  $\text{out}(\mathcal{L})$  is minimal. Then, according to lemma 1  $\text{in}(\mathcal{L})$  is also minimal. Then, by theorem 11,  $\text{Lab2Ext}(\mathcal{L})$  is the grounded extension.  $\square$

**theorem 14.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and  $\mathcal{A}$  be the grounded extension in this framework. Then  $\text{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling where  $\text{out}(\mathcal{L})$  is minimal.*

*Proof.* Let  $\mathcal{A}$  be the grounded extension. Let  $\mathcal{L} = \text{Ext2Lab}(\mathcal{L})$ . Then, by theorem 12,  $\text{in}(\mathcal{L})$  is minimal. Then, by lemma 2,  $\text{out}(\mathcal{L})$  is also minimal.  $\square$

## 4.8 Reinstatement labellings with minimal undec

The last remaining case to be examined is that of reinstatement labellings where **undec** is minimized. We show that this does not coincide with any currently known semantics.

There is a one-way relation between reinstatement labellings with minimal **undec** and preferred extensions, as is stated in the following theorem.

**theorem 15.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and  $\mathcal{L}$  be a reinstatement labelling such that  $\text{undec}(\mathcal{L})$  is minimal. Then  $\text{Lab2Ext}(\mathcal{L})$  is a preferred extension.*

*Proof. (reductio ad absurdum)* Suppose  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$  is not a preferred extension. Then there exists an admissible set  $\mathcal{A}'$  that is a strict superset of  $\mathcal{A}$  ( $\mathcal{A} \subsetneq \mathcal{A}'$ ). Now consider  $\text{Ext2Lab}(\mathcal{A}') = \mathcal{L}'$ . Obviously, it holds that  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$ . This also implies (lemma 1) that  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$ . From the facts that  $\text{in}(\mathcal{L}) \subsetneq \text{in}(\mathcal{L}')$  and  $\text{out}(\mathcal{L}) \subsetneq \text{out}(\mathcal{L}')$ , it follows that  $\text{undec}(\mathcal{L}') \subsetneq \text{undec}(\mathcal{L})$ . But then  $\text{undec}(\mathcal{L})$  is not minimal. Contradiction.  $\square$

Unfortunately, it doesn't work the other way around. If  $\mathcal{A}$  is a preferred extension, then it is not necessarily the case that  $\text{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling where  $\text{undec}(\mathcal{L})$  is minimal. This is shown in the following example.

**example 1.** *Let  $\text{Args} = \{A, B, C, D, E\}$  and let  $A$  defeat  $B$ ,  $B$  defeat  $A$ ,  $B$  defeat  $C$ ,  $C$  defeat  $D$ ,  $D$  defeat  $E$ , and  $E$  defeat  $C$  (see also figure 2). Here, there exists two preferred extensions:  $\mathcal{E}_1 = \{B, D\}$  and  $\mathcal{E}_2 = \{A\}$ . As  $\mathcal{E}_1$  is also a stable extension, it holds that  $\text{Ext2Lab}(\mathcal{E}_1)$  yields a labelling (say  $\mathcal{L}$ ) with  $\text{undec}(\mathcal{L}) = \emptyset$ . However,  $\text{Ext2Lab}(\mathcal{E}_2)$  yields a labelling (say  $\mathcal{L}'$ ) with  $\text{undec}(\mathcal{L}') = \{C, D, E\}$ . So, even though  $\mathcal{E}_2$  is a preferred extension,  $\text{Ext2Lab}(\mathcal{E}_2)$  is not a reinstatement labelling in which **undec** is minimal.*

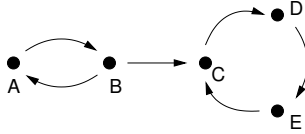


Figure 2: A preferred extension does not necessarily imply minimal **undec**.

Before continuing with our analysis, we first state two helpful lemmas.

