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# A structural model of La<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub>–B<sub>2</sub>O<sub>3</sub> glasses based upon infrared and luminescence spectroscopy and quantum chemical calculations

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#### Abstract

Infrared spectra of  $20\text{La}_2\text{O}_3$ – $x\text{Nb}_2\text{O}_5$ – $(80-x)\text{B}_2\text{O}_3$ ,  $24\text{La}_2\text{O}_3$ – $x\text{Nb}_2\text{O}_5$ – $(76-x)\text{B}_2\text{O}_3$  and  $28\text{La}_2\text{O}_3$ – $x\text{Nb}_2\text{O}_5$ – $(72-x)\text{B}_2\text{O}_3$  glasses, with x=1, 5, 10, 15 and 20, have been obtained. Also, the luminescence spectrum of the  $28\text{La}_2\text{O}_3$ – $10\text{Nb}_2\text{O}_5$ – $62\text{B}_2\text{O}_3$  sample has been obtained. Density functional theory (DFT-B3LYP) calculations on clusters containing BO<sub>3</sub>, BO<sub>4</sub>, NbO<sub>6</sub>, edge-sharing NbO<sub>6</sub>–NbO<sub>6</sub>, edge-sharing NbO<sub>6</sub>–NbO<sub>6</sub> (niobyl), and corner-sharing NbO<sub>6</sub>–NbO<sub>6</sub> groups have been used to aid the infrared spectra assignments. From these data it was possible to propose a structural model for the La<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub>–B<sub>2</sub>O<sub>3</sub> glasses that is consistent with all the spectroscopic and theoretical results as well with previous luminescence study of similar samples. Briefly, this model consists of distorted NbO<sub>6</sub> octahedral groups replacing the BO<sub>4</sub> tetrahedral groups giving rise to non-bridging oxygen ions and distorted NbO<sub>6</sub> chains. These chains change from edge-sharing to corner-sharing distorted NbO<sub>6</sub> octahedra depending upon the La<sub>2</sub>O<sub>3</sub> concentration. For La<sub>2</sub>O<sub>3</sub> concentration larger than 28 mol% there seems to be a segregation of La(III) to another domain, restoring the structure observed for samples with La<sub>2</sub>O<sub>3</sub> concentrations lower than 20 mol%.

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#### 1. Introduction

Glasses of composition  $x\text{La}_2\text{O}_3$ – $y\text{M}_2\text{O}_5$ – $(100 - x - y)\text{B}_2\text{O}_3$  (M = Nb or Ta) have been developed for optical application and present interesting properties, such as, large chemical resistance and surface hardness, high refractive indices, excellent transparency in the visible–IR region and intense UV absorption. Glasses with a low M(V) contents show broad band luminescence upon UV excitation (blue for Ta and green for Nb). The in-

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crease in the M(V) concentration gives rise to energy migration among the  $MO_6^-$  groups [1].

The niobate luminescence has been extensively investigated in crystalline materials [2–6], and is strongly dependent upon the crystal structure. The most efficient luminescence occurs in niobyl groups [4], i.e., an Nb–O group with a short bond distance,  $\approx 0.17$  nm. Structurally isolated NbO<sub>6</sub> octahedra, such as in ordered perovskites and in MgNb<sub>2</sub>(P<sub>2</sub>O<sub>7</sub>)<sub>3</sub> are not efficient luminescent centers [7], whereas isolated distorted niobate groups, such as in LaNbO<sub>4</sub>, where the Nb(V) has a 4+2 coordination, provide very efficient centers [3]. Edge- or face-shared NbO<sub>6</sub> octahedral groups show efficient luminescence with a large Stokes shift,  $\Delta_{ST}$ , i.e. the energy difference between the emission and excitation

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maxima; while corner-sharing of NbO<sub>6</sub> groups leads to a shift of the optical absorption to lower energies, exciton delocalization, smaller  $\Delta_{ST}$ ; lower quenching temperatures, energy migration and consequently luminescence quenching [3].

