

THERMAL-NEUTRON CAPTURE GAMMA RAYS FROM NATURAL MAGNESIUM AND ENRICHED ^{25}Mg

P. SPILLING, H. GRUPPELAAR and A. M. F. OP DEN KAMP

Fysisch Laboratorium der Rijksuniversiteit, Utrecht, the Netherlands

Received 1 June 1967

Abstract: Gamma rays from neutron capture in natural magnesium and in enriched ^{25}Mg have been studied with Ge(Li) detectors. Altogether 101 γ -rays have been observed. Most of these γ -rays could be fitted into the level schemes of ^{25}Mg , ^{26}Mg and ^{27}Mg .

The Q -values for the following reactions have been determined

$^{24}\text{Mg}(n, \gamma)^{25}\text{Mg}$	$Q = 7332.8 \pm 0.4 \text{ keV,}$
$^{25}\text{Mg}(n, \gamma)^{26}\text{Mg}$	$Q = 11096.0 \pm 0.5 \text{ keV,}$
$^{26}\text{Mg}(n, \gamma)^{27}\text{Mg}$	$Q = 6446.3 \pm 0.9 \text{ keV,}$
$^{56}\text{Fe}(n, \gamma)^{57}\text{Fe}$	$Q = 7643.9 \pm 1.5 \text{ keV,}$
$^{63}\text{Cu}(n, \gamma)^{64}\text{Cu}$	$Q = 7916.5 \pm 1.5 \text{ keV,}$
$^{207}\text{Pb}(n, \gamma)^{208}\text{Pb}$	$Q = 7371.0 \pm 2.5 \text{ keV.}$

If it is assumed that the capture cross section for natural magnesium amounts to $64 \pm 3 \text{ mb}$, the capture cross sections for ^{24}Mg , ^{25}Mg and ^{26}Mg have been determined as $52 \pm 13 \text{ mb}$, $182 \pm 50 \text{ mb}$ and $34 \pm 10 \text{ mb}$, respectively.

E

NUCLEAR REACTIONS $^{24, 25, 26}\text{Mg}$, ^{56}Fe , ^{63}Cu , $^{207}\text{Pb}(n, \gamma)$, $E = \text{thermal}$;
measured $\sigma(E_\gamma)$; deduced Q .
 $^{25, 26, 27}\text{Mg}$ deduced levels, branching. Enriched ^{25}Mg target, Ge(Li) detector.

1. Introduction

The $^{25}\text{Mg}(n, \gamma)^{26}\text{Mg}$ reaction has been investigated very little. Yet this reaction may give valuable information on the ^{26}Mg level scheme.

Preliminary measurements of γ - γ coincidence spectra and angular correlations with NaI detectors made it clear that the decay is quite complicated. Several sets of levels, situated very close together, are excited. It was felt that much better resolution was needed in order to clarify the situation.

The present paper describes an investigation of the γ -ray spectra from thermal-neutron capture in natural magnesium and in magnesium enriched in ^{25}Mg by means of Ge(Li) counters.

Prior to the present investigation, the gamma rays from neutron capture in natural magnesium had been studied with a pair spectrometer ¹⁾ and a magnetic Compton spectrometer ²⁾. Altogether 27 lines had been found. Most of these lines were fitted into the level schemes of ^{25}Mg , ^{26}Mg and ^{27}Mg , but not all of them in a satisfactory way. Several weak high-energy lines were indicated, which were not observed in the

present investigation. Most of the data known for the three magnesium isotopes are tabulated in the review article by Endt and van der Leun³).

The nucleus ^{26}Mg is rather difficult to investigate because of the many doublets and triplets appearing in the level scheme. Partly because of this, I_n value assignments from the (d, p) reaction are made difficult. Also it is found that for many levels, more than one I_n value contribute to the transitions⁴). Therefore many of the I_n values are doubtful.

By combining the results of investigations of the (t, p), (d, p) and (d, d') reactions leading to the levels in ^{26}Mg , Hinds *et al.*⁵) were able to assign spins and parities to levels up to 7 MeV. Strikingly, no negative parity state was found below 6.8 MeV.

The triplet at $E_x = 4.3$ MeV was not completely resolved in the (t, p) and (d, p) reactions, and therefore the spin assignments to these levels were difficult. However, it was shown that the upper level in this triplet certainly has $J^\pi = 2^+$. For the other two levels no unique assignments could be made. From systematics of doubly even nuclei in the neighbourhood of ^{26}Mg , one would expect a 4^+ level between 4 and 5 MeV. Thus one of the lower levels in the triplet might well have $J^\pi = 4^+$.

2. Experimental arrangement

As samples, 6 g of natural magnesium metal and 2.4 g MgO enriched to 85 % in ^{25}Mg were used. The enriched MgO was on loan from the Electromagnetic Separation Group at Harwell, England. It was placed in a thin-walled teflon container.

The samples were placed in the neutron beam emerging from one of the radial beam holes in the Dutch High Flux reactor in Petten. The thermal-neutron flux at the sample was approximately $10^7 \text{ cm}^{-2} \cdot \text{s}^{-1}$. At the position of the sample, the neutron beam was surrounded by a ^6LiF shield, absorbing scattered neutrons.

For γ -ray detection, an Ortec 1.6 cm^3 Ge(Li) detector, 4 mm thick and a RCA 5 cm^3 Ge(Li) detector, 7 mm thick, were used. The detectors were placed approximately 10 cm from the centre of the neutron beam, with the depletion layer perpendicular to the incoming γ -rays.

The initial measurements with the Ortec detector were performed with an Ortec 109 preamplifier, main amplifier, biased amplifier and stretcher, and an Intertechnique 400-channel analyser. For the RCA detector, the electronics consisted of an Ortec 109 preamplifier, a Nuclear Enterprises main amplifier, biased amplifier and stretcher, and an Intertechnique 4096-channel analyser with a 2048-channel A.D.C. The resolution obtained with the last system was 5 keV at 1 MeV and about 12 keV at 7 MeV. The overall stability of the system was quite good. This has been checked by recording spectra of radioactive sources before and after each run. Over a period of four days, it was found that for strong peaks situated in the upper half of the spectrum, the fluctuations in the peak positions were not greater than about 0.5 channels. This corresponds to an uncertainty in the energy calibration of less than 0.5 keV for energies below 3 MeV.

For good γ -ray energy determinations, the knowledge of the response function of the spectrometer is of utmost importance. The response function can be determined in two ways. One way is to use γ -ray sources with accurately known energies. This is only applicable, however, up to about 3 MeV. To extend the method to higher energies, one can, in a spectrum of neutron-capture γ -rays, make use of the reaction Q -value. Gamma-ray energies, summing up to the neutron binding energy, can then be used to determine the response function at higher energies. This method is not very accurate, because one relies on Q -values which are not known to better than 3-5 keV.

The other way to determine the response function of the system is with a precision pulse generator. The detector is then, of course, not included, and one has to assume a linear relationship between the energy dissipated in the detector and the charge appearing at the input of the preamplifier. The system has to be calibrated with accurately known energies, and then by means of the response function one can interpolate and extrapolate to all energies in the measured spectrum.