**lemma 3.** *Let  $(\text{Args}, \text{def})$  be an argumentation framework and  $\mathcal{A}$  be a complete extension. Let  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$ . Then:*

1.  $\text{in}(\mathcal{L}) = \mathcal{A}$
2.  $\text{out}(\mathcal{L}) = \mathcal{A}^+$
3.  $\text{undec}(\mathcal{L}) = \text{Args} \setminus (\mathcal{A} \cup \mathcal{A}^+)$



*Proof.* This follows directly from the definition of **Ext2Lab** (Definition 6). □

**lemma 4.** *Let  $(Args, def)$  be an argumentation framework and let  $\mathcal{L}$  be a reinstatement labelling. Let  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$ . Then:*

1.  $\mathcal{A} = \text{in}(\mathcal{L})$
2.  $\mathcal{A}^+ = \text{out}(\mathcal{L})$
3.  $Args \setminus (\mathcal{A} \cup \mathcal{A}^+) = \text{undec}(\mathcal{L})$

*Proof.*

1. This follows directly from the definition of **Lab2Ext** (Definition 6).
2. This follows from 1 and the definition of a reinstatement labelling (Definition 5).
3. This follows from 1 and 2, together with the fact that a reinstatement labelling is a total function (it assigns exactly one label from  $\{\text{in}, \text{out}, \text{undec}\}$  to each argument). □

Labellings in which **undec** is minimized can be seen as produced by an agent that is eager to take a position (**in** or **out**) on as many arguments as possible. It is not too difficult to specify what such an “eager semantics” would look like as a Dung-style semantics.

**definition 7.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{A} \subseteq Args$ .  $\mathcal{A}$  is called an eager extension iff  $\mathcal{A}$  is a complete extension where  $\mathcal{A} \cup \mathcal{A}^+$  is maximal.*

The following two theorems state that eager semantics indeed coincides with reinstatement labellings in which **undec** is minimal.

**theorem 16.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{L}$  be a reinstatement labelling such that  $\text{undec}(\mathcal{L})$  is minimal. Then  $\mathcal{A} = \text{Lab2Ext}(\mathcal{L})$  is an eager extension.*

*Proof.* This follows directly from Lemma 4 and Definition 7. □

**theorem 17.** *Let  $(Args, def)$  be an argumentation framework and  $\mathcal{A}$  be an eager extension. Then  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$  is a reinstatement labelling such that  $\text{undec}(\mathcal{L})$  is minimal.*

*Proof.* This follows directly from Lemma 3 and Definition 7. □

An interesting property of eager extensions is the following.

**theorem 18.** *Let  $(Args, def)$  be an argumentation framework. If there exists a stable extension, then the eager extensions coincide with the stable extensions.*

*Proof.* Suppose there exists a stable extension  $\mathcal{A}$ . Let  $\mathcal{L} = \text{Ext2Lab}(\mathcal{A})$ . From Theorem 4 it follows that  $\text{undec}(\mathcal{L}) = \emptyset$ . As an eager extension minimizes **undec** (Theorem 17), the fact that  $\mathcal{A}$  has empty **undec** means that in the particular argumentation framework  $(Args, def)$  every eager extension should have empty **undec**. This means that in  $(Args, def)$  every eager extension is a stable extension. The fact that every stable extension is an eager extension follows from the fact that the empty set is the minimal element w.r.t. set-inclusion. □

restriction reinst. labellings	Dung-style semantics	linked by theorems
no restrictions	complete semantics	theorems 1 and 2
empty <b>undec</b>	stable semantics	theorems 3 and 4
maximal <b>in</b>	preferred semantics	theorems 5 and 6
maximal <b>out</b>	preferred semantics	theorems 7 and 8
maximal <b>undec</b>	grounded semantics	theorems 9 and 10
minimal <b>in</b>	grounded semantics	theorems 11 and 12
minimal <b>out</b>	grounded semantics	theorems 13 and 14
minimal <b>undec</b>	eager semantics	theorems 16 and 17

Table 1: Reinstatement labellings versus Dung-style semantics.

## 4.9 Overview

From the previous discussion, it is clear that there exists a connection between the various forms of reinstatement labellings on one hand and the various Dung-style semantics on the other hand. This connection is summarized in table 1.

There also exists a partial ordering between the various Dung-style semantics. Every stable extension is an eager extension, every eager extension is a preferred extension, every preferred extension is a complete extension, and every grounded extension is a complete extension. This is graphically depicted in figure 3.