The observation of niobate luminescence thus implies a considerable degree of short- and intermediate-range order in La<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub>–B<sub>2</sub>O<sub>3</sub> glasses. In our previous work, we observed a relationship between the luminescence and the sample composition [8]. Crystalline niobate were used as model systems for extrinsic sub-networks in glasses structures. Even in samples at 20 mol% of La<sub>2</sub>O<sub>3</sub> pairs of edge-sharing NbO<sub>6</sub> groups occur and the luminescence is typical for this structure. The increase of La<sub>2</sub>O<sub>3</sub> concentrations at 25 mol% seems to disrupt these chains of niobate edge-sharing into corner-sharing off-center units. This leads to structural changes that are reflected into the luminescence properties [8].

In this work we reported the infrared spectroscopy study that agrees with our previous work hypothesis and expands the luminescence study for a sample with 28 mol% of  $\text{La}_2\text{O}_3$ .

# 2. Experimental and computational procedures

Glass samples of  $x\text{La}_2\text{O}_3$ – $y\text{Nb}_2\text{O}_5$ – $(100 - x - y)\text{B}_2\text{O}_3$  (x = 20, 24, and 28, y = 1, 5, 10, 15 and 20) composition were prepared by melting 5 g batches at 1180 °C for 1 h, in Pt–5%Au crucibles, followed by quenching by pouring onto Pt plates at room temperature. The H<sub>3</sub>BO<sub>3</sub> was used for obtaining the B<sub>2</sub>O<sub>3</sub> and an excess of

12 wt% was added to compensate for evaporation losses. Considering that the melting temperature (1180 °C) is well below the fusion temperatures of  $La_2O_3$  (2320 °C) and  $Nb_2O_5$  (1512 °C), but larger than that of  $B_2O_3$  (450 °C), it is safe to assume that  $B_2O_3$  is the volatile species. Then, by mass differences it was shown for nine samples that the final compositions were within 0.5 mol% from the nominal ones, and for the same nominal compositions the differences were no larger than 0.04 mol%.

The samples were characterized by IR vibrational spectroscopy. The IR vibrational absorption spectra were measured on a Bruker IF566 spectrophotometer, using KBr pellet techniques.

Theoretical calculations were performed in order to aid the spectral assignments, and Fig. 1 presents the clusters used for these calculations. Structures I and II represent the BO<sub>3</sub> and BO<sub>4</sub> groups in a borate chain, respectively, whereas III, IV, V and VI contain the NbO<sub>6</sub> octahedra replacing the BO<sub>4</sub> group in the borate chain, the edge-sharing NbO<sub>6</sub> groups, the edge-sharing NbO<sub>6</sub> groups with only niobyl moiety, and the cornersharing of NbO<sub>6</sub> groups, respectively. Geometry optimizations and vibrational frequencies calculations were performed with the Gaussian 98 program [9] with the hybrid-DFT B3LYP method [10]. The basis sets employed were LANL2DZ [11] with ECP for Nb, 6-31 + G [12] for O, and 6-31G [12] for B and H atoms. All calculations were performed without any symmetry constraints and the program default criteria were used for convergence and cutoffs.

The 28La<sub>2</sub>O<sub>3</sub>–10Nb<sub>2</sub>O<sub>5</sub>–62B<sub>2</sub>O<sub>3</sub> glass sample was studied with luminescence spectroscopy. The luminescence

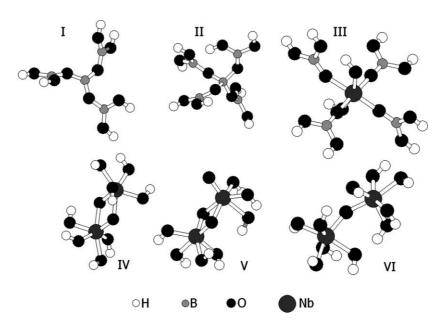


Fig. 1. Cluster models used in the calculation of the vibrational frequencies associated with BO<sub>3</sub>, BO<sub>4</sub>, NbO<sub>6</sub>, edge-sharing NbO<sub>6</sub>–NbO<sub>6</sub>, edge-sharing NbO<sub>6</sub>–NbO<sub>6</sub> (niobyl), and corner-sharing NbO<sub>6</sub>–NbO<sub>6</sub> groups.