A precision pulse generator has been built, with a deviation from linearity less than 4×10^{-5} . With the pulse generator, the response function for the system was determined, and found to be slightly S-shaped. This shape could be fitted very well to a polynomial of the third degree

$$P = \sum_{i=0}^3 a_i c^i, \quad (1)$$

where P stands for pulse height and c for the corresponding channel number.

The pulse generator can be calibrated with γ -rays of accurately known energies, E_γ ,

$$E_\gamma = B_0 + B_1 P. \quad (2)$$

The constants a_i , B_0 and B_1 are found by least-squares fitting of eqs. (1) and (2) to the measured data with a computer. Before and after a measurement, calibration was performed with the pulse generator and with radioactive sources. The average of these runs has been used in the fitting procedure. Table 4 gives the energies of the γ -rays used for calibration.

The full-energy, single and double-escape efficiency was determined with radioactive sources with known intensities, and with the γ -rays from the reactions $^{32}\text{Si}(n, \gamma)^{33}\text{S}$ and $^{35}\text{Cl}(n, \gamma)^{36}\text{Cl}$. The intensities of the dominant lines from these two reactions were previously determined with a scintillation detector ⁶⁾ and with a magnetic Compton spectrometer ⁷⁾.

3. Results and discussion

Gamma rays from neutron capture in natural magnesium have been measured with the 5 cm³ Ge(Li) detector in three runs, covering the ranges $E_\gamma = 0$ -3.5 MeV, 0-7.2 MeV and 5-12 MeV. Non-overlapping parts of these spectra for energies up to 8.3 MeV are shown in fig. 1. Above this energy no γ -ray peaks were observed.

Gamma rays from neutron capture in ^{25}Mg have been measured with the 1.6 cm³

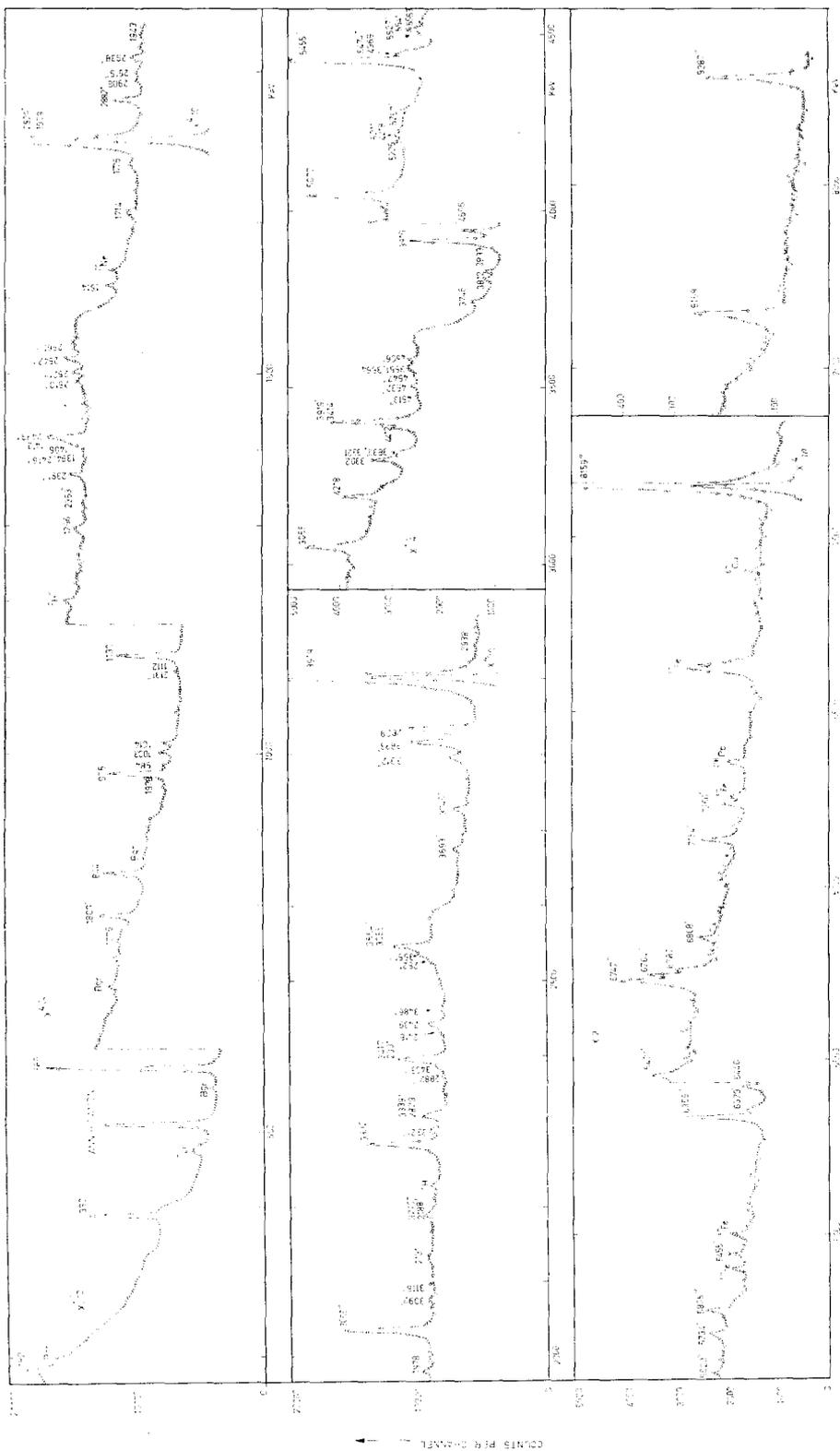


Fig. 1. Spectra of γ -rays following neutron capture in natural magnesium. All peaks are labelled with their energies in keV. Full-energy, single-escape and double-escape peaks have been indicated by unprimed, primed and double-primed energies, respectively. Background peaks from unknown origin have been labelled with "Bgr". Where it has been possible to trace the origin, the background peak has been labelled with the corresponding nucleus. All energies have been corrected for recoil loss.