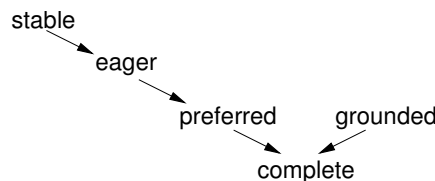


Figure 3: An overview of the different semantics.

## 5 Semantics Revisited

In essence, a reinstatement labelling can be seen as a subjective but reasonable point of view that an agent can take with respect to which arguments are **in**, **out** or **undec**. Each such position is internally coherent in the sense that, if questioned, the agent can use its own position to defend itself. It is possible for the position to be disagreed with, but at least one cannot point out an internal inconsistency. The set of all reinstatement labellings therefore stands for all possible and reasonable positions an agent can take.

When determining the overall justified arguments, two approaches are possible: the sceptical and the credulous one. Under the credulous approach, an argument is justified iff there is at least one reasonable position (= reinstatement labelling) where it is labelled **in**. Under the sceptical approach, an argument is justified iff it is **in** in every reasonable position; that is, a reasonable agent cannot deny that the argument is **in**. As reinstatement labellings coincide with complete extensions (as was explained in section 4.1), it would seem that credulous and sceptical inference could be modelled by applying complete semantics.

It is interesting to compare complete semantics with some current approaches. Let us consider the example of figure 4

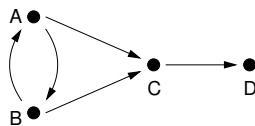


Figure 4: A floating argument.

In the case of the argumentation framework of Figure 4 there are three reinstatement labellings, as stated in Figure 5.

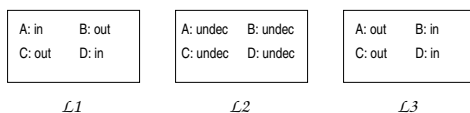


Figure 5: Three reinstatement labellings.

When all reinstatement labellings are taken into account (such is the case in complete semantics) then  $A$ ,  $B$  and  $D$  are credulously justified, whereas no arguments are sceptically justified.

It is interesting to compare this approach with preferred semantics, which has been the subject of much recent research [16, 7, 6]. As was explained in section 4.3, a preferred extension coincides with a reinstatement labelling in which the set of arguments labelled **in** is maximal. In case of figure 4, for instance, the relevant labellings are only  $\mathcal{L}_1$  and  $\mathcal{L}_3$ ; thus,  $\mathcal{L}_2$  is ruled out (see figure 6).

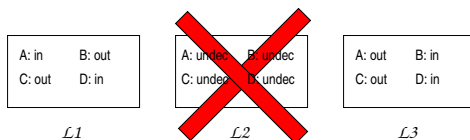


Figure 6: Preferred semantics rules out particular labellings.

What preferred semantics essentially does is to rule out zero or more reinstatement labellings before determining which arguments are credulously or sceptically justified. Under the sceptical approach, this can lead to more conclusions becoming justified. In the case of figure 4, for instance, argument  $D$  is sceptically justified under preferred semantics but not under complete semantics.

The fact that under preferred semantics, reinstatement labelling  $\mathcal{L}_2$  is ruled out can be seen as odd.  $\mathcal{L}_2$ , after all, is a perfectly valid reinstatement labelling. The fact that it is ruled out under preferred semantics means that those who defend preferred semantics must have some reason to justify this. This reason should state why  $\mathcal{L}_2$  is “wrong” or “irrelevant”, thus making it possible to ignore  $\mathcal{L}_2$ . One such reason could be (theorems 5 and 6) “ $\mathcal{L}_2$  should be ignored because the set of **in**-labelled arguments is not maximal.” This reason does not appear to be a very strong one.

A more pragmatic reason in favor of preferred semantics is the issue of floating conclusions and floating arguments. Suppose the following information is available: (1) Lars’s mother is Norwegian, (2) Lars’s father is Dutch, (3) Norwegians like ice-skating and (4)

Dutch like ice-skating. We can now construct two arguments that defeat each other: (A) Lars likes ice-skating because he's Norwegian and (B) Lars likes ice-skating because he's Dutch. Under sceptical complete semantics, the proposition that Lars likes ice-skating is not justified, despite the fact that, intuitively, it should be. Under sceptical preferred semantics, on the other hand, the proposition that Lars likes ice-skating *is* justified. At a first sight, this seems to illustrate a clear advantage of preferred semantics above complete semantics.