spectra were obtained by using a SPEX Fluorolog DM3000F spectrofluorometer with double-grating 0.22 m SPEX 1680 monochromators, and a 450 W Xe lamp as the excitation source. This setup is equipped with an Oxford LF205 liquid helium flow cryostat, allowing for measurements down to 4.2 K.

#### 3. Results

Fig. 2 shows the vibrational spectra of 20La<sub>2</sub>O<sub>3</sub> glass series, and Figs. 3 and 4 present the vibrational spectra for 24 and 28La<sub>2</sub>O<sub>3</sub> glass series, respectively.

Table 1 presents the spectra assignment supported by the literature data [13,14] and the calculated vibrational frequencies.

The excitation and emission spectra of the 28La<sub>2</sub>O<sub>3</sub>–10Nb<sub>2</sub>O<sub>5</sub>–62B<sub>2</sub>O<sub>3</sub> glass sample are presented in Fig. 5.

In addition to these results obtained for the  $28La_2O_3$ –  $10Nb_2O_5$ – $62B_2O_3$  sample, Table 2 presents the luminescence results for other samples from our previous work [8] as well as for three other crystalline niobates.

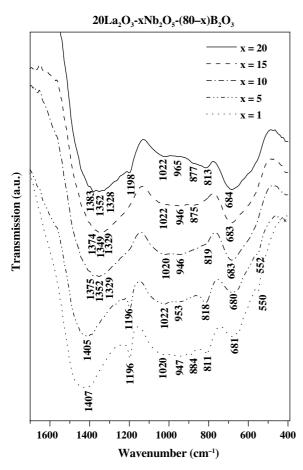


Fig. 2. Infrared spectra of  $20\text{La}_2\text{O}_3$ – $x\text{Nb}_2\text{O}_5$ – $(80-x)\text{B}_2\text{O}_3$  glasses with x=1, 5, 10, 15 and 20. The data have been plotted with a displacement in the *y*-axis (arbitrary units – a.u.) in order to improve visualization and comparison.

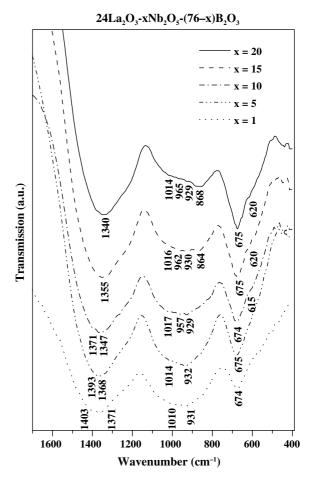


Fig. 3. Infrared spectra of  $24\text{La}_2\text{O}_3$ — $x\text{Nb}_2\text{O}_5$ — $(76-x)\text{B}_2\text{O}_3$  glasses with x=1, 5, 10, 15 and 20. The data have been plotted with a displacement in the *y*-axis (arbitrary units – a.u.) in order to improve visualization and comparison.

# 4. Discussion

All vibrational spectra present three broad bands in the 400–1700 cm<sup>-1</sup> region according to Figs. 2–4. For all three series of samples, the intensities of the BO<sub>4</sub> group stretching vibrational frequencies (1020–1030 cm<sup>-1</sup>) decrease and the intensities of the NbO<sub>6</sub> group characteristic vibrational frequencies (around 680 cm<sup>-1</sup>) increase with the increase of Nb<sub>2</sub>O<sub>5</sub> contents. These suggest that the distorted NbO<sub>6</sub> octahedra groups replace the BO<sub>4</sub> tetrahedral groups and give rise to non-bridging oxygen atoms.