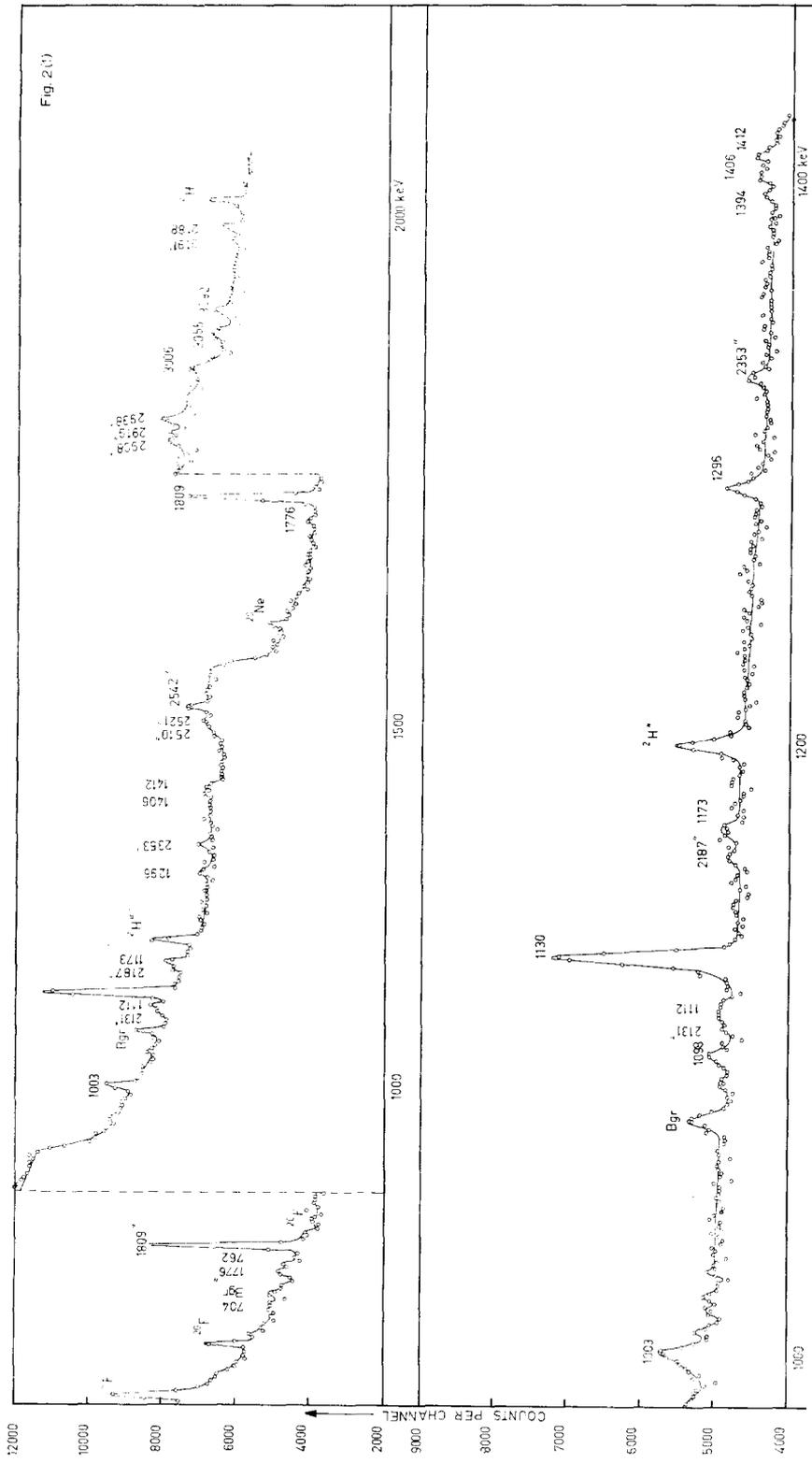


Fig. 2a. See fig. 2b.

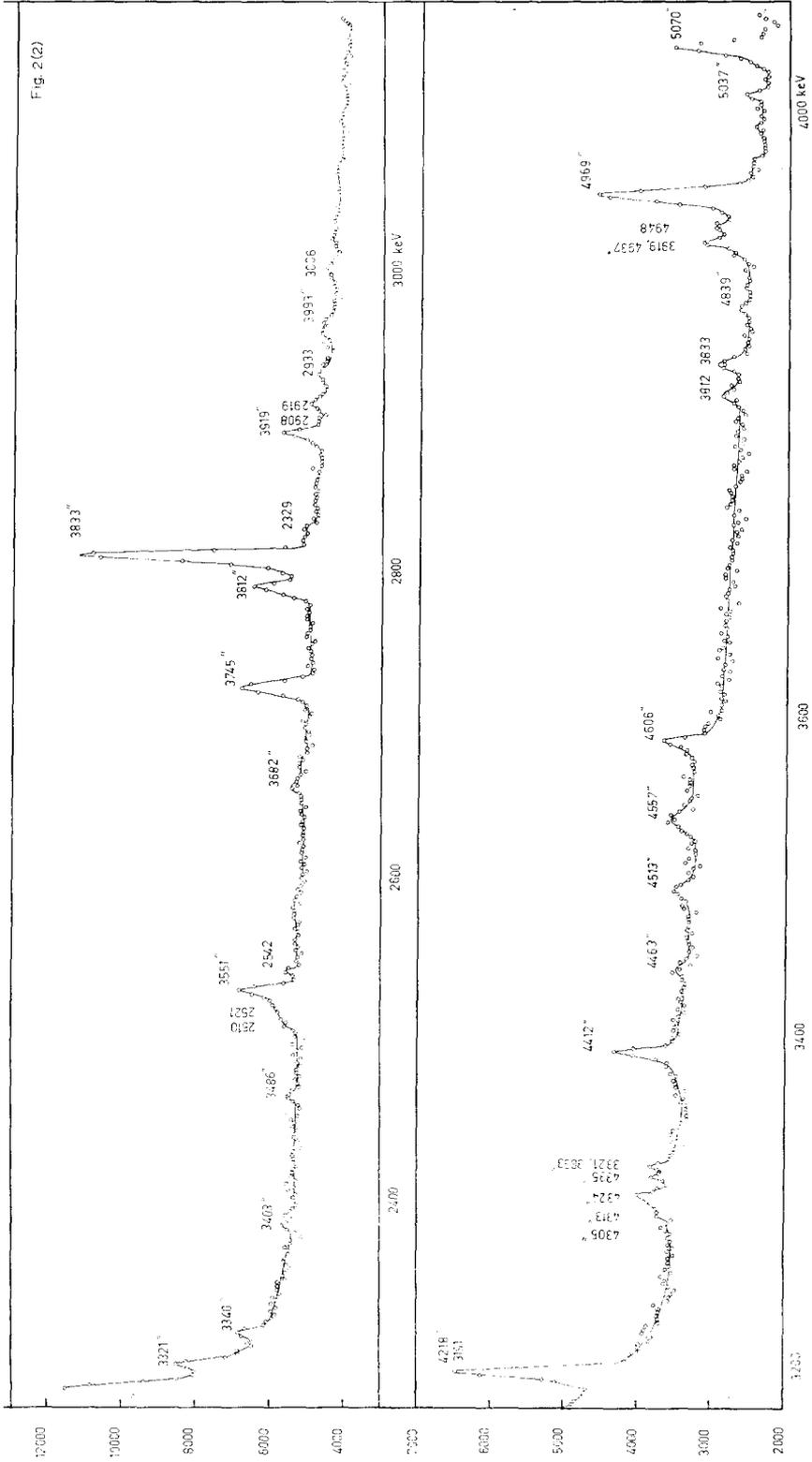


Fig. 2b. Spectra of γ -rays following neutron capture in ^{25}Mg . All the remarks for fig. 1 are also valid here.