If we take a closer look, however, the situation becomes more complex. This is because the issue of whether or not Lars likes ice-skating depends on whether or not the principle of the excluded middle is regarded as valid. In monotonic logic, the validity of a statement  $p \vee \neg p$  depends on the number of truth-values. Whereas in a two-valued logic (where each proposition is either **true** or **false** in a given model) the proposition  $p \vee \neg p$  is usually regarded as valid, it is *not* regarded as valid in, for instance, three-valued logics. Similarly, for one of the two conflicting arguments  $A$  and  $B$  to be regarded as valid (or *justified*), one should require that an argument is either **in** or **out**, resulting in a two-valued reinstatement labelling (without **undec**). In section 4.2, it was shown that this essentially boils down on stable semantics. Stable semantics, however, suffers from the problem that for some argumentation frameworks, no stable extensions exist. Consequently, it is not always possible to have a reinstatement labelling with only **in** and **out**. A third possibility (**undec**) is needed. Therefore, the principle of the excluded middle, as an absolute criterion, should be rejected.<sup>1</sup> For those who nevertheless feel that the principle of the excluded middle should perhaps not hold at all times, but at least as much as possible (thus not completely ruling out **undec** but merely *minimizing* it), eager semantics would seem a more appropriate choice than preferred semantics.

Given the observation that the principle of complete semantics can be given a decent philosophical justification, it is interesting to examine how complete semantics could be implemented. Fortunately, it turns out that both sceptical and credulous complete semantics have relatively easy and well-documented proof procedures.

As for sceptical semantics, an argument is in each complete extension iff it is in the grounded extension.

**theorem 19.** *Let  $CE_1, \dots, CE_n$  be the set of complete extensions and  $GE$  be the grounded extension. Let  $A$  be an argument. It holds that  $A \in GE$  iff  $A \in CE_1 \cap \dots \cap CE_n$ .*

*Proof.* See [8]. □

As for credulous semantics, an argument is in some complete extension iff it is in some admissible set.

**theorem 20.** *Let  $CE_1, \dots, CE_n$  be the set of complete extensions and  $AS_1, \dots, AS_m$  be the set of admissible sets. Let  $A$  be an argument. It holds that  $\exists CE_i \in \{CE_1, \dots, CE_n\} : A \in CE_i$  iff  $\exists AS_j \in \{AS_1, \dots, AS_m\} : A \in AS_j$ .*

*Proof.*

“ $\rightarrow$ ”:

Suppose  $A$  is in some complete extension  $CE_i$ . As  $F(CE_i) = CE_i$ , it holds that  $A$  is admissible. Therefore,  $A$  is in some admissible set.

“ $\leftarrow$ ”:

Suppose  $A$  is in some admissible set  $AS_j$ . Then there also exists a maximal admissible set  $\mathcal{A}'$  such that  $AS_j \subseteq \mathcal{A}'$ . By definition, this maximally admissible set is a preferred

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<sup>1</sup>Another issue where the principle of the excluded middle does not hold in most formalisms for defeasible reasoning is in handling disjunctive information. If  $\{p \vee q\} \subseteq \mathcal{P}$  and  $\{p \Rightarrow r; q \Rightarrow r\} \subseteq \mathcal{D}$  then in most formalisms for defeasible reasoning,  $r$  is not justified, although intuitively it should be, if one accepts the principle of the excluded middle.

extension. Furthermore, every preferred extension is also a complete extension [8]. This means that  $A$  is also in some complete extension.  $\square$

The fact that sceptical complete semantics coincides with grounded semantics, and credulous complete semantics coincides with credulous preferred semantics is advantageous, as these have relatively straightforward and well-studied proof procedures. Proof procedures for grounded semantics are given in [14, 1], and proof procedures for credulous preferred semantics are given in [16, 4].