Bands in the 550–560 cm<sup>-1</sup> and 810–830 cm<sup>-1</sup> regions, which are characteristics of edge-sharing niobate groups (Table 1), were observed in infrared spectra of the samples with 20 and 28 mol% of La<sub>2</sub>O<sub>3</sub> (Figs. 2 and 4), but not in spectra with 24 mol% La<sub>2</sub>O<sub>3</sub> (Fig. 3). We suppose that the increase of La<sub>2</sub>O<sub>3</sub> concentration from 20 to 24 mol% disrupts the edge-sharing NbO<sub>6</sub> pairs, but that another increase to 28 mol% of La<sub>2</sub>O<sub>3</sub> induces a phase segregation, which gives rise to a decrease of lanthanum concentration content around

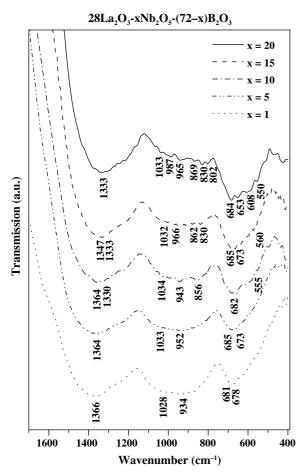


Fig. 4. Infrared spectra of  $28\text{La}_2\text{O}_3$ – $x\text{Nb}_2\text{O}_5$ – $(72-x)\text{B}_2\text{O}_3$  glasses with x=1, 5, 10, 15 and 20. The data have been plotted with a displacement in the *y*-axis (arbitrary units – a.u.) in order to improve visualization and comparison.

the niobates groups, thus increasing the formation of NbO<sub>6</sub> pair edge-sharing groups.

In order to ascertain this hypothesis we have studied the 28La<sub>2</sub>O<sub>3</sub>–10Nb<sub>2</sub>O<sub>5</sub>–62B<sub>2</sub>O<sub>3</sub> sample using luminescence spectroscopy. It is clear that if distorted octahedra

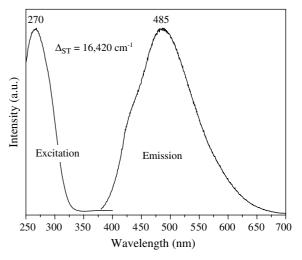


Fig. 5. Excitation and emission spectra at 4.2 K of the  $28La_2O_3-10Nb_2O_5-62B_2O_3$  sample.

connected by the edges are present in the sample, then their characteristic luminescence would be observed.

The maximum excitation ( $\lambda_{\rm exc}$ ) and emission ( $\lambda_{\rm em}$ ) wavelengths were 270 and 485 nm, respectively, yielding a Stokes shift ( $\Delta_{\rm ST}$ ) of 16420 cm<sup>-1</sup>. These results are very close to those observed for crystalline CaNb<sub>2</sub>O<sub>6</sub>, namely  $\lambda_{\rm exc} = 260$  nm,  $\lambda_{\rm em} = 460$  nm and  $\Delta_{\rm ST} = 16\,000$  cm<sup>-1</sup>, which has a columbite structure characterized by edge-sharing distorted NbO<sub>6</sub> octahedra [15].

Based upon the present vibrational and luminescence spectroscopic results as well as our previous luminescence study [8] we are now able to propose a model for the structural changes with respect to the composition of the vitreous system La<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub>–B<sub>2</sub>O<sub>3</sub>. Even at concentrations as low as 1 mol% of Nb<sub>2</sub>O<sub>5</sub> in 19–20 mol% of La<sub>2</sub>O<sub>3</sub> it is possible to observe edge-sharing NbO<sub>6</sub> groups according to the observed vibrational frequencies in the 550 and 810–820 cm<sup>-1</sup> region, which are also responsible for the observed luminescence in these