TABLE 1

Gamma rays from thermal-neutron capture in natural magnesium and in ^{25}Mg . All energies are corrected for recoil loss

E_γ (keV)	Relative intensity	Final Mg isotope	Probable transition (E_x in keV)
182.0 \pm 0.3	20 \pm 5		
389.7 \pm 0.3	420 \pm 60	25	975 \rightarrow 585
511.0 \pm 0.3	2100 \pm 300		annihil. rad.
585.2 \pm 3.0	2000 \pm 300	25	585 \rightarrow 0
704.0 \pm 3.0	10 \pm 5	26	
762.4 \pm 3.0	10 \pm 5	26	4350 \rightarrow 3585
844.1 \pm 0.3	140 \pm 20	$^{27}\text{Mg}(\beta^-)^{27}\text{Al}$	844 \rightarrow 0
974.7 \pm 0.3	410 \pm 60	25	975 \rightarrow 0
984.1 \pm 0.5	60 \pm 10	27	984 \rightarrow 0
1002.9 \pm 0.5	110 \pm 15	26	3941 \rightarrow 2938
1014.3 \pm 0.5	70 \pm 10	$^{27}\text{Mg}(\beta^-)^{27}\text{Al}$	1014 \rightarrow 0
1097.6 \pm 1.0	15 \pm 5	26	
1112.0 \pm 3.0	15 \pm 5	26	
1129.5 \pm 0.3	525 \pm 80	26	2938 \rightarrow 1809
1172.6 \pm 2.0	10 \pm 5	26	5485 \rightarrow 4313
1296.1 \pm 1.0	35 \pm 5	26	8179 \rightarrow 6879
1394.1 \pm 2.0	20 \pm 10	26	4331 \rightarrow 2938
1405.7 \pm 2.0	25 \pm 10	26	
1411.5 \pm 2.0	75 \pm 10	26	4350 \rightarrow 2938
1613.7 \pm 1.5	115 \pm 20	25	1614 \rightarrow 0
1713.7 \pm 1.0	80 \pm 10	25	4277 \rightarrow 2562
1775.8 \pm 2.0	120 \pm 30	26	3585 \rightarrow 1809 6127 \rightarrow 4350 7262 \rightarrow 5485
1808.8 \pm 0.5	1060 \pm 160	26	1809 \rightarrow 0
1942.5 \pm 2.0	20 \pm 10	(27)	(1942 \rightarrow 0)
1977.6 \pm 2.0	70 \pm 10	25	2562 \rightarrow 585
2131.3 \pm 2.0	70 \pm 15	26	3941 \rightarrow 1809
2187.5 \pm 2.0	40 \pm 20	26	6127 \rightarrow 3941
2352.5 \pm 1.5	35 \pm 10	26	5291 \rightarrow 2938
2390.8 \pm 1.0	50 \pm 10		
2416.0 \pm 2.0	20 \pm 10		
2438.7 \pm 1.0	275 \pm 40	25	3414 \rightarrow 975
2509.9 \pm 1.0	40 \pm 10	26	
2521.4 \pm 1.5	80 \pm 10	26	4331 \rightarrow 1809
2541.8 \pm 1.0	60 \pm 10	26	4350 \rightarrow 1809
2561.1 \pm 1.5	15 \pm 10	25	2562 \rightarrow 0
2828.8 \pm 0.3	1450 \pm 220	25	3414 \rightarrow 585
2882.4 \pm 0.3	130 \pm 20	27	C \rightarrow 3564
2908.3 \pm 1.5	25 \pm 5	26	C \rightarrow 8188
2918.5 \pm 1.5	30 \pm 10	26	C \rightarrow 8179
2937.7 \pm 1.5	50 \pm 10	26	2938 \rightarrow 0
3005.5 \pm 1.5	30 \pm 10	26	
3054.5 \pm 0.5	465 \pm 70	25	C \rightarrow 4277
3092.0 \pm 2.0	15 \pm 5	26	
3116.0 \pm 2.0	65 \pm 30	(27)	(3116 \rightarrow 0)
3191.0 \pm 2.0	10 \pm 5	26	7543 \rightarrow 4350

TABLE 1 (continued)

E_γ (keV)	Relative intensity	Final Mg isotope	Probable transition (E_x in keV)
3210.0±2.0	25± 5	26	7543 → 4331
3302.0±0.5	360± 35	25	4277 → 975
3321.0±1.0	40± 15	26	7262 → 3941
3340.0±1.5	25± 5	26	7281 → 3941
3403.0±2.0	10± 5	26	
3414.6±1.0	125± 30	25	3414 → 0
3486.0±2.0	5± 4	26	
3551.4±1.5	60± 10	26	C → 7543
3563.8±1.5	170± 35	27	3564 → 0
3681.5±3.0	10± 5	26	7262 → 3585
3692.9±1.5	55± 10	25	4277 → 585
3745.8±1.5	65± 10	26	C → 7350
3812.3±0.7	50± 10	26	C → 7281
3833.1±0.7	240± 35	26	C → 7262
3918.6±0.7	1900±300	25	C → 3414
3993.2±3.0	10± 5	26	
4128.4±0.7	70± 10	26	C → 6879
4305.0±2.0	4± 2	26	
4313.0±3.0	7± 2	26	4313 → 0
4324.0±2.0	20± 5	26	7262 → 2938
4336.0±2.0	10± 3	26	
4412.5±1.5	45± 7	26	7350 → 2938
4462.9±2.0	6± 2	26	
4513.2±2.0	15± 3	26	
4531.5±1.0	15± 3		
4557.0±1.5	20± 3	26	
4606.2±1.0	20± 3	26	7543 → 2938
4889.1±2.0	4± 2	26	
4937.0±1.0	25± 5	26	
4948.0±2.0	20± 5	26	
4969.1±1.0	90± 15	26	C → 6127
5036.8±1.5	7± 2	26	
5070.2±1.5	50± 10	26	6879 → 1809
5225.0±1.5	6± 8		
5240.6±2.0	6± 2	26	8179 → 2938
5256.6±3.0	15± 3	26	
5455.0±1.0	115± 15	26	7262 → 1809
5473.5±1.5	5± 2	26	7281 → 1809
5526.5±2.0	10± 4		
5540.8±1.5	20± 5	26	7350 → 1809
5558.2±2.0	6± 2	26	
5622.2±1.5	4± 2		
5733.6±1.5	4± 2	26	7543 → 1809
5804.5±1.5	15± 3	26	C → 5291
6358.7±1.0	50± 8	25	C → 975
6379.0±1.5	12± 3	26	8188 → 1809
6446.3±1.5	20± 4	27	C → 0
6470.2±1.5	8± 2		

TABLE 1 (continued)

E_γ (keV)	Relative intensity	Final Mg isotope	Probable transition (E_x in keV)
6746.7 ± 1.0	40 ± 5	} 25 } 26	C \rightarrow 585
6763.7 ± 1.5	12 ± 2		C \rightarrow 4350
6781.8 ± 3.0	3 ± 1	26	C \rightarrow 4331
6867.7 ± 2.0	2 ± 1	26	C \rightarrow 4313
7154.3 ± 1.5	5 ± 2	26	C \rightarrow 3941
7255.7 ± 2.0	5 ± 2	26	
8159.0 ± 1.0	180 ± 25	26	C \rightarrow 2938
9286.9 ± 1.0	40 ± 5	26	C \rightarrow 1809

The errors in the energies are mainly due to errors made in reading-off peak positions. The errors in the intensities are partly due to statistics, partly due to uncertainties in the efficiency curves for the detector. The efficiency curves are believed to be true to within 15%. The intensities given all refer to capture in natural magnesium.