## 6 Summary and Conclusions

In this paper, we showed it is possible to describe Dung’s standard semantics in terms of reinstatement labellings, which provide an intuitive and relatively simple way of dealing with the issue of reinstatement. We also showed how reinstatement labellings can be used to pinpoint the exact differences between Dung’s standard semantics. Using a systematic analysis of reinstatement labellings, we were also able to specify an additional form of semantics (eager semantics) and showed how this semantics fits into the overall picture (Figure 3). We then reexamined the various semantical approaches and made a case for grounded semantics for sceptical entailment and credulous preferred semantics for credulous entailment.

One of the researchers who has done some work on the relation between reinstatement labellings (“status assignments”) and Dung’s various semantics is Prakken. In particular, Prakken proofs (in his own terms and particular formalization) that reinstatement labellings without **undec** correspond to stable extensions, and that reinstatement labellings with maximal **in** correspond to preferred extensions. [13]. It was the work of prakken that served as an inspiration for the more thorough analysis in this paper.

Other recent work on reinstatement labellings has been done by Jakobovits and Vermeir [11]. Their definition of a labelling, however, is different than ours. First of all, they allow for an argument to be labelled **in**, **out**, both **in** and **out**, or neither **in** or **out**. Furthermore, their main reinstatement postulate is different.

**definition 8** ([11], **syntax and formulation adjusted**).  $\mathcal{L}$  is a labelling iff:

- $\forall A \in \text{Args} : (\mathcal{L}(A) = \text{out} \equiv \exists B \in \text{Args} : (B \text{def } A \wedge \mathcal{L}(B) = \text{in}))$  and
- $\forall A \in \text{Args} : (\mathcal{L}(A) = \text{in} \supset \forall B \in \text{Args} : (B \text{def } A \supset \mathcal{L}(B) = \text{out}))$ .

The difference between Definition 8 and the earlier presented Definition 5 is that the former does not require an argument of which all defeaters are **out** to be labelled **in**. This is quite strange, since it also means that an argument that has no defeaters at all is not required to be labelled **in**. To some extent, this problem is repaired for *complete labellings*, in which each argument is labelled either **in**, **out** or both.

The overall aim of Jakobovits and Vermeir is to come up with a semantics that is different from Dung’s. Jakobovits and Vermeir justify their approach by discussing a number of small examples. However, the general approach of using examples in order to justify a particular formalism has some important downsides. To illustrate our main point, consider the following example provided in [11].

**example 2.**

*A: If the bacteria in the patient’s blood is not of type X then it must be of type Y.*

*B: If the bacteria in the patient’s blood is not of type Y then it must be of type X.*

*C: If the patient does not have bacterial infection then giving antibiotics to the patient is superfluous.*

*D: If it is not superfluous to give the patient antibiotics then the antibiotics should be prescribed.*

Example 2 is represented in the argumentation framework of Figure 7.

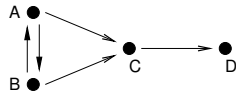


Figure 7: The argumentation framework of Example 2 and 3.

Jakobovits and Vermeir argue that the correct outcome should be that argument  $D$  is justified. However, it is quite easy to provide another example, with essentially the same structure, where the desired outcome is totally different.

**example 3.**

*A: The suspect killed the victim by stabbing him with a knife.*

*B: The suspect killed the victim by shooting him with a gun.*

*C: The suspect is innocent.*

*D: The suspect should go to jail.*

This essentially gives the argumentation framework of Figure 7. However, an analysis of this case yields a different outcome. As essentially none of the witness statements is without doubt, none of them can serve as a good reason to refute the innocence of the suspect, and the conclusion that suspect should go to jail is definitely not an intuitive or desired one.

The main problem of working with small informal examples (like examples 2 and 3) is that they have an inherent ad-hoc nature. The use of examples for justifying a particular logic formalism is therefore criticized by researchers such as Vreeswijk [15] and Caminada [1].

It is the author’s opinion that a better justification for the design of a particular logic can be found in postulates, as these have a more general nature than separate examples. And for reasons explained earlier, we feel that Definition 5 can serve as a more intuitive and acceptable postulate for reinstatement than Definition 8. It is the author’s firm opinion that Dung’s traditional semantics have a solid basis and that one should have very good reasons for adjusting them.

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