Assignments of the vibrational bands (cm<sup>-1</sup>) in the infrared spectra of borate and niobate groups

| Assignment   | Observed present work | Calculated present work | Literature [13,14]  |
|--|-----------------------|-------------------------|---------------------|
| B-O stretching in BO <sub>3</sub> groups (model I)                                 | 1330–1400             | 1320–1490               | 1220, 1330 and 1440 |
| B-O stretching in BO <sub>4</sub> groups (model II)                                | 960-1030              | 965, 1101 and 1138      | 900-1040            |
| Nb-O stretching of the terminal oxygen atoms                                       | 670-685               | 682                     | _                   |
| in the NbO <sub>6</sub> group connected to four BO <sub>3</sub> groups (model III) |                       |                         |                     |
| Nb-O symmetric stretching of the edge-sharing                                      | 800-830               | 800                     | 850                 |
| oxygen atoms in the edge-sharing NbO <sub>6</sub> groups (model IV)                |                       |                         |                     |
| Nb-O asymmetric stretching of the terminal   | 550-560               | 530                     | 500                 |
| oxygen atoms in the edge-sharing NbO <sub>6</sub> groups (model IV)                |                       |                         |                     |
| Nb=O stretching of the niobyl in the edge-sharing                                  | 860-880               | 857                     | _                   |
| NbO <sub>6</sub> groups (model V)  |                       |                         |                     |
| Nb-O-Nb symmetric stretching in the corner-sharing                                 | 608-620               | 603                     | 620 and 700         |
| NbO <sub>6</sub> groups (model VI)   |                       |                         |                     |

Table 2 Spectroscopic and structural properties at 4.2 K of crystalline and non-crystalline niobates

| Structure   | $\lambda_{em(max)}$ | $\lambda_{\mathrm{exc(max)}}$ | $\it \Delta_{ m ST}$ |
|---|---------------------|-------------------------------|----------------------|
| α-LaNb <sub>3</sub> O <sub>9</sub> – double chains of distorted NbO <sub>6</sub>                    | 535                 | 310                           | 14000                |
| octahedra which share opposite corners along the  |                     |                               |                      |
| chain and share edges across the chain, with Nb-O-Nb = 130°-155° [6]                                |                     |                               |                      |
| $CaNb_2O_6$ – columbite [15]  | 455                 | 260                           | 16500                |
| α-NbPO <sub>5</sub> – single chains of corner-sharing   | 490                 | 260                           | 18000                |
| distorted NbO <sub>6</sub> octahedra with Nb–O = $0.210 \text{ nm}$                                 |                     |                               |                      |
| and Nb–O = $0.177$ nm (niobyl), leading to  |                     |                               |                      |
| approximately isolated niobyl groups [6]  |                     |                               |                      |
| $19La_2O_3-1Nb_2O_5-80B_2O_3$   | 490                 | 280                           | 15300                |
| $19La_2O_3-10Nb_2O_5-71B_2O_3$  | 510                 | 290                           | 14800                |
| $19La_2O_3-20Nb_2O_5-61B_2O_3$  | 570                 | 340                           | 11800                |
| 25La <sub>2</sub> O <sub>3</sub> -10Nb <sub>2</sub> O <sub>5</sub> -65B <sub>2</sub> O <sub>3</sub> | 510                 | 265                           | 18100                |
| $28La_2O_3-10Nb_2O_5-62B_2O_3$  | 485                 | 270                           | 16420                |

Wavelengths (nm) at maximum of emission,  $\lambda_{\text{em(max)}}$ , and of excitation,  $\lambda_{\text{exc(max)}}$ , and Stokes shifts,  $\Delta_{\text{ST}}$ , in cm<sup>-1</sup>.