Ge(Li) detector and a 400-channel analyser. Four of these spectra, covering the range $E_\gamma = 0-5$ MeV, are shown in fig. 2.

The peaks are labelled with unprimed, primed and double-primed energies in keV, indicating full-energy, single and double-escape peaks. All energies were corrected for recoil loss. Where it has been possible to trace the origin of a background peak, the peak has been labelled with the corresponding final nucleus, otherwise only with "Bgr".

The background radiation originates from neutron capture in the iron and lead shielding around neighbouring neutron diffraction experiments, from neutron capture in a copper monochromator in one of the diffraction experiments and from neutron capture in the teflon target holder. In order to get a better understanding of the background radiation, separate measurements of γ -rays from neutron capture in iron, copper and teflon have been performed.

In table 1, all observed γ -rays which can be assigned to capture in one of the three magnesium isotopes or to the $^{27}\text{Mg}(\beta^-)^{27}\text{Al}$ decay, are listed. In the determination of energies, three types of errors have been considered. These are, errors made in reading-off peak positions, errors due to the differential non-linearity of the analyser and errors made in calibrating spectra. Only the first type of errors has been found to be of importance for this investigation. This conclusion was based on several considerations. For strong lines in the measured spectra, where both full-energy and double-escape peaks were seen, one finds the correct energy difference, 1022 keV. One can compare the Q -values determined in the present paper, with those calculated from the 1964 mass table¹⁴) and with recent determinations of Q -values from the reactions $^{56}\text{Fe}(n, \gamma)^{57}\text{Fe}$, $^{63}\text{Cu}(n, \gamma)^{64}\text{Cu}$ and $^{207}\text{Pb}(n, \gamma)^{208}\text{Pb}$ (ref. 15)). The comparison is shown in table 3. The agreement is very good. Also, one finds good internal agree-

TABLE 2

Q -values for the reactions $^{24}\text{Mg}(n, \gamma)^{25}\text{Mg}$, $^{26}\text{Mg}(n, \gamma)^{26}\text{Mg}$ and $^{26}\text{Mg}(n, \gamma)^{27}\text{Mg}$ found by calculating the weighted average of the sums of γ -ray energies in cascades between capturing state and ground state in the three isotopes ^{25}Mg , ^{26}Mg and ^{27}Mg

$^{24}\text{Mg}(n, \gamma)^{25}\text{Mg}$	
6746.7+ 585.2	= 7331.9±1.0
6358.7+ 974.7	= 7333.4±1.0
3918.6+3414.6	= 7333.2±0.8
3918.6+2828.8+ 585.2	= 7332.6±1.3
3918.6+2438.7+ 974.7	= 7332.0±1.2
3054.5+3692.9+ 585.2	= 7332.6±1.6
3054.5+3302.0+ 974.7	= 7331.2±0.8
weighted average	7332.8

internal error 0.5

external error 0.4

Adopted value: $Q = 7332.8 \pm 0.5$ keV.

All energies are in keV. The internal and external errors have been calculated in every case, and it was always found that the internal errors are bigger than the external errors. This should indicate that the estimated errors in the measured energies are too big. The internal errors have been chosen as errors in the Q -value.

$^{25}\text{Mg}(n, \gamma)^{26}\text{Mg}$	
Cascades to $^{26}\text{Mg}(1)$	
9286.9	= 9286.9±1.0
8159.0+1129.5	= 9288.5±1.0
7154.3+2131.3	= 9285.6±2.5
6763.7+2521.4	= 9285.1±2.1
6746.7+2541.8	= 9288.5±2.2
4218.4+5070.2	= 9288.6±1.7
3833.1+5455.0	= 9288.1±1.2
3812.3+5473.5	= 9285.8±1.7
3745.8+5540.8	= 9286.6±2.1
3551.4+5733.6	= 9285.0±2.1
2908.3+6379.0	= 9287.3±2.1
weighted average	9287.3

internal error 0.5

external error 0.4

Energy difference between the capturing state and the first excited state is 9287.3 ± 0.5 keV.

Cascades to $^{26}\text{Mg}(2)$	
8159.0	= 8159.0±1.0
7154.3+1002.9	= 8157.0±1.6
6763.7+1394.1	= 8157.8±2.5
6746.7+1411.5	= 8158.2±2.8
5804.5+2352.5	= 8157.0±2.1
4969.1+2187.5+1002.9	= 8159.5±2.3
3833.1+4324.0	= 8157.1±2.1
3833.1+3321.0+1002.9	= 8157.0±1.3
3812.3+3340.0+1002.9	= 8155.2±1.7
3745.8+4412.5	= 8158.3±2.1
3551.4+4606.2	= 8157.6±1.8
2918.5+5240.6	= 8159.1±2.5
weighted average	8157.8

internal error 0.5

external error 0.4

Energy difference between the capturing state and the second excited state is 8157.8 ± 0.5 keV.

9287.3+1808.8	= 11096.1 \pm 0.7
8157.8+2937.7	= 11095.5 \pm 1.6
8157.8+1808.8+1129.5	= 11096.1 \pm 0.8
4313.0+6781.8	= 11094.8 \pm 4.2
weighted average	11096.0

internal error 0.5

external error 0.1

Adopted value: $Q = 11096.0 \pm 0.5$ keV

	$^{26}\text{Mg}(n, \gamma)^{27}\text{Mg}$
6446.3	= 6446.3 \pm 1.5
2882.4+3563.8	= 6446.2 \pm 1.5
weighted average	6446.3

internal error 0.9

external error 0.1

Adopted value: $Q = 6446.3 \pm 0.9$ keV

TABLE 3

Comparison of Q -values measured in the present investigation with some recent determinations, and with the Q -values given in the 1964 mass table

Reaction	Present work	van Middelkoop ¹⁵⁾	1964 mass table ¹⁴⁾
$^{24}\text{Mg}(n, \gamma)^{25}\text{Mg}$	7332.8 \pm 0.4		7328.8 \pm 2.2
$^{25}\text{Mg}(n, \gamma)^{26}\text{Mg}$	11096.0 \pm 0.5		11095.0 \pm 2.4
$^{26}\text{Mg}(n, \gamma)^{27}\text{Mg}$	6446.3 \pm 0.9		6439.8 \pm 3.5
$^{56}\text{Fe}(n, \gamma)^{57}\text{Fe}$	7643.9 \pm 1.5	7645.9 \pm 3.0	7641.5 \pm 2.8
$^{63}\text{Cu}(n, \gamma)^{64}\text{Cu}$	7916.5 \pm 1.5	7916.5 \pm 2.0	7916.0 \pm 4.1
$^{207}\text{Pb}(n, \gamma)^{208}\text{Pb}$	7371.0 \pm 2.5	7369.7 \pm 3.0	7375.5 \pm 4.5

All values are in keV.

ment for the Q -values determined from cascades between the capturing state and the ground state.

The intensities given in table 1 refer to capture in natural magnesium. Intensities of lines found from capture in ^{25}Mg have been normalized to capture in natural magnesium. The errors in the intensities are partly due to statistics, and partly due to the uncertainties in the efficiency curves for the detectors. These curves are believed to be true to within 15 %.

The decay schemes of ^{26}Mg and ^{27}Mg are shown in fig. 3 and those of ^{25}Mg and the mirror nucleus, ^{25}Al , in fig. 4. The decay scheme of ^{25}Al is from ref. ³⁾, and only the part relevant to the decay in ^{25}Mg is shown. The given intensities in the three Mg isotopes are normalized such that the sum of the intensities of primary γ -rays equals 100. The same has been done for the decay of the various levels.

In fitting γ -rays into the level schemes of the three isotopes, it was required that the sum of the energies of γ -rays in a cascade going from capturing state to ground state, should be equal to the Q -value within 3 keV. In this way, most of the γ -rays in table 1 could be fitted between known levels. Comparison of the sum of the intensities of the

lines feeding a level with that of the lines by which the same level is de-excited gives a check on the consistency of the three decay schemes. For all levels in ^{25}Mg quite good agreement is found. In ^{26}Mg , the intensity sum of γ -rays feeding the two lowest levels is 20 % smaller than that of the γ -rays by which they are de-excited. This indicates that weak γ -rays leading to these two levels may have been missed. For the rest of the levels in ^{26}Mg the consistency is reasonable.

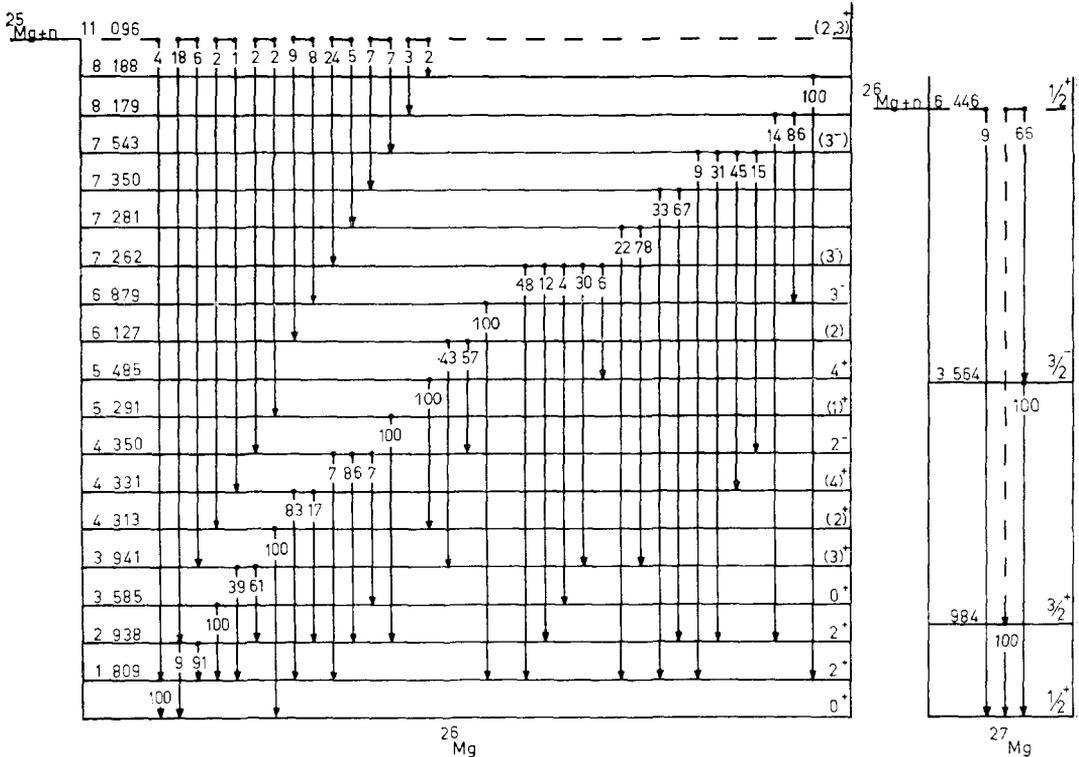


Fig. 3. Decay schemes of ^{26}Mg and ^{27}Mg . The level energies are given in keV. The intensities are normalized for each nucleus such that the intensity sum of all primary γ -rays equals 100. Spins and parities are from refs. ^{3,4,15}).

For the cascade $C \rightarrow 3564 \rightarrow 0$ in ^{27}Mg , the consistency is good. The intensity sum of ground-state transitions in ^{27}Mg and the intensity sum of ground-state transitions in the decay product ^{27}Al are approximately equal. This means that the most intense lines in the decay scheme of ^{27}Mg have been found.

Sum-coincidence measurements performed with two NaI detectors, show that the only possible two-step cascades in ^{26}Mg are those going via the first, second and fifth level.

In ^{25}Mg , four new transitions have been found. These are transitions between the following levels (in keV) $4277 \rightarrow 585$, $4277 \rightarrow 2562$, $2562 \rightarrow 0$, $2562 \rightarrow 585$.

Most of the transitions found in ^{26}Mg have not been observed before. Four high-energy lines with $E_\gamma = 11.09 \pm 0.03$, 10.08 ± 0.02 , 8.93 ± 0.02 , 8.55 ± 0.02 MeV found by Campion and Bartholomew ¹⁾, were not seen in the present investigation. They were not observed either by Groshev ²⁾. Since the detector used in the present investigation is small, it is not strange that the weak 11.09 MeV line is not seen. But the three other lines should have been observed. Either the intensities of these lines are smaller than those given in ref. ¹⁾, or the lines originate from impurities.

In ^{27}Mg , one new cascade was found, viz. $C \rightarrow 3564 \rightarrow 0$.

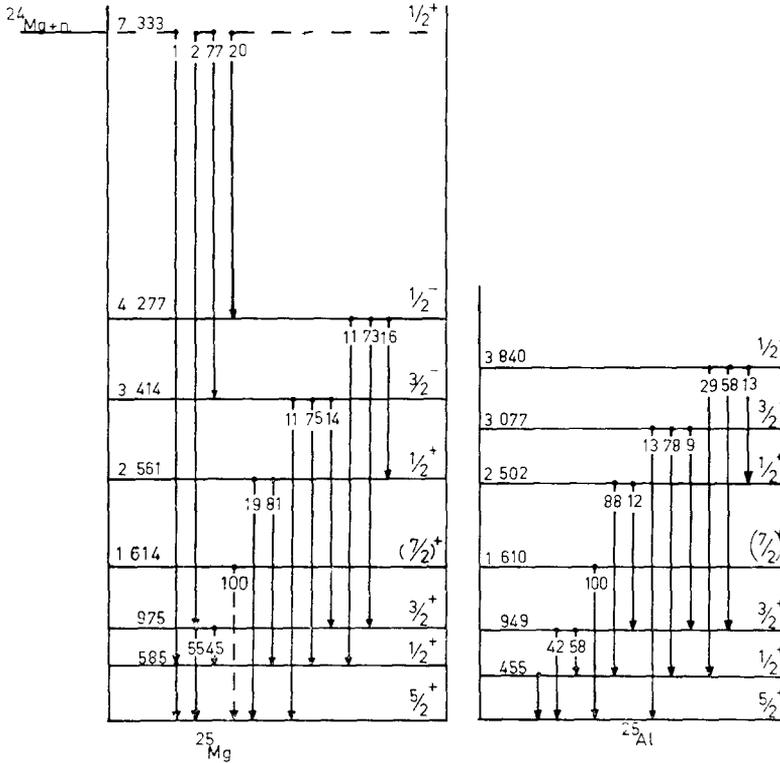


Fig. 4. Decay schemes of ^{26}Mg and ^{25}Al . The intensities of γ -rays in ^{26}Mg are normalized such that the intensity sum of primary γ -rays equals 100. The decay scheme of ^{25}Al and spins and parities are from ref. ³⁾.

Table 2 lists the cascades used for calculating the neutron binding energies for the three isotopes. For ^{25}Mg and ^{27}Mg , this has been done in a straightforward way. In ^{26}Mg , nearly all γ -ray cascades are going via the first and second excited state. Here, the weighted averaged energy differences between the capturing state and these two levels have first been calculated. In calculating the errors in the Q -values, it was always found that the internal errors were bigger than the external errors. This indicates that the estimated errors in the energies in table 1 are too big. The results of these cal-

culations are

$$\begin{aligned} {}^{24}\text{Mg}(n, \gamma){}^{25}\text{Mg}: & \quad Q = 7332.8 \pm 0.4 \text{ keV}, \\ {}^{25}\text{Mg}(n, \gamma){}^{26}\text{Mg}: & \quad Q = 11096.0 \pm 0.5 \text{ keV}, \\ {}^{26}\text{Mg}(n, \gamma){}^{27}\text{Mg}: & \quad Q = 6446.3 \pm 0.9 \text{ keV}. \end{aligned}$$

Also Q -values for neutron capture in ${}^{56}\text{Fe}$, ${}^{63}\text{Cu}$ and ${}^{207}\text{Pb}$ were determined. These Q -values are listed in table 3. For comparison, the Q -values calculated from the 1964 mass table ¹⁴), and Q -values for capture in ${}^{56}\text{Fe}$, ${}^{63}\text{Cu}$ and ${}^{207}\text{Pb}$ recently determined ¹⁵), are also listed. The agreement is quite good.

The thermal-neutron capture cross sections for the three isotopes and for natural magnesium, are measured to be 34 ± 10 mb, 280 ± 90 mb, 27 ± 5 mb and 63 ± 3 mb, respectively ³).

From these values and the abundances, one should expect for capture in natural magnesium approximately equal capture contributions in ${}^{24}\text{Mg}$ and ${}^{25}\text{Mg}$, viz. 45-50 % in each, and approximately 5 % capture in ${}^{26}\text{Mg}$. From the present investigation it follows, when one uses the intensity sum of primary γ -rays in ${}^{25}\text{Mg}$ and of ground-state γ -rays in ${}^{26}\text{Mg}$ and ${}^{27}\text{Mg}$, that the isotopic capture cross sections are

$$\begin{aligned} {}^{24}\text{Mg}(n, \gamma){}^{25}\text{Mg} &= 52 \pm 13 \text{ mb}, \\ {}^{25}\text{Mg}(n, \gamma){}^{26}\text{Mg} &= 181 \pm 50 \text{ mb}, \\ {}^{26}\text{Mg}(n, \gamma){}^{27}\text{Mg} &= 34 \pm 10 \text{ mb}. \end{aligned}$$

Excitation energies of several levels in ${}^{25}\text{Mg}$, ${}^{26}\text{Mg}$, ${}^{27}\text{Mg}$ and ${}^{27}\text{Al}$ can be determined with a precision exceeding that obtained with the (d, p) reaction ³). These energies are presented in table 5.

Since ${}^{25}\text{Mg}$ and ${}^{25}\text{Al}$ are mirror nuclei, one should expect a close relationship between the level structures of the two nuclei and between the decay pattern associated with mirror levels. It is therefore of some value to compare the decay scheme of ${}^{25}\text{Mg}$ found in the present investigation with the relevant part of the decay scheme of ${}^{25}\text{Al}$ found in ref. ³). The two decay schemes are shown in fig. 4. One can see that the branching ratios for the two negative parity states in ${}^{25}\text{Mg}$ are in good agreement with those for the corresponding states in ${}^{25}\text{Al}$. Poor agreement is found for the branching ratios for the two mirror levels at $E_x = 2.5$ MeV. In ${}^{25}\text{Al}$ this level has transitions to the first and second excited state and a very weak transition to the ground state. The mirror level in ${}^{25}\text{Mg}$ has only transitions to the ground state and the first excited state. The main part of the decay of these two mirror levels goes to the first excited states. The disagreement in the decay of these levels may perhaps partly be ascribed to the fact that transitions between intrinsic states in ${}^{25}\text{Mg}$ are due to a single neutron jump, while those in ${}^{25}\text{Al}$ are due to a single proton jump.

Theoretical investigations of the level structures of ${}^{25}\text{Mg}$ and ${}^{25}\text{Al}$ (refs. ^{18,19}) show that it is possible to construct rotational bands based on the mirror levels at

$E_x = 2.5$ MeV. These rotational bands may be strongly perturbed by the overlapping negative parity rotational band based on the $\frac{3}{2}^-$ levels shown in fig. 4. This perturba-

TABLE 4
Energies of γ rays used for calibration

Isotope	E_γ (keV)	Ref.
^{57}Co	122.05 ± 0.05	8)
ann. rad.	511.006 ± 0.002	9)
^{137}Cs	661.595 ± 0.076	10)
^{54}Mn	834.84 ± 0.07	11)
^{88}Y	898.01 ± 0.07	11)
^{60}Co	1173.226 ± 0.040	12)
^{22}Na	1274.52 ± 0.07	11)
^{60}Co	1332.483 ± 0.046	12)
^{24}Na	1368.526 ± 0.044	12)
^{88}Y	1836.08 ± 0.07	11)
$^1\text{H}(n, \gamma)^2\text{H}$	2224.5 ± 0.2	13)
^{24}Na	2753.92 ± 0.12	8)

TABLE 5
Excitation energies deduced from the present investigation

^{25}Mg	^{26}Mg
585.2 ± 0.3	1808.8 ± 0.5
974.7 ± 0.3	2938.0 ± 0.3
(1613.7 ± 1.5)	3584.7 ± 2.0
2561.8 ± 1.5	3940.5 ± 0.5
3414.0 ± 0.5	4313.0 ± 1.5
4277.4 ± 1.0	4331.0 ± 1.0
	4350.1 ± 0.5
	5290.5 ± 0.5
^{27}Mg	5485.0 ± 2.0
984.1 ± 0.5	6127.2 ± 0.8
3563.8 ± 1.5	6879.1 ± 1.5
	7262.4 ± 1.5
	7281.4 ± 0.5
	7350.1 ± 0.6
^{27}Al	7543.3 ± 0.9
844.1 ± 0.3	8178.6 ± 1.0
1014.3 ± 0.5	8187.8 ± 1.0

All energies are given in keV.

tion will also affect the decay of the levels at $E_x = 2.5$ MeV and can perhaps partly explain the observed difference. In ^{25}Mg this level has a pure E2 transition to the ground state and a pure M1 transition to the first excited state. The γ_0/γ_1 intensity

ratio is 0.23, about 20 times larger than what one would expect from the Weisskopf estimates, showing that the E2 transition is collectively enhanced.

From the results of the present investigation it was not possible to establish a transition to the level at $E_x = 1.6$ MeV. However, a γ -ray with energy 1614 keV was found and interpreted as the decay of this level to the ground state.

The branching ratios for the two mirror levels around 0.95 MeV are in agreement with each other.

The transitions found in ^{26}Mg agree with the spin and parity assignments made by Hinds, Marchant and Middleton⁵⁾, except for the 4^+ assignment to the lowest component of the triplet at $E_x = 4.3$ MeV. In the present investigation a γ -ray with energy 4313 keV was found and interpreted as the ground-state transition from this level. Therefore this level cannot have J^π equal to 4^+ as proposed, but 1^+ or 2^+ . The level is fed from a 4^+ level at $E_x = 5485$ keV and also weakly fed from the capturing state. Therefore the $E_x = 4313$ keV level may have $J^\pi = 2^+$. The middle component of the triplet was also proposed to have $J^\pi = 4^+$, and this is not in contradiction with the present results.

The levels with excitation energies higher than 6.9 MeV involved in the present investigation are not well resolved in the (d, p) reaction⁴⁾. Groups of levels in this region show $l_n = 1$ stripping patterns. One may therefore assume that most of the primary γ -rays feeding these levels have E1 character. This explains the large intensity of the $E_\gamma = 3833$ keV transition feeding the $E_x = 7262$ keV level. This level decays to the $J^\pi = 4^+$, $E_x = 5485$ keV level, the 3^+ , $E_x = 3941$ keV level, the two 2^+ levels at $E_x = 2938$ keV and 1809 keV and, weakly, to the 0^+ state at $E_x = 3585$ keV. The only possible assignment for the $E_x = 7262$ keV level seems to be $J^\pi = 3^-$. Using similar arguments one can make tentative spin and parity assignments of $J^\pi = (2, 3)^-$ to the $E_x = 7281$ keV level, $(1, 2, 3)^-$ to the $E_x = 7350$ keV level and 3^- to the $E_x = 7543$ keV level.

For the doublet at 8.2 MeV both levels may have odd parity. The lowest level in the doublet has a transition to the $J^\pi = 3^-$ level at $E_x = 6879$ keV and a weak transition to the $J^\pi = 2^+$ level at $E_x = 2938$ keV. The low-energy transition to the 3^- level may be a strongly enhanced M1 transition, and the lower level in the doublet may therefore have odd parity with spin 2 or 3. The other member of the doublet may then have odd parity with spin 1, 2 or 3.

The strong cascade found in ^{27}Mg going through the $\frac{3}{2}^-$ level at $E_x = 3564$ keV (ref. ¹⁶⁾), is in good agreement with the odd-parity assignment to this level.

An attempt was made to compare the reduced intensities of primary γ -rays feeding levels with $l_n = 1$, with the reduced widths for the same levels in the (d, p) reaction. Such a comparison can give information about the capture mechanism.

If the capture process is dominated by direct capture, one expects to find correlation between reduced E1 strengths and the reduced (d, p) widths. This is the case for capture in ^{24}Mg and ^{26}Mg . The decay of the capturing states is here dominated by E1 transitions with strengths exceeding the average E1 strength in (n, γ) reactions

found by Bartholomew¹⁷). There are strong correlations between the reduced intensities of the primary E1 transitions and the (d, p) widths of the levels they are feeding. For these two nuclei direct capture dominates.

In ^{26}Mg only one strong primary E1 transition appears with a strength approximately equal to the average E1 strength. The other primary γ -rays are weaker E1 transitions or relatively strong M1 transitions. Comparisons between reduced γ -ray intensities and reduced (d, p) widths could be made only for one level, viz. the level at $E_x = 6879$ keV. For this level the (d, p) width is large, while the E1 strength is small. This fact and the many weak primary γ -rays suggest that capture in ^{25}Mg mainly proceeds via the compound nuclear reaction or through doorway states.

It is a pleasure to thank Professor P. M. Endt for his encouragement and great interest in this work, and for his critical reading of the manuscript. It is also a pleasure to thank R. J. S. Harry for the use of his Ge(Li) detector and 4096 channel analyser.

This work has been sponsored by the Foundation for Fundamental Research on Matter (F.O.M.).

References

- 1) P. J. Campion and G. A. Bartholomew, *Can. J. Phys.* **35** (1957) 1365
- 2) L. V. Groshev, V. N. Lutsenko, A. M. Demidov and V. I. Pelekhov, *Atlas of γ -ray spectra from radiative capture of thermal neutrons* (Pergamon, London, 1959)
- 3) P. M. Endt and C. van der Leun, *Nuclear Physics* **34** (1962) 1
- 4) B. Cujec, *Phys. Rev.* **136** (1964) B1305
- 5) S. Hinds, H. Marchant and R. Middleton, *Nuclear Physics* **67** (1965) 257
- 6) G. van Middelkoop and H. Gruppelaar, *Nuclear Physics* **80** (1966) 321
- 7) L. V. Groshev, A. M. Demidov and V. N. Lutsenko, *Izv. Akad. Nauk (ser. fiz.)* **24** (1960) 833
- 8) G. T. Ewan and A. J. Tavendale, *Can. J. Phys.* **42** (1964) 2286
- 9) E. R. Cohen and J. W. M. Dumond, *Revs. Mod. Phys.* **37** (1965) 537
- 10) R. L. Graham, *Nucl. Instr.* **9** (1960) 245
- 11) W. W. Black and R. L. Heath, *Nuclear Physics* **A90** (1967) 650
- 12) G. Murray, R. L. Graham and J. S. Geiger, *Nuclear Physics* **63** (1965) 353
- 13) J. W. Knowles, *Can. J. Phys.* **40** (1962) 257
- 14) J. H. E. Mattauch, W. Thiele and A. H. Wapstra, *Nuclear Physics* **67** (1965) 32
- 15) G. van Middelkoop, *Nuclear Physics* **A97** (1967) 209
- 16) J. M. Lacambra, D. R. Tilley and N. R. Roberson, *Nuclear Physics* **A92** (1967) 30
- 17) G. A. Bartholomew, *Ann. Rev. Nucl. Sci.* **11** (1961) 259
- 18) R. K. Sheline and R. A. Harlan, *Nuclear Physics* **29** (1962) 177
- 19) A. E. Litherland, H. McManus, E. B. Paul, D. A. Bromley and H. E. Gove, *Can. J. Phys.* **36** (1958) 378