samples. As the Nb<sub>2</sub>O<sub>5</sub> concentration increases from 1 up to 20 mol%, the niobate chains and the La(III) ions, intercalated within the borate chains, are organized similarly to the structure observed in α-LaNb<sub>3</sub>O<sub>9</sub>, namely, double chains of distorted NbO<sub>6</sub> octahedra which share opposite corners along the chain, and the double chains are interconnected by single chains of corner-sharing NbO<sub>6</sub> octahedra [6]. The luminescence of the La<sub>2</sub>O<sub>3</sub>-Nb<sub>2</sub>O<sub>5</sub>-B<sub>2</sub>O<sub>3</sub> glass is then very similar to the luminescence of the crystalline  $\alpha$ -LaNb<sub>3</sub>O<sub>9</sub>, yielding the best agreement when the glass composition is 19La<sub>2</sub>O<sub>3</sub>-10Nb<sub>2</sub>O<sub>5</sub>-71B<sub>2</sub>O<sub>3</sub> as observed in Table 2. The increase of the La<sub>2</sub>O<sub>3</sub> concentration to 25 mol% causes the breakdown of the niobate chains so that the presence of edge-sharing NbO6 groups is negligible, and the resulting structure is similar to that found in crystalline α-NbPO<sub>5</sub> [6]. This latter structure can be interpreted as corner-sharing distorted NbO<sub>6</sub> octahedra single chains, where the Nb(V) ion is not perfectly centered between the two oxygen ions, leading to approximately isolated niobyl groups. Corroborating this proposal is the fact that the bands associated with the edge-sharing niobate groups are not observed in the infrared spectra of the samples containing La<sub>2</sub>O<sub>3</sub> 24 mol%, whereas bands at 620 cm<sup>-1</sup>, which are associated with corner-sharing NbO<sub>6</sub> groups, are quite intense. The further increase of the La<sub>2</sub>O<sub>3</sub> concentration to 28 mol% causes the segregation of La<sub>2</sub>O<sub>3</sub> into a distinct domain, where the excess of La(III) is probably segregated to this domain that should be structurally similar to the binary La<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glass. As a result, the effective concentration of La(III) in the borate-niobate glass decreases allowing again the formation of edge-sharing niobate chains. This would also lead to an observed luminescence similar to that of crystalline α-LaNb<sub>3</sub>O<sub>9</sub>, which can be verified in Fig. 5 and Table 2. Consistent with these results are the infrared spectra for the glass samples with La<sub>2</sub>O<sub>3</sub> at 28 mol% and Nb<sub>2</sub>O<sub>5</sub>, at concentration larger than

10 mol%, where the bands at 550 and 830 cm<sup>-1</sup>, due to the edge-sharing NbO<sub>6</sub> groups, reappear as seen in Fig. 4. Also, for these samples the band at 680 cm<sup>-1</sup> is broader compared to lower La<sub>2</sub>O<sub>3</sub> concentrations, which might suggest the presence of a band at 640 cm<sup>-1</sup> characteristic of binary La<sub>2</sub>O<sub>3</sub>–B<sub>2</sub>O<sub>3</sub> glass [1].

#### 5. Conclusions

The combination of infrared and luminescence spectroscopy with vibrational frequency calculations has provided a consistent structural model for the La<sub>2</sub>O<sub>3</sub>-Nb<sub>2</sub>O<sub>5</sub>-B<sub>2</sub>O<sub>3</sub> glasses, where distorted NbO<sub>6</sub> octahedral groups replace the BO<sub>4</sub> tetrahedral groups giving rise to non-bridging oxygen ions. For concentrations of La<sub>2</sub>O<sub>3</sub> lower than 20 mol% the results are consistent with the presence of edge-sharing distorted NbO6 octahedra chains, even for Nb<sub>2</sub>O<sub>5</sub> concentrations as low as 1 mol%. This structure is disrupted when the La<sub>2</sub>O<sub>3</sub> concentration is increased up to 28 mol%, leading to cornersharing distorted NbO<sub>6</sub> octahedra single chains with the presence of approximately isolated niobyl groups. Beyond 28 mol% of La<sub>2</sub>O<sub>3</sub> there seems to be a segregation of La(III) to a binary La<sub>2</sub>O<sub>3</sub>-B<sub>2</sub>O<sub>3</sub> glass domain, restoring the structure observed for samples with La<sub>2</sub>O<sub>3</sub> concentrations lower than 20 mol%.